To the Graduate Council:

I am submitting herewith a dissertation written by Saumil Girish Merchant entitled “Intrinsically Evolvable Artificial Neural Networks.” I have examined the final electronic copy of this dissertation for form and content and recommend that it be accepted in partial fulfillment of the requirements for the degree of Doctor of Philosophy, with a major in Electrical Engineering.

_________________________
Gregory D. Peterson, Major Professor

We have read this dissertation and recommend its acceptance:

_________________________
Donald W. Bouldin

_________________________
Itamar Elhanany

_________________________
Ethan Farquhar

_________________________
J. Wesley Hines

Accepted for the Council:

_________________________
Carolyn R. Hodges

Vice Provost and Dean of the Graduate School

(Original signatures are on file with official student records.)
INTRINSICALLY EVOLVABLE
ARTIFICIAL NEURAL NETWORKS

A Dissertation Presented for the
Doctor of Philosophy
Degree
The University of Tennessee, Knoxville

Saumil Merchant
August 2007
DEDICATION

This dissertation is dedicated to my wife, Jaya

for her love and support and

to my parents, Kokila and Girish Merchant

for their love and encouragement.
ACKNOWLEDGEMENTS

I have been fortunate to have so many people in my life who have been a part of my graduate education and without them this dissertation wouldn't have been possible. I am what I am today because of all these people.

First and foremost, I would like to thank my advisor and teacher, Dr. Gregory Peterson. I couldn't have wished for a better mentor who was always able to help me see the bigger picture and create a vision for this dissertation. His faith in me has inspired me, and his patience and constructive criticisms have guided me. Throughout this journey he has been a friend and a mentor with my best interest in his mind. He has molded an aspiring student from a novice to a researcher.

I would also like to express my sincere thanks to Dr. Seong Kong for his guidance, Dr. Donald Bouldin for his teachings on VLSI systems and serving on my committee. I would also like to express my heartfelt gratitude to Dr. Itamar Elhanany, Dr. Wesley Hines, and Dr. Ethan Farquhar for serving on my dissertation committee.

I would like to thank my friends and lab mates, Junqing Sun, Akila Gothandaraman, Yu Bi, Junkyu Lee, Depeng Yang, Sang Ki Park, and Wei Jiang for their valuable feedback at various times during this work. I would also like to take this opportunity to thank all my friends in Knoxville who were always there for me at times I felt I would be losing my sanity.
I would like to acknowledge and appreciate the financial support provided for this research work and my graduate studies by the Electrical and Computer Engineering Department at University of Tennessee, the National Science Foundation, and the Office of Information Technology – Lab Services.

I owe special gratitude to my parents, Kokila and Girish Merchant, who always kept faith in me, and offered unconditional support and encouragement; to my aunt and uncle, Jayshree and Sanjay Merchant for inspiration and the needed push; my sister Snehal Merchant and cousin Rahil Merchant for their support and encouragement; my niece Shweta Merchant for her affection; and my mother and father-in-law Usha and Suresh Bajaj for their trust. Thank you!

Last but not the least; I thank my best friend and wife Jaya for her enduring patience, love, and support through these years. She is the one responsible to inspire me to pursue doctoral studies. Her love has been my strength, and her faith my inspiration.
ABSTRACT

Dedicated hardware implementations of neural networks promise to provide faster, lower power operation when compared to software implementations executing on processors. Unfortunately, most custom hardware implementations do not support intrinsic training of these networks on-chip. The training is typically done using offline software simulations and the obtained network is synthesized and targeted to the hardware offline. The FPGA design presented here facilitates on-chip intrinsic training of artificial neural networks. Block-based neural networks (BbNN), the type of artificial neural networks implemented here, are grid-based networks neuron blocks. These networks are trained using genetic algorithms to simultaneously optimize the network structure and the internal synaptic parameters. The design supports online structure and parameter updates, and is an intrinsically evolvable BbNN platform supporting functional-level hardware evolution. Functional-level evolvable hardware (EHW) uses evolutionary algorithms to evolve interconnections and internal parameters of functional modules in reconfigurable computing systems such as FPGAs. Functional modules can be any hardware modules such as multipliers, adders, and trigonometric functions. In the implementation presented, the functional module is a neuron block. The designed platform is suitable for applications in dynamic environments, and can be adapted and retrained online. The online training capability has been demonstrated using a case study. A performance characterization model for RC implementations of BbNNs has also been presented.
# Table of Contents

<table>
<thead>
<tr>
<th>Chapter</th>
<th>Page</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Introduction ................................................................................................................. 1</td>
</tr>
<tr>
<td></td>
<td>1.1 Technology Overview: RC, EHW, and ANN ................................................................. 1</td>
</tr>
<tr>
<td></td>
<td>1.1.1 RC Acceleration for ANNs ............................................................................... 5</td>
</tr>
<tr>
<td></td>
<td>1.2 Dissertation Synopsis ........................................................................................... 6</td>
</tr>
<tr>
<td></td>
<td>1.3 Manuscript Organization ........................................................................................ 9</td>
</tr>
<tr>
<td>2</td>
<td>Artificial Neural Networks ......................................................................................... 11</td>
</tr>
<tr>
<td></td>
<td>2.1 Introduction to Artificial Neural Networks ........................................................... 11</td>
</tr>
<tr>
<td></td>
<td>2.2 Historical Perspective ......................................................................................... 14</td>
</tr>
<tr>
<td></td>
<td>2.3 Building Artificial Neural Networks .................................................................... 15</td>
</tr>
<tr>
<td></td>
<td>2.4 Genetic Evolution of Artificial Neural Networks ................................................... 17</td>
</tr>
<tr>
<td></td>
<td>2.5 Review of Neural Hardware Implementations ........................................................... 19</td>
</tr>
<tr>
<td></td>
<td>2.5.1 Neural Network Hardware .............................................................................. 19</td>
</tr>
<tr>
<td></td>
<td>2.5.2 Digital Neural Network Implementations ........................................................... 21</td>
</tr>
<tr>
<td></td>
<td>2.5.3 Analog Neural Hardware Implementations ........................................................... 35</td>
</tr>
<tr>
<td></td>
<td>2.5.4 Hybrid Neural Hardware Implementations ........................................................... 36</td>
</tr>
<tr>
<td></td>
<td>2.6 Summary .............................................................................................................. 37</td>
</tr>
<tr>
<td>3</td>
<td>Evolvable Hardware Systems ....................................................................................... 39</td>
</tr>
<tr>
<td></td>
<td>3.1 Gate-level, Transistor-level, and Functional-level Evolution .................................... 40</td>
</tr>
<tr>
<td></td>
<td>3.2 Review of Evolvable Hardware Systems ................................................................. 42</td>
</tr>
<tr>
<td></td>
<td>3.2.1 EHW Chips and Applications ............................................................................. 44</td>
</tr>
<tr>
<td></td>
<td>3.2.2 EHW Algorithms and Platforms .......................................................................... 49</td>
</tr>
<tr>
<td></td>
<td>3.3 Summary .............................................................................................................. 51</td>
</tr>
<tr>
<td>4</td>
<td>Block-based Neural Networks ....................................................................................... 53</td>
</tr>
<tr>
<td></td>
<td>4.1 Introduction ......................................................................................................... 53</td>
</tr>
<tr>
<td></td>
<td>4.2 Evolving BbNNs Using Genetic Algorithms .............................................................. 56</td>
</tr>
<tr>
<td></td>
<td>4.2.1 Genetic Operators ............................................................................................. 59</td>
</tr>
<tr>
<td></td>
<td>4.2.2 BbNN Encoding .................................................................................................. 61</td>
</tr>
<tr>
<td></td>
<td>4.2.3 Fitness Function ............................................................................................... 64</td>
</tr>
<tr>
<td></td>
<td>4.2.4 Genetic Evolution ............................................................................................. 65</td>
</tr>
<tr>
<td></td>
<td>4.3 Summary .............................................................................................................. 68</td>
</tr>
<tr>
<td>5</td>
<td>Intrinsically Evolvable BbNN Platform ....................................................................... 70</td>
</tr>
<tr>
<td></td>
<td>5.1 BbNN FPGA Design Details ................................................................................... 70</td>
</tr>
<tr>
<td></td>
<td>5.1.1 Data Representation and Precision .................................................................... 73</td>
</tr>
<tr>
<td></td>
<td>5.1.2 Activation Function Implementation .................................................................. 74</td>
</tr>
<tr>
<td></td>
<td>5.1.3 Smart Block-based Neuron Design .................................................................... 76</td>
</tr>
<tr>
<td></td>
<td>5.1.4 Dataflow Implementation .................................................................................. 81</td>
</tr>
<tr>
<td></td>
<td>5.2 Embedded Intrinsically Evolvable Platform ............................................................. 86</td>
</tr>
<tr>
<td></td>
<td>5.2.1 PSoC Platform Design ...................................................................................... 88</td>
</tr>
<tr>
<td></td>
<td>5.3 Fixed Point BbNN Software for Genetic Evolution ................................................... 91</td>
</tr>
<tr>
<td></td>
<td>5.4 Performance and Device Utilization Summary ........................................................ 92</td>
</tr>
<tr>
<td></td>
<td>5.5 Design Scalability ............................................................................................... 93</td>
</tr>
<tr>
<td></td>
<td>5.5.1 Scaling BbNN Across Multiple FPGAs ................................................................. 96</td>
</tr>
</tbody>
</table>
5.5.2 Scaling via Time Folding ................................................................. 96
5.5.3 Hybrid Implementation ................................................................. 97
5.6 Applications .................................................................................... 97
  5.6.1 N-bit Parity Classifier ................................................................. 97
  5.6.2 Iris Plant Classification .............................................................. 102
5.7 Summary .......................................................................................... 107

6 Online Learning With BbNNs ............................................................ 109
  6.1 Online Training Approach ........................................................... 110
  6.2 Online Evolution of BbNNs ........................................................... 115
  6.3 Case Study: Adaptive Neural Luminosity Controller .................... 118
    6.3.1 Simulation Experimental Setup .............................................. 120
    6.3.2 Adaptive BbNN Predictor ..................................................... 124
  6.4 Summary ....................................................................................... 156

7 Performance Analysis .......................................................................... 157
  7.1 Computational Device Space ....................................................... 157
  7.2 RP Space ....................................................................................... 159
  7.3 Performance Characterization Metrics .......................................... 162
    7.3.1 Computational Device Capacity .......................................... 163
    7.3.2 Computational Density ....................................................... 165
    7.3.3 Power Efficiency .............................................................. 166
    7.3.4 Discussion ....................................................................... 167
  7.4 BbNN Performance Analysis ......................................................... 168
    7.4.1 Performance Characterization on Processors ....................... 169
    7.4.2 Performance Characterization on FPGAs ............................. 172
    7.4.3 Results and Discussion ..................................................... 177
    7.4.4 Performance of SBbNs ....................................................... 186
  7.5 Model Sensitivity to Parametric Variations ................................. 187
  7.6 Summary ....................................................................................... 190

8 Summary and Conclusions ................................................................. 191

References ............................................................................................ 198
Appendix ............................................................................................... 214
Vita ........................................................................................................ 218
LIST OF TABLES

Table 1  Typical FPGA runtime reconfiguration times .................................................... 29
Table 2  Device Utilization Summary on Xilinx Virtex-II Pro FPGA (XC2VP30) ........... 94
Table 3  Device Utilization Summary on Xilinx Virtex-II Pro FPGA (XC2VP70) ....... 95
Table 4  Genetic evolution parameters used for $N$-bit Parity problem ........................ 98
Table 5  Genetic evolution parameters used for Iris classification problem ................. 104
Table 6  Light and sensor specifications for the test room ............................................ 123
Table 7  Genetic evolution parameters used for BbNN predictor ............................... 127
Table 8  GA evolution parameters used for BbNN controller ..................................... 140
Table 9  Re-train cycle times ....................................................................................... 147
Table 10 Peak Computational Capacity (in $MCPS$) and density (in $CP\lambda^2$) of RISC processors for BbNN block computation ......................................................... 171
Table 11 BbNN Computational Density on FPGAs ................................................... 176
LIST OF FIGURES

Figure 1  Venn diagram showing the technology overlaps between RC, EHW, and ANN .......................... 6
Figure 2  (a) Block-based neural network topology (b) 2 input / 2 output neuron block configuration ............................................. 8
Figure 3  Mathematical model of an artificial neuron .................................................................................. 11
Figure 4  (a) Non-recurrent multilayer perceptron network (b) Recurrent artificial neural network ............................................................................................................................. 12
Figure 5  Multilayer Perception Example (a) Training Iteration ‘n’ (b) Training iteration ‘n+1’ .................................................. 17
Figure 6  Neural network hardware classification ......................................................................................... 21
Figure 7  Block-based Neural Network topology .......................................................................................... 54
Figure 8  Four different internal configurations of a basic neuron block ...................................................... 54
Figure 9  Three different 2 x 2 BbNN network structures ........................................................................ 56
Figure 10 Flowchart depicting genetic evolution process ............................................................................ 58
Figure 11 Recurrent BbNN network structure encoding (a) BbNN (b) Structure encoding .......................................................... 62
Figure 12 Feedforward BbNN network structure encoding (a) BbNN (b) Structure encoding .......................................................... 62
Figure 13 BbNN weight gene encoding (a) Neuron block (b) Weight encoding ........................................... 63
Figure 14 BbNN chromosome encoding for a 2 x 2 network ........................................................................ 63
Figure 15 Structure crossover operation in BbNN .................................................................................... 66
Figure 16 Structure mutation operation in BbNN ..................................................................................... 67
Figure 17 Activation function LUT illustration ........................................................................................... 76
Figure 18 Smart Block-based Neuron to emulate all internal neuron block configurations ........................................................................... 78
Figure 19 Bit fields of Block Control and Status Register (BCSR) of SBbN ................................................. 79
Figure 20 Dynamic gene translation logic for internal configuration emulation ........................................ 80
Figure 21 Equivalent Petri Net models for BbNN blocks (a) 1/3 (b) 2/2 (c) 3/1 ........................................ 83
Figure 22 An example 2 x 2 BbNN firing sequence ................................................................................. 84
Figure 23 SBbN neuron logical block diagram .......................................................................................... 85
Figure 24 Programmable System on a Chip - logical diagram ...................................................................... 89
Figure 25 BbNN PSoC platform. GA operators execute on PPC405 ......................................................... 91
Figure 26 Fitness evolution trends for (a) 3-bit and (b) 4-bit parity examples ........................................ 99
Figure 27 Structure evolution trends for (a) 3-bit and (b) 4-bit parity examples ........................................... 100
Figure 28 Evolved networks for (a) 3-bit and (b) 4-bit parity examples .................................................. 101
Figure 29 BbNN training error for Iris plant classification database. Results show .................................. 104
Figure 30 Fitness trends was Iris plant classification using BbNN .......................................................... 105
Figure 31 Structure evolution trends for Iris plant classification using BbNN ........................................... 105
Figure 32 Evolved BbNN network for Iris plant classification database ................................................ 106
Figure 33 Single network scheduled to switch between training and active modes .................................. 111
Figure 34 Two networks scenario. One in active mode and the other in training mode .......................... 113
Figure 35 Online training system model .................................................................................................. 115
Figure 36 Time delayed neural network .................................................................................................. 117
Figure 37 Layout of the reference room used for simulation ...................................................................... 121
Figure 38  Plot of measured relative light output (%) versus ballast control input .......... 122
Figure 39  Plot of sensor signal output (V) versus measured light intensity .................. 122
Figure 40  Ideal luminosity levels in the test room......................................................... 125
Figure 41  Results of the BbNN pre-training. Plot shows the actual and the predicted
ambient luminosity values as learnt by BbNN ............................................................... 126
Figure 42  Prediction error for the offline evolution....................................................... 126
Figure 43  Average and maximum fitness values over generations (offline evolution). 127
Figure 44  Evolved BbNN after 1557 generations........................................................ 128
Figure 45  Ambient luminosity test cases and expected target luminosity..................... 129
Figure 46  Pre-trained ambient luminosity predictions and the current ambient luminosity
......................................................................................................................................... 131
Figure 47  Predictions improve after first re-training cycle at 8:00......................... 131
Figure 48  Predictions improve after the second re-training cycle at 17:50 ............... 132
Figure 49  Prediction errors for pre-trained, first re-training, and second re-training
cycles............................................................................................................................... 132
Figure 50  Average and maximum fitness trends for the first re-training cycle........ 133
Figure 51  Average and maximum fitness trends for the second re-training cycle ..... 133
Figure 52  Evolved network after the first re-training cycle....................................... 134
Figure 53  Evolved network after the second re-training cycle.................................. 135
Figure 54  BbNN predictor - controller block diagram ................................................. 140
Figure 55  Target and measured luminosity levels as recorded by the...................... 141
Figure 56  Error between target and measured luminosities (pre-trained case) ........... 141
Figure 57  Target and measured luminosity levels as recorded by the....................... 142
Figure 58  Error between target and measured luminosities (online evolution case).... 142
Figure 59  Power consumption (pre-trained case)......................................................... 143
Figure 60  Power consumption (online evolution case)............................................... 143
Figure 61  BbNN controller at time - 4:00hrs. (a) Fitness Curves (b) Evolved BbNN .. 145
Figure 62  Actual and pre-trained predictions of ambient light intensity....................... 147
Figure 63  Actual and predicted ambient light intensity values throughout the course.. 148
Figure 64  Prediction errors of all the re-training steps. The errors curves show the..... 149
Figure 65  The plot shows the prediction errors for the eighth re-training cycle and.... 150
Figure 66  Fitness curves for the evolves BbNN eighth re-training cycle..................... 150
Figure 67  Evolved BbNN network after eighth re-training cycle............................... 151
Figure 68  Target and measured luminosity reading for the sunnydataset - pre-trained
case.................................................................................................................................. 153
Figure 69  Luminosity error for the sunny dataset - pre-trained case............................... 153
Figure 70  Target and measured luminosity readings for the sunny dataset.............. 154
Figure 71  Luminosity error for the sunny case with all eight re-training cycles....... 154
Figure 72  Total power consumption for sunny case - pre-trained case....................... 155
Figure 73  Total power consumption with sunny dataset - eight re-training cycles..... 155
Figure 74  Reorganization of the VP space with advances in RP device technologies .. 162
Figure 75  RISC assembly code for a single neuron processing................................. 169
Figure 76  Pipelined multiplier accumulator circuit for neural processing ......... 173
Figure 77  Pipelined parallel multiplier circuit for neural processing ..................... 173
Figure 78  Comparing processors and FPGAs (Hard MAC) (a) Capacity (b) Density .. 178
Figure 79  Comparing processors and FPGAs (LUT MAC) (a) Capacity (b) Density .. 179
Figure 80  Comparing processors and FPGAs (Hard Multipliers) (a) Capacity (b) Density
......................................................................................................................................... 180
Figure 81  Comparing processors and FPGAs (LUT Multipliers) (a) Capacity (b) Density
......................................................................................................................................... 181
Figure 82  Comparing power efficiencies of processors and FPGAs (Hard MAC) ...... 182
Figure 83  Comparing power efficiencies of processors and FPGAs (LUT MAC) ...... 182
Figure 84  Comparing power efficiencies of processors and FPGAs (Hard Multiplier) 183
Figure 85  Comparing power efficiencies of processors and FPGAs (LUT Multiplier) 183
Figure 86  Computational capacities of FPGAs and processors as a function of network size ........................................................................................................................................ 185
Figure 87  Deviation in computational density verses die area deviation factor............ 189
1 INTRODUCTION

1.1 Technology Overview: RC, EHW, and ANN

Reconfigurable computing (RC) technology has grown considerably in the past two decades and continues to arouse much interest among the computing community. Performance advantages of dedicated custom/semi-custom implementations, shorter design and verification times, device reusability, and lower implementation costs as compared to application specific integrated circuits (ASIC) have been the major contributing factors in the success of this technology. The most prominent and commercially successful device in this technology is the field programmable gate array (FPGA). Increasing speeds and capacities, availability of on-chip cores such as embedded processors, memories, multipliers, and accumulators, and functional diversity advantages with runtime reconfiguration make FPGAs very attractive low-volume and low-cost custom hardware solutions. Increasing commercial acceptance has promoted significant research in CAD tools to efficiently program these devices and a huge market for intellectual property cores to facilitate shorter design cycles. Broad application range, from embedded computing to supercomputing, continues to stimulate research into this technology [1].

The runtime reconfiguration capability of RC devices has resulted in the conception of a different computing paradigm among a small community of researchers. The computing paradigm is Evolvable hardware (EHW) [2]. The key objective of EHW
systems is to use the runtime hardware reconfiguration ability along with evolutionary algorithms to evolve a digital or analog circuit in hardware. The configuration bitstream (viewed as a phenotype in an evolutionary algorithm) of these devices is encoded as a chromosome (viewed as a genotype) and evolved under the control of evolutionary algorithms over multiple generations. Evolutionary algorithms use mechanisms inspired by the Darwinian theory of biological evolution such as reproduction, mutation, recombination, natural selection, and survival of the fittest to evolve a population of chromosomes over multiple generations. A population of chromosomes (encoded FPGA bitstreams) is first ranked according to their fitness levels. Fitness is determined by an objective function that can include parameters such as correctness of circuit functionality, speed, area, and power. A selection scheme selects the chromosomes from the population for reproduction via genetic crossover, mutation, and recombination. The higher the rank, the higher is the probability of selection of the chromosomes for reproduction to form new generations. The survival of the fittest policy tends to increase the average fitness of the population over multiple generations. Evolution continues over multiple generations until either a chromosome with fitness at least equal to the predetermined target fitness is found or the preset maximum number of generations is reached. EHW systems are classified in two groups depending upon the role of reconfigurable hardware during evolution: intrinsic and extrinsic EHW systems. Intrinsic EHW systems include the RC hardware in the evolution loop to test the fitness of each chromosome in the population. Extrinsic EHW systems use a software model to simulate the underlying RC hardware and perform an offline evolution. Using the configuration FPGA bitstream for evolution in essence evolves the connections and configurations of the logic blocks in the hardware
circuitry. This is termed as *gate-level evolution*. Evolving hardware at a higher level of abstraction than gates is termed as *functional-level evolution*. Functional-level evolution evolves the configurations and interconnections of bigger functional modules such as multipliers, adders, and trigonometric functions. The functional modules to use for the evolution can be chosen depending on the target circuit functionality. The potential modules that can be chosen are unbounded. If the functional module chosen is an artificial neuron, the evolution process evolves the interconnections between the neurons and their internal configurations (synaptic weights and biases). Thus, the evolutionary process evolves an artificial neural network.

An *artificial neural network (ANN)* is an interconnected network of artificial neurons [3]. Artificial neurons are loosely analogous to their biological counterparts, typically producing an output that is a function of the weighted summation of synaptic inputs and a bias. ANNs can be classified as recurrent and feedforward networks depending on the flow of data from inputs to outputs of the network. Recurrent networks allow bidirectional flow between inputs and outputs, whereas in feedforward networks the data flows only in one direction, from inputs to outputs. ANNs are very popular among the machine intelligence community. They can be used to effectively model complex nonlinear input – output relationships, and to learn characteristic patterns in input data flowing through the network. They have been successfully applied to a variety of problems such as classification, prediction, and approximation in the fields of robotics, industrial control, signal/image processing, and finance. To learn the input – output relationships in the data, the ANNs go through a phase of learning or training. Many
Training algorithms exist such as the backpropagation algorithm, genetic algorithms, reinforcement learning, simulated annealing, and unsupervised training algorithms. The learning process can be broadly classified into an offline (or batch) training scheme or an online training scheme. In offline training, a batch of training datasets is used to train the neural network. The network obtained from training is then used in the field to process new data that the network has not seen during training. Online training schemes train the neural networks in the field. There are many advantages of online training with artificial neural networks such as improved generalization via adaptability in dynamic environments and system reliability. One reason for the popularity of neural networks is their ability to generalize based on the information acquired from the training datasets. But to obtain good generalizations in practice, the training dataset has to be a representative set of the real data the network is likely to encounter in the field. This is non-trivial for applications in dynamic environments where the training data may be drawn from some time-dependent environmental distributions. The ability to train the artificial neural networks in the field using online training algorithms helps to improve generalizations in dynamic environments. Improved generalizations are achieved via adaptation and re-training to learn the variations in the input data. The ability to adapt and re-train in the field maintains reliable system performance and as a result increases the system’s reliability.
1.1.1 RC Acceleration for ANNs

Inherent computational parallelism in artificial neural networks has attracted significant research into the implementation of custom hardware designs for neural networks (see chapter 2). But most implementations rely on offline training using computer simulations to find a suitable network for the training dataset. The network obtained as a result of training is then implemented in hardware to achieve higher recall speeds. Although attractive processing speedups can be achieved, every new application may necessitate a hardware redesign with this approach. To improve generalizations, networks may require more training with larger or more representative datasets. For hardware implementations relying on offline training, implementing the new trained network may require a hardware redesign. Implementation costs of hardware redesigns have attracted a lot of interest in FPGAs for implementing artificial neural networks. Runtime reconfigurations in FPGAs can be used to configure different artificial neural circuit designs, reusing the same FPGA chip for different applications. But the neural network learning process is offline. As noted above, there are many advantages to online training of artificial neural networks. To implement online training in hardware requires support for dynamic network structure and synaptic parameter updates to the neural circuit design. Online and offline learning processes for RC implementations of artificial neural networks are analogous to the intrinsic and the extrinsic functional-level evolution schemes in EHW systems. Thus, an intrinsically evolvable ANN is a custom ANN implementation that supports online learning. Figure 1 shows a Venn diagram of the technology overlaps between RC, EHW, and ANN systems as discussed above.
1.2 Dissertation Synopsis

This dissertation work is an extension of an NSF-funded project on evolvable block-based neural networks for dynamic environments. The overall project goal was algorithmic, structural, and custom implementation oriented investigation of block-based neural networks and their suitability for evolution in dynamic environments. Block-based neural networks (BbNN) are a type of artificial neural networks with a neuron block as the basic processing element of the network. The network structure is a grid with the neuron blocks positioned at the intersections of the grid. Typically the inputs are applied at the top of grid and the outputs appear at the bottom of the grid. The dataflow through the network determines the internal configurations of the neuron blocks. Each neuron block can have at the most three inputs and three outputs, aligned in north, east, west, and
south (NEWS) directions. Depending on the dataflow through the grid, the internal configurations of the neuron blocks can be 1-input / 3 outputs, 2 inputs / 2 outputs, or 3 inputs / 1 output. Every unique dataflow pattern through the grid is a unique network structure of the BbNN. Each neuron block has weighted synaptic links from all inputs to all outputs. Each output is a function of weighted summation of all the inputs and a bias. The synaptic weights and biases of the neuron blocks are the internal parameters of the network. Thus, the network outputs are unique functions of applied inputs and the internal parameters for every unique BbNN structure, as shown below.

$$y_k = f(x_{0\ldots N-1}, w_{0\ldots (10*M*N-1)}, k = 0\ldots N-1$$

where,

- $y_k$ Output $k$ of the network
- $x_{0\ldots N-1}$ $N$ inputs of the network
- $M$ Number of rows in the grid
- $N$ Number of columns in the grid
- $w_{0\ldots (10*M*N-1)}$ 10*M*N synaptic parameters (10 parameters per neuron block)
- $f(\bullet)$ Nonlinear activation function

Figure 2 shows the network architecture and a neuron block with a 2/2 (2 inputs / 2 outputs) internal configuration. Just as with other artificial neural networks, BbNNs can be applied to solve classification, prediction, and approximation problems in machine learning. The learning process for the BbNNs is a multi-parametric optimization problem to find a unique structure and a set of internal parameters to model the input – output.
Figure 2  (a) Block-based neural network topology (b) 2 input / 2 output neuron block configuration

relationships in the training datasets. Thus, global search techniques such as genetic algorithms (GAs) are used to train the BbNNs. Although GA training may take more time to converge to a solution than gradient descent search techniques such as backpropagation algorithm, it avoids getting trapped in the local minima, a problem often faced with backpropagation training algorithm. Hybrid training algorithms for BbNNs have been investigated that take the advantages of global sampling of GAs and fast convergence of gradient descent techniques for efficient training of BbNNs. More information on these can be found in [4-6]. The research work presented in this dissertation uses genetic algorithms to train the BbNNs.

This dissertation presents an intrinsically evolvable implementation of BbNNs on RC systems. The implementation supports functional-level intrinsic evolution with neuron blocks as the functional modules for the EHW system. The dissertation also
presents online learning techniques with BbNNs and performance characterization of these networks on RC systems. The major contributions from this research work are as follows:

1. RC implementation of an intrinsically evolvable platform for BbNNs. The platform supports on-chip evolution (evolutionary algorithm + BbNN on the same FPGA of BbNNs).
2. Online training algorithm to evolve BbNNs on-chip, in field enabling applications in dynamically variant environments.
3. Performance characterization of BbNNs on RC systems. The performance model presented enables quantitative and qualitative performance comparison across different computing platforms such as general purpose computing and RC systems.

1.3 Manuscript Organization

Chapter 2 introduces artificial neural networks and provides a review of reported literary contributions to neural hardware implementations. Chapter 3 introduces block-based neural networks and applies multi-parametric genetic evolution of these networks. Chapter 4 introduces block-based neural networks and provides a review of reported literary contributions to evolvable hardware systems. Chapter 5 gives the design details of the intrinsically evolvable BbNN implementation on RC systems and demonstrates the on-chip training ability of the BbNN platform. Chapter 6 provides these networks on RC systems. The major contributions from this research work are as
details on the online evolution algorithm for BbNNs. It demonstrates the advantages of online evolution using a case study, ‘Adaptive Neural Luminosity Controller’. Chapter 7 introduces a performance characterization model for BbNNs on RC systems. The model enables quantitative and qualitative performance comparison across different computing platforms. Chapter 8 concludes the dissertation providing a summary of the research work accomplished and the prospects of future research directions in the field.
2 ARTIFICIAL NEURAL NETWORKS

2.1 Introduction to Artificial Neural Networks

Artificial Neural Networks (ANN) have gained a lot of popularity in the computational intelligence and machine learning community. They are networks of fully or partially interconnected information processing elements called artificial neurons. Artificial neurons are loosely analogous to their biological counterparts. Each artificial neuron produces an output from a function of the weighted sums of inputs and a bias. The function is called an activation function or a transfer function. Typically these are nonlinear, monotonically increasing functions such as a hyperbolic tangent, logistic sigmoid, step function, or ramp function. Figure 3 shows a mathematical model of an artificial neuron.

Various network topologies proposed for the artificial neural networks can be broadly classified into recurrent and nonrecurrent networks. Recurrent networks have

![Figure 3 Mathematical model of an artificial neuron](image)

11
feedback connections from outputs back to input nodes or to one of the hidden layers. Nonrecurrent networks are feedforward networks such as the popular multilayer perceptron model. Figure 4 shows an example of recurrent and non-recurrent artificial neural networks. Neural networks can model complex nonlinear input-output relationships in a dataset. These networks are exposed to a training dataset from which they extract information and learn over time the input-output relationship in the dataset. The learning algorithm tunes the internal parameters such as weights and biases. There are three major learning paradigms: supervised, unsupervised, and reinforcement learning.

♦ *Supervised Learning*

Under supervised learning, the input data used to train the network has corresponding target output vectors that are typically used to calculate the mean squared error between the network output and target output. This error is used to guide the search in the weight space to optimize the network. It is a gradient descent search algorithm, popularly known as the backpropagation algorithm,
which tries to minimize the total mean squared error between network and target output [3].

♦ **Unsupervised Learning**

Unsupervised learning uses no external teacher and is based upon only local information. It is also referred to as self-organization, in the sense that it self-organizes data presented to the network and detects their emergent collective properties. Hebbian learning and the competitive learning are the two types of widely used unsupervised learning techniques [3].

♦ **Reinforcement Learning**

In reinforcement learning an agent learns from interaction with the environment. At every time step, the agent performs an action and the environment generates an observation and an instantaneous cost depending on the agent’s action. The environment is modeled as a Markov decision process (MDP) with sets of states and actions, and the probability distributions for costs, observations, and state-action transitions. The policy of selecting the actions is defined as a conditional distribution over actions given the observations. The aim is to discover a policy for selecting actions that minimizes some measure of a long-term cost, i.e. the expected cumulative cost [7].

Artificial neural networks are widely used in pattern classification, sequence recognition, function approximation, and prediction. Many successful artificial neural network implementations have been reported with applications in medical diagnostics, autonomously flying aircrafts, and credit card fraud detection systems.
2.2 Historical Perspective

Fascination with building machines that can demonstrate some degree of human-like intelligent behavior has driven the research efforts in the fields of artificial intelligence. Alan Turing in his classic 1950 paper in Mind, “Computing Machinery and Intelligence” laid out the test for machine intelligence, what is now famously known as the Turing test for the quality of artificial intelligence [8]. He proposed that if a machine can intelligently converse with a human such that an external observer cannot distinguish between the two, the machine is intelligent. The pursuit of intelligent machines and fascination with the human brain lead to the evolution of the fields of artificial intelligence and machine learning. In a 1943 classic paper McCulloch and Pitts described the logical calculus of neural networks, proposing that a neuron follows an all-or-none law [9]. If a sufficient number of these neurons with their synaptic connections set properly operate synchronously, then in principle it could compute any computable function. Donald Hebb, in his 1949 book The Organization of Behavior, used the McCulloch-Pitts model of neurons and presented a physiological learning rule for synaptic modifications [10]. Hebb’s learning rule suggested that the effectiveness of a variable synapse between two neurons is increased by the repeated activation of one neuron by the other across the synapse. He proposed that the connectivity of the brain is continuously changing as an organism learns differing functional tasks, and that neural assemblies are created by such changes. This view of the brain dynamically evolving its internal synaptic connections has been widely accepted and many later neural models for machine learning have adopted this functional philosophy to a varying degree. Some 15 years after the publication of McCulloch and Pitts’s classic paper on the logical calculus
of neural network models, Rosenblatt in 1958, introduced a new neural learning

of neural network models, Rosenblatt in 1958, introduced a new neural learning
technique for pattern recognition problem in his work on the perceptron [11]. In 1960,
Widrow and Hoff proposed a different training algorithm than the perceptron
convergence theorem, the least mean-square (LMS) algorithm and used it to formulate
the Adaline (adaptive linear element) [12]. One of the earliest trainable layered neural
networks with multiple adaptive elements was the Madaline (multiple-adaline) proposed
by Widrow and his students in 1962 [13]. After an initial upsurge in the research into
perceptron based neural networks came the downside after a 1969 book by Minsky and
Papert, titled ‘The Perceptron’ in which they mathematically demonstrated fundamental
limitations on what single-layer perceptrons could compute [14]. This was followed by a
decade of dormancy in the field of artificial neural networks until Hopfield’s classic
paper in 1982 brought together many older ideas that helped revive the field of artificial
neural networks [15]. Since then they have gained a lot of popularity in the computational
intelligence and machine learning community.

2.3 Building Artificial Neural Networks

To build realizable intelligent systems with artificial neural networks we need to
design networks with flexible synaptic connections capable of evolving dynamically as
the network learns new behavior. A lot of earlier work on artificial neural networks was
based on software simulations of neural network training to obtain an optimized network
which was then implemented in hardware for faster recall speeds. The trial and error
based training algorithms for these networks make application specific integrated circuit
(ASIC) implementations of on-chip training challenging. The dynamic structure and parameter updates required during training are harder to implement on an ASIC. Consider the hugely popular multilayer Perceptron (MLP) model of an ANN. The MLP is a feedforward neural network comprised of layers of artificial neurons typically trained using the backpropagation algorithm. The first layer is called the input layer, the last layer is called the output layer, and the layers in between are the hidden layers. Figure 5a shows an example of an MLP network under training at training iteration ‘n’. Assume that in the next iteration ‘n+1’ there is a change to the structure of the network; say an additional neuron has been added in the first hidden layer of the MLP. This is shown with dotted lines in Figure 5b. If this network is implemented in an ASIC for online training, additional routing nets have to be accommodated dynamically for each new neuron, which is non-trivial. Also, the numbers of inputs to the neurons in the second hidden layer of our example have increased from 4 to 5. Hence the neurons in this layer will have to either dynamically increase the number of pipeline stages in the multiply and accumulate units or add additional parallel multipliers and adders depending on the implementation of the sum of products modules for the neuron computations. This may require hardware re-synthesis and routing making the training process cumbersomely slow. These dynamic structural changes can be handled easily in software, making it an attractive choice for implementing neural network training. Providing this flexibility in an ASIC comes at a significant cost of area and speed, requiring a careful and time-consuming logic design. The costs of implementing online neural network training in an ASIC sometimes overweigh the benefits, hence encouraging software-only implementations of the training algorithms and hardware implementation of the trained
network to achieve higher connections per second (CPS) recall speeds. Section 2.5 provides a review of the neural hardware implementations reported in the literature.

2.4 Genetic Evolution of Artificial Neural Networks

The popularly used backpropagation algorithm for the training of ANNs, being a gradient descent approach, has two drawbacks as outlined by Sutton [16]. First, the search often gets trapped in local minima if the gradient step is too small, whereas for large gradient steps it could have an oscillatory behavior. The method is inefficient in searching for global minima, especially with multimodal and nondifferentiable search spaces. Second, there is a problem of catastrophic interference with these methods. There is a high level of interference between learning with different patterns, because those units that have so far been found most useful are also the ones most likely to be changed to handle new patterns. The problem of global minima can be solved by using global search procedures like genetic algorithms. Many researchers have proposed using genetic algorithms to evolve neural networks to find optimized candidates in the large deceptive
multimodal search spaces [17-25]. Genetic algorithms (GAs) evolve a population of neural networks, encoded as chromosomes over multiple generations using genetic operators such as selection, crossover, and mutation. A population of chromosomes is first ranked according to their fitness levels. The fitness is usually determined from the mean squared error between the target and the actual outputs of each individual network in the population. A selection scheme selects the chromosomes from the population based on their rankings for reproduction via genetic crossover and mutation. The survival of the fittest policy tends to increase the average fitness of the population over multiple generations. The evolution continues over multiple generations until either a chromosome with fitness at least equal to the predetermined target fitness is found or the preset maximum number of generations is reached.

GA, being a global search algorithm, avoids the pit-falls of local minima faced in gradient descent algorithms. It does not need to calculate derivatives of the error function and hence works very well with nondifferentiable error surfaces. Also there are no restrictions on network topologies as long as an appropriate fitness function can be defined for the network, network structure, and internal parameters encoded as chromosomes. Thus GA can handle a wide variety of artificial neural networks, but the evolutionary approach is a computationally intensive approach. It is also slower than the directed gradient descent based training algorithms such as the backpropagation algorithm [16]. Genetic evolution, being an adaptive process, is good at global sampling, but performs poorly for local fine tuning. If the initial guess of the network is closer in proximity on the error surface to the global minimum, the gradient descent based search
algorithm may converge much faster than a global sampling technique such as the genetic algorithms. If the neural network is more complex with multiple hidden neural layers, the error surface will be complex, with many discontinuities. In such cases, gradient descent search algorithms often will be stuck in local minima and will not converge to the global minimum, whereas, the global search techniques such as GAs are more likely to find the optimal answer.

In this work we concentrate mainly on a type of neural networks called block-based neural networks (BbNN) [23] and use GA to train the network structure and the internal parameters of the BbNNs. Chapter 4 introduces BbNNs.

2.5 Review of Neural Hardware Implementations

This section provides a brief overview of reported work in the literature for artificial neural network hardware implementations.

2.5.1 Neural Network Hardware

Dedicated hardware units for neural networks are called neurochips or neurocomputers [26]. Due to limited commercial prospects and their required development and support resources, these chips have seen little commercial viability. Also, due to the existence of wide-ranging neural network architectures and a lack of a complete and comprehensive theoretical understanding of their capabilities, most commercial neurocomputer designs are dedicated implementations of popular paradigms such as multilayer perceptrons, Hopfield networks, or Kohonen networks. Various
classification and overview studies of neural hardware have appeared in the literature [26-36]. Heemskerk has a detailed review of neural hardware implementations until about 1995 [26]. He classified the neural hardware according to their implementation technologies such as the neurocomputers built using general purpose processors, digital signal processors, or custom implementations using analog, digital, or mixed-signal design. Zhu et al. has a good survey of ANN FPGA implementations up until 2003 [36]. The neural network hardware review presented in this dissertation addresses custom hardware implementations of artificial neural networks. These are more directly related to the research presented in this manuscript. Figure 6 shows the classification structure used in this review. The reported implementations have been first broadly classified into digital, analog, and hybrid implementations. Since this dissertation focuses on digital implementations of neural network hardware a detailed review of digital implementations is presented first, followed by the analog, and hybrid implementations. The digital (ASIC and FPGA) implementations are further classified according to their implementation design choices such as representation formats for values, design flexibility to accommodate different applications of neural networks, support for on-chip or off-chip learning, and transfer function implementation.
2.5.2 Digital Neural Network Implementations

Digital neural network implementations offer high computational precision, reliability, and programmability. The implementations are targeted towards either ASICs or FPGAs. The synaptic weights and biases of the neurons in the network can be stored on or off chip, representing a trade-off between the speed and the size of the design. ASIC neurochips can achieve higher processing speeds, lower power, and more density than corresponding FPGAs implementations, but have significantly higher design and fabrication costs. FPGAs have slower processing speeds than ASICs but have the advantage of runtime circuit reconfigurations allowing reuse of the FPGA chip for
different applications. FPGAs are commercial-off-the-shelf products, lowering the implementation costs significantly. The last decade has seen a lot of advancement in reconfigurable hardware technology. FPGA chips with built-in RAMs, multipliers, gigabit transceivers, on-chip embedded processors, and faster clock speeds have attracted many neural network FPGA implementations. In general, the digital implementation disadvantages as compared to the analog implementations are relatively larger circuit sizes and higher power consumption, but digital implementations our easier to build and scale as compared to their analog counterparts.

2.5.2.1 Real Value Representation

Digital neural network hardware implementations represent the real valued weights, biases, and I/O using fixed point, floating point, or specialized representations such as pulse stream encoding. The choice of a particular representation is a trade-off between arithmetic circuit size and speed, data precision, and the available dynamic range for the real values. Floating point arithmetic units are slower, larger, and more complicated than their fixed point counterparts, which are faster, smaller, and less complicated.

Generally, floating point representations of real valued data for neural networks are found in custom ASIC implementations. Aibe et al. [37] used floating point representation for their implementation of probabilistic neural networks (PNNs). In PNNs, the estimator of the probabilistic density functions is very sensitive to the
smoothing parameter (the network parameter to be adjusted during neural network learning). Hence, a very high accuracy is needed for the smoothing parameter, making floating point implementations more attractive. Ayela et al. demonstrated an ASIC implementation of MLPs using a floating point representation for weights and biases [38]. They also support on-chip neural network training using the backpropagation algorithm and are listed also in section 2.5.2.3. Ramacher et al. present a digital neurochip called SYNAPSE-1 [39, 40]. It consists of a 2-dimensional systolic array of neural signal processors that directly implement parts of common neuron processing functions such as matrix-vector multiplication and finding maximum. These processors can be programmed for specific neural networks. All the real values are represented using floating point representation.

For FPGA implementations the preferred choice is fixed point representation. Despite the current advances in technology, the floating-point representation of real valued data may still be impractical to implement in FPGAs. Larger arithmetic circuit sizes limit the neural network sizes that can be implemented on a single FPGA [41]. Moussa, Arebi, and Nichols demonstrate an implementation of MLP on FPGAs using fixed and floating point representations. Their results show that the MLP implementation using fixed point representation was over 12x greater in speed, over 13x smaller in area, and achieves far greater processing density as compared to the MLP using floating point representations [42]. There exists a body of research to show that it is possible to train ANNs with fixed point weights and biases [42-44]. But there is a delicate trade-off between minimum precision, dynamic data range, and the area required for the
implementation of arithmetic units. A finer precision will have fewer quantization errors but requires larger multiply-accumulate units, whereas smaller bit width, lower precision arithmetic unit implementations are smaller, faster, and more power efficient. But due to lesser precision there are larger quantization errors that could severely limit the ANN’s capabilities to learn and solve a problem. There is a tradeoff between precision and area/speed, and a way to resolve this conflict is to select a ‘minimum precision’ that would be required for a target application. Holt and Baker, Holt and Hwang, and Holi and Hwang investigated the minimum precision problem on a few ANN benchmark classification problems using simulations and found 16-bit data widths with 8-bit fractional parts were sufficient for networks to learn and correctly classify the input datasets [43-45]. Ros et al. demonstrate a successful fixed point implementation of spiking neural networks on FPGAs [46]. Pormann et al. demonstrate fixed point implementations of neural associative memories, self-organizing feature maps, and basis function networks on FPGAs [47]. Some other reported implementations that used fixed point representations can be found in [48-56].

The trade-offs between fixed and floating point representations are due to area and speed of the arithmetic circuits (especially the multipliers and accumulators) required in the implementation of the neural computations. Researchers have proposed different encoding techniques that simplify the designs of the arithmetic circuits. Marchesi et al. proposed special training algorithms for multilayer perceptrons that use weight values that are powers of two. The weight constraint eliminates any need for multipliers in the ANN implementations as they are replaced with simple shifters [57]. Other approaches
encode real values in bit streams and implement the multipliers in bit-serial fashion, serializing the flow and using simple logic gates instead of complex, expensive multipliers for smaller and faster arithmetic units. But the disadvantage of using a pulse stream arithmetic approach is the precision limitation which can severely affect ANNs capability to learn and solve a problem. Also, for multiplications to be correct, the bit streams should be uncorrelated. To produce these would require independent random sources which again require larger resources to implement. Murray and Smith’s VLSI implementation of ANNs [58], used pulse-stream encoding for real values which was later adopted by Lysaght et al. [59] for ANN implementations on Atmel FPGAs. Implementation using pulse stream encoding can also be found in [60, 61]. The advantage of using serial stochastic bit streams for encoding real valued data is that the product of the two stochastic bit streams can be computed using a simple bitwise ‘xor’. Implementations using these can be found in [62-65]. Economou et al. show a pipelined bit serial arithmetic implementation for ANNs [66]. Salapura used delta encoded binary sequences to represent real values and used bit stream arithmetic to calculate a large number of required parallel synaptic calculations [67]. Zhu and Sutton [34] has a good survey of hardware implementations of artificial neural networks using pulse stream arithmetic.

Researchers have also proposed other approaches as discussed next. Chujo et al. have proposed an iterative calculation algorithm of the perceptron type neuron model, which is based on multidimensional binary search algorithm. Since binary search doesn’t need any sum of products functionality, it eliminates the need for expensive multiplier
circuitry in hardware [68]. Guccione and Gonzalez used a vector-based data parallel approach to represent real values and compute the sum of products [69]. The distributed arithmetic (DA) approach of Mintzer for implementing FIR filters on FPGAs [70] was used by Szabo et al. for a digital implementation of pre-trained neural networks. They used Canonic Signed Digit Encoding (CSD) to improve the hardware efficiency of the multipliers [71]. Noory and Groza also used the DA neural network approach and targeted their design for implementation on FPGAs [72]. Pasero and Perri use LUTs to store all the possible multiplication values in an SRAM to avoid implementing costly multiplier units in FPGA hardware. At system boot-up a microcontroller computes all the possible product values of the fixed weight and an 8-bit input vector, and loads it into the SRAM [73].

The neural network hardware implementation presented in this dissertation is on FPGAs. As discussed above floating point implementations of neural networks on FPGAs may not be practical. Larger floating point arithmetic circuits limit the size of the neural networks that can be implemented on the FPGA [41]. Also, there exists a body of research to show that it is possible to train ANNs with fixed point weights and biases [42-44]. Hence, the chosen approach chosen for representing real valued data in the neural network FPGA implementation presented in this dissertation is fixed point.
### 2.5.2.2 Design Flexibility

An important design choice for neural network hardware implementations is the degree of structure adaptation and synaptic parameter flexibility. An implementation of a neural network with fixed network structure and weights can only be used in the recall stage and cannot be adapted to different network structures and parameters without a hardware redesign. One motivation of using FPGAs for ANN implementations is the advantage of circuit adaptation using runtime reconfigurations. Runtime reconfigurations can be used to load different neural network circuit designs for different applications, reducing the implementation cost substantially by reusing the FPGA. Hardware redesigns in an ASIC are much more expensive and time consuming due to fabrication costs and time. FPGAs are used in neural network implementations for different purposes such as prototyping and simulation, density enhancement, and topology adaptation. The purpose of using FPGAs for prototyping and simulation is to thoroughly test a prototype of the final design for correctness and functionality before sending it for expensive ASIC fabrication. This approach was used in [74]. Full or partial FPGA reconfigurations can be used to implement larger circuits, which a single FPGA cannot hold, via temporal folding. This increases the amount of effective functionality per unit reconfigurable circuit area of FPGAs. Eldredge et al. used this technique to implement the backpropagation training algorithm on the FPGAs. The algorithm was divided temporally in three different executable stages and each stage was loaded on the FPGA using runtime reconfigurations. More details on this and other follow up implementations to Eldredge’s technique are covered in section 2.5.2.3 for on-chip learning [75, 76]. The runtime reconfiguration in FPGAs can also be used for topology adaptation. Neural
networks with different structure and internal parameters targeting different applications can be loaded on the FPGA via runtime reconfigurations. One of the earliest implementations of artificial neural networks on FPGAs, the Ganglion connectionist classifier, used FPGA reconfigurations to load networks with different structures for each new application of the classifier [77]. This approach to use full or partial FPGA runtime reconfigurations for structure and/or parameter adaptation can also be seen in the neural network implementations of Perez-Uribe et al. [78-80], Restrepo et al. [81], Ros et al. [46], Kothandaraman [49], Ferrer et al. [50], Chin Tsu, Wan-de, and Yen-Tsun [51], Wang et al. [52], Syiam et al. [53], Krips, Lammert, and Kummert [54], Zhu, Milne, and Gunther [55], and Kurokawa and Yamashita [82].

The approach of using FPGA runtime reconfigurations for topological adaptation is acceptable when the neural network is trained offline using software simulations. For online trainable implementations of neural networks the overheads of FPGA reconfigurations far outweigh any benefits. Typical current generation FPGA reconfiguration times are of the order of a few milliseconds (see Table 1). Overall performance of the system using reconfigurations for topological adaptation during online training depends on the total amount of time spent performing computations versus the time spent in reconfiguration cycles. Guccione and Gonzalez investigated this issue and came up with the following equation reported in [83]:

\[
q = r / (s - 1)
\]  

(2)
Table 1 Typical FPGA runtime reconfiguration times

\[ t_{conf} = \frac{N_{bits} \times f_{CCLK}}{M_{\text{bits per cycle}}}; \quad M_{\text{bits per cycle}} = 8 \text{ bits} \]

<table>
<thead>
<tr>
<th>Device</th>
<th>Number of Configuration Bits (N_{bits})</th>
<th>Slave SelectMAP configuration mode (in secs)</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>VirtexIIPro with CCLK = 50MHz (max frequency)</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>XC2VP2</td>
<td>1,305,376</td>
<td>0.003263</td>
</tr>
<tr>
<td>XC2VP4</td>
<td>3,006,496</td>
<td>0.007516</td>
</tr>
<tr>
<td>XC2VP7</td>
<td>4,485,408</td>
<td>0.011214</td>
</tr>
<tr>
<td>XC2VP20</td>
<td>8,214,560</td>
<td>0.020536</td>
</tr>
<tr>
<td>XC2VPX20</td>
<td>8,214,560</td>
<td>0.020536</td>
</tr>
<tr>
<td>XC2VP30</td>
<td>11,589,920</td>
<td>0.028975</td>
</tr>
<tr>
<td>XC2VP40</td>
<td>15,868,192</td>
<td>0.03967</td>
</tr>
<tr>
<td>XC2VP50</td>
<td>19,021,344</td>
<td>0.047553</td>
</tr>
<tr>
<td>XC2VP70</td>
<td>26,098,976</td>
<td>0.065247</td>
</tr>
<tr>
<td>XC2VPX70</td>
<td>26,098,976</td>
<td>0.065247</td>
</tr>
<tr>
<td>XC2VP100</td>
<td>34,292,768</td>
<td>0.085732</td>
</tr>
<tr>
<td><strong>Virtex4 with CCLK = 60MHz (max frequency)</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>XC4VLX15</td>
<td>4765184</td>
<td>0.009927</td>
</tr>
<tr>
<td>XC4VLX25</td>
<td>7942848</td>
<td>0.016548</td>
</tr>
<tr>
<td>XC4VLX40</td>
<td>12568960</td>
<td>0.026185</td>
</tr>
<tr>
<td>XC4VLX60</td>
<td>18236800</td>
<td>0.037993</td>
</tr>
<tr>
<td>XC4VLX80</td>
<td>24038464</td>
<td>0.05008</td>
</tr>
<tr>
<td>XC4VLX100</td>
<td>31771392</td>
<td>0.06619</td>
</tr>
<tr>
<td>XC4VLX160</td>
<td>41816064</td>
<td>0.087117</td>
</tr>
<tr>
<td>XC4VLX200</td>
<td>50601216</td>
<td>0.105419</td>
</tr>
<tr>
<td>XC4VSX25</td>
<td>9540864</td>
<td>0.019877</td>
</tr>
<tr>
<td>XC4VSX35</td>
<td>14382144</td>
<td>0.029963</td>
</tr>
<tr>
<td>XC4VSX55</td>
<td>24009600</td>
<td>0.05002</td>
</tr>
<tr>
<td>XC4VFX12</td>
<td>4906880</td>
<td>0.010223</td>
</tr>
<tr>
<td>XC4VFX20</td>
<td>7530880</td>
<td>0.015689</td>
</tr>
<tr>
<td>XC4VFX40</td>
<td>14232576</td>
<td>0.029651</td>
</tr>
<tr>
<td>XC4VFX60</td>
<td>22183296</td>
<td>0.046215</td>
</tr>
<tr>
<td>XC4VFX100</td>
<td>35059264</td>
<td>0.07304</td>
</tr>
<tr>
<td>XC4VFX140</td>
<td>50853120</td>
<td>0.105944</td>
</tr>
</tbody>
</table>
where $s$ denotes the computational time, $r$ denotes the reconfiguration time, and $q$ is the number of times the configured logic should be used before another configuration is tried to achieve good performance. Thus, time spent in FPGA computations must be much higher than the time spent in FPGA reconfiguration cycles to achieve reasonable performance speedups.

The neural network implementation presented in this dissertation is an online trainable neural network implementation on FPGAs. It supports dynamic structure and parameter updates to the neural network without FPGA reconfigurations. The implemented network topology and design details are in chapters 4 and 5, respectively.

ASIC implementations of flexible neural networks that can adapt structure and parameter values have been reported in literature. One commercially available dedicated neural hardware design is the Neural Network Processor (NNP) from Accurate Automation Corp. [84]. It is a neural network processor that has instructions for various neuron functions such as multiply and accumulate or transfer function calculation. Thus the neural network can be programmed using the NNP assembly instructions for different neural network implementations. Mathia and Clark compared performance of a single and parallel (1 to 4 NNPs) multiprocessor NNP against that of the Intel Paragon Supercomputer (1 to 128 parallel processor nodes). The NNP outperformed the Intel Paragon by a factor of 4 [85].
2.5.2.3 On-chip/Off-chip Learning

Neural network training algorithms are typically iterative algorithms that adjust neural network parameters and structure over multiple iterations based on a cost function. Thus to do an on-chip training, one needs a design that can be dynamically adapted to change its network structure and parameters. Few implementations reported in the literature actually support an on-chip training of neural networks due to the complexities involved. Eldredge et al. reported an implementation of the backpropagation algorithm on FPGAs by temporally dividing the algorithm into three sequentially executable stages of the feedforward, error backpropagation, and synaptic weight update [75, 76]. The feedforward stage feeds in the inputs to the network and propagates the internal neuronal outputs to output nodes. The backpropagation stage calculates the mean squared output errors and propagates them backward in the network in order to find synaptic weight errors for neurons in the hidden layers. The update stage adjusts the synaptic weights and biases for the neurons using the activation and error values found in the previous stages. Hadley et al. improved the approach of Eldredge by using partial reconfiguration of FPGAs instead of full-chip runtime reconfiguration [86]. Gadea et al. show a pipelined implementation of the backpropagation algorithm in which the forward and backward passes of the algorithm can be processed in parallel on different training patterns, thus increasing the throughput [87]. Ayala et al. demonstrated an ASIC implementation of MLP with on-chip backpropagation training using floating point representation for real values and corresponding dedicated floating point hardware [38]. The backpropagation algorithm implemented is similar to that of Eldredge et al. [75, 76]. A ring of 8 floating point processing units (PU) are used to compute the intermediate weighted sums in the
forward stage and the weight correction values in the weight update stage. The size of the memories in the PUs limits the number of neurons that can be simulated per layer to 200. A more recent FPGA implementation of backpropagation algorithm can be found in [88]. Witkowski, Neumann, and Ruckert demonstrate an implementation of hyper basis function networks for function approximation [89]. Both learning and recall stages of the network are implemented in hardware to achieve higher performance. The GRD (Genetic Reconfiguration of DSPs) chip by Murakawa et al. can perform on-chip online evolution of neural networks using genetic algorithms [90]. Details on it are covered in chapter 3 on evolvable hardware systems. Two commercially available neurochips from the early 1990s are the CNAPS (Hammerstrom [91]) and MY-NEUPOWER (Sato et al. [92]). CNAPS was a SIMD array of 64 processing elements per chip that are comparable to low precision DSPs and was marketed commercially by Adaptive solutions. The complete CNAPS system consisted of a CNAPS server which connected to a host workstation, and Codenet, a set of software development tools. It supports Kohonen LVQ (linear vector quantization), backpropagation, and convolution at high speed. Another commercially available on-chip trainable neurocomputer is MY-NEUPOWER. It supports various learning algorithms such as backpropagation, Hopfield, and LVQ and contains 512 physical neurons. It was a neural computational engine for software packet called NEUROLIVE [92].

The following references discuss analog and hybrid implementations that support on-chip training. Zheng et al. have demonstrated a digital implementation of backpropagation learning algorithm along with an analog transconductance-model neural
network [93]. A digitally-controlled synapse circuit and an adaptation rule circuit with a R-2R ladder network, a simple control logic circuit, and an UP/DOWN counter are implemented to realize a modified technique for the backpropagation algorithm. Linares-Barranco et al. also show an on-chip trainable implementation of an analog transconductance-model neural network [94]. Field Programmable Neural Arrays (FPNA), an analog neural equivalent of FPGAs, are a mesh of analog neural models interconnected via a configurable interconnect network [95-99]. Thus, different neural networks structures can be created dynamically, enabling on-chip training.

A more typical implementation approach has been to train the network offline using software simulations and implement the network obtained in hardware for faster recall speeds. [46, 48-50, 52, 53, 100, 101] adhere to this approach.

Newer FPGA generations have on-chip embedded processors that some implementations have used to run the training algorithms and thus provide in-system network training. Schmitz et al. use the embedded processor on the FPGA to implement genetic algorithm operators like selection, crossover, and mutation [102]. This FPGA is closely coupled as a coprocessor to a reconfigurable analog artificial neural network ASIC on a single PCB. A host processor initializes this PCB and oversees the genetic evolution process.
2.5.2.4 Activation Function Implementation

Activation functions, or transfer functions, are typically non-linear monotonically increasing sigmoid functions. Examples of typical activation functions include hyperbolic tangent, logistic sigmoid, and hard limit functions. Direct implementation of nonlinear sigmoid functions in FPGAs can occupy significant reconfigurable resources. A typical approach is to use piece-wise linear approximations of these functions and interpolate the values between piece-wise samples using straight lines. The computations for piecewise approximations can either be implemented in logic or the values can be pre-computed and stored in lookup tables (LUTs). Omondi, Rajapakse, and Bajger show an implementation of piece-wise linear approximation of activation functions using the CORDIC algorithm on FPGAs [103]. Krips et al. show an implementation of piece-wise linear approximation of activation functions pre-computed and stored in LUTs [54].

One problem of direct implementations of the activation function is that one has to redesign the hardware logic for every application that is using a different activation function. In such scenarios the LUT approach serves well as the values can be pre-computed and loaded in the LUT. But the size of the LUT is directly influenced by the data widths. Every extra bit in the data more than doubles the size of the LUT.
2.5.3 Analog Neural Hardware Implementations

Analog artificial neurons are more closely related to their biological counterparts as the biological neurons perform analog computations. Many characteristics of analog electronics can be helpful for neural network implementations. Typical analog neurons use operational amplifiers to directly perform neuron-like computations, such as integration and sigmoid transfer functions. These can be modeled using physical processes such as summing of currents or charges. Also, the interface to the environment may be easier as no analog-to-digital and digital-to-analog conversions are required. Some of the earlier analog implementations used resistors for representing free network parameters such as synaptic weights [104]. These implementations using fixed weights are not adaptable and hence can only be used in the recall phase. Adaptable analog synaptic weight techniques represent weights using variable conductance [94, 105, 106], voltage levels between floating gate CMOS transistors [107-110], capacitive charges [111, 112], or using charged coupled devices [113, 114]. Some implementations use digital memories for more permanent weight storage [115]. There have been many commercial and research implementations of analog neural networks. Some of the prominent ones are the Intel ETANN (Electronically Trainable Analog Neural Network) [107, 116-120] and the Mod2 Neurocomputer [121]. Although there are many advantages of implementing analog neural networks as discussed above, the disadvantage is that the analog chips are susceptible to noise and process parameter variations, and hence need a very careful design.
2.5.4 Hybrid Neural Hardware Implementations

Hybrid implementations combine analog, digital, and other strategies such as optical communication links with mixed mode designs in an attempt to get the best that each can offer. Typically the hybrid implementations use analog neurons taking advantage of their smaller size and lower power consumption, and use digital memories for permanent weight storage [122, 123]. But the mixed-signal design of the analog neurons with the digital memories on the same die introduces a lot of noise problems and requires isolation of the sensitive analog parts from the noisy digital parts using guard rings. Sackinger et al. demonstrate a high speed character recognition application on the ANNA (Analog Neural Network Arithmetic and logic unit) chip [124]. This ANNA chip can be used for a wide variety of neural network architectures but is optimized for locally connected weight-sharing networks, and time-delay neural networks (TDNNs). Zatorre-Navarro et al. demonstrate a mixed mode neuron architecture for sensor conditioning [125]. It uses an adaptive processor that consists of a mixed four-quadrant multiplier and a current conveyor that performs the nonlinearity. Synaptic weight storage uses digital registers and neural network training is performed off-chip.

Due to the large number of interconnections, routing quickly becomes a bottleneck in digital ASIC implementations. Higher fan-in and fan-out neurons require more drive strength resulting in larger transistor widths and more intermediate signal drive buffers. Some researchers have proposed hybrid designs using optical communication channels. Maier et al. [126] have shown a hybrid digital-optical implementation that performs neural computations electronically, but the communication
links between neural layers uses an optical interconnect system. This increases the speed of neural processing by a factor of one magnitude higher than a purely digital approach. But on the flip side they increase hardware cost and complexity for transferring signals between the electronic and the optical systems. Craven et al. [127] proposed using frequency multiplexed communication channels to overcome the communication bottleneck in fully connected neural networks.

2.6 Summary

Custom neural network hardware implementations can best exploit the inherent parallelism in computations observed in artificial neural networks. Many implementations have relied on offline training of neural networks using software simulations. The trained neural network is then implemented in hardware. Although these implementations have good recall speedups, they are not directly comparable to the implementation reported here which supports on-chip training of neural networks. On-chip trainable neural hardware implementations have also been reported in literature. Most of the reported ones are custom ASIC implementations such as the GRD chip by Murakawa et al. [90], on-chip backpropagation implementation of Ayala et al. [38], CNAPS by Hammerstrom [91], MY-NEUPOWER by Sato et al. [92], and FPNA by Farquhar, Gordon and Hasler [95]. FPGA based implementations of on-chip training algorithms have also been reported such as the backpropagation algorithm implementations in [75, 76, 86-88]. An online trainable implementation of hyper basis function networks has been reported in [89]. The implementation presented here differs
from the reported ones in one or more of the following: (i) the artificial neural network implemented, the block-based neural networks (see chapter 4), (ii) the training approach using the genetic algorithms, and (iii) the FPGA implementation platform. The implementation supports on-chip training without reliance on FPGA reconfigurations, unlike some of the approaches listed above. It uses genetic algorithms to train the BbNNs. The genetic operators such as selection, crossover, and mutation are implemented on the embedded processor PPC 405 on the FPGA die, similar to the approach of Schmitz et al. [102]. But unlike their approach the neural network designed is a digital implementation in the configurable logic portion of the same FPGA chip. Schmitz et al. [102] use a separate neural analog chip for fitness evaluations for the GA running on PPC 405 on the closely coupled FPGA on the same PCB board.
3 Evolvable Hardware Systems

Evolvable hardware systems (often called E-hard or EHW systems) are systems built using programmable/reconfigurable hardware devices such as programmable logic devices (PLDs), field programmable gate arrays (FPGAs), field programmable transistor arrays (FPTAs), or custom-built programmable chips. The central idea of these systems is to use the runtime hardware reconfiguration ability of these devices along with evolutionary algorithms to evolve a digital or analog circuit. The configuration bitstream (viewed as a phenotype in an evolutionary algorithm) for these devices is encoded as a chromosome (viewed as a genotype) and evolved using evolutionary algorithms over multiple generations. Genetic operators such as selection, crossover, and mutation are applied to a randomly generated population of these chromosomes to create newer generations. Fitter genotypes survive through multiple generations and are used for breeding newer generations. The aim is to increase the average fitness of the population from one generation to the next with the goal of finding a genotype with fitness that is equal to greater than the target fitness. The population fitness is determined by a fitness function which is application-specific. Apart from evaluating the correctness of the EHW’s output for the training data set, the fitness function can also consider other constraints such as circuit size, speed, or power. EHW systems were first conceptualized by DeGaris back in 1992. He classified these systems into two classes: extrinsic and intrinsic EHW systems [2].
**EXTRINSIC EHW** systems perform an offline evolution using software simulations. The evolutionary algorithm is wrapped around a software model of the hardware and evolution is done using software simulations. The fittest evolved circuit is then used and configured on the hardware.

**INTRINSIC EHW** systems include the hardware in the evolution loop. It is an online evolution technique that directly evolves the underlying hardware circuitry.

This chapter introduces EHW systems and reviews reported contributions to this field over the last one and a half decades. Section 3.1 discusses gate-level and functional-level evolution strategies and their corresponding advantages and disadvantages. Section 3.2 provides a literature review of EHW systems.

### 3.1 Gate-level, Transistor-level, and Functional-level Evolution

Evolving an FPGA bitstream in essence is evolving gate-level logic circuitry. Due to a time consuming evolution process, evolving larger circuits using this strategy is impractical. Longer chromosomal lengths for larger circuits need larger memories to store the genotype generations during evolution and need significantly higher processing speeds to speedup the time-consuming evolution process. Larger circuits also mean significantly larger search spaces. Evolutionary algorithms are global search algorithms and as a result may take much longer to converge to a solution over many generations.
This limits the practical circuit sizes that can be used in the evolution process. Also, for intrinsic gate-level evolution, slow circuit reconfigurations times may pose a significant bottleneck for some applications. Typical FPGA reconfiguration times are on the order of a few milliseconds (see section 2.5.2.2). The number of runtime reconfigurations that are required during the intrinsic evolution process could be significantly high and depends on the population size and number of generations required to meet the fitness goals. Hence the evolution process will incur significant reconfiguration cycle time overheads which may not be practical for many applications.

Just as FPGAs are used for gate-level evolution in EHW systems, FPTAs enable development of transistor-level EHW systems. Field programmable transistor arrays enable circuit reconfigurability at transistor levels allowing synthesis of analog, digital, and mixed-signal electronic circuits. These devices consist of cells of programmable transistors, resistors, and capacitors interconnected via programmable switches. FPTAs can be used to build analog circuits such as amplifiers, and filters as well as digital logic circuits. More details on FPTAs can be found in [128].

Higuchi et al. [129, 130] proposed to use the concepts of evolvable hardware systems to do functional-level hardware evolution as opposed to the traditional gate-level evolution. They proposed to evolve internal parameters and connections of higher-level functional modules such as adders, multipliers, dividers, and sine generators. A criticism for this approach has been that the circuit is limited in functionality by the available hardware modules and newer functional modules may be required for a different
application. But this approach also significantly reduces the genotype length, facilitating more complex practical circuits for evolution. Since the EHW concept involves the evolution of desirable hardware circuits by genetic learning, without giving any specifications in advance, it provides a contrasting bottom-up approach to the conventional top-down hardware design methodology. Thus, different functional modules can be used for different applications.

So for neuromorphic circuit applications, artificial neuron models can be used as functional modules. The evolutionary algorithm can then be used to evolve the synaptic connections and free parameters of artificial neural networks. Prior work uses evolutionary algorithms instead of more traditional gradient descent approaches for training artificial neural networks [17-25]. This work follows in their footsteps to develop an intrinsically evolvable neural network EHW system. The following section provides a review of reported literature in evolvable hardware systems.

3.2 Review of Evolvable Hardware Systems

Typical FPGAs are not suitable for EHW as they cannot be programmed with random bitstreams due to the risk of damaging the device. The idea of intrinsic evolution really took off after the introduction of Xilinx 6200 series FPGAs [2]. These FPGAs were EHW friendly; the devices included a SRAM-cell-based architecture in which all internal connections were unidirectional. Thus, no random configuration bits in these cells could damage the device as it is impossible to connect two outputs together. So an evolutionary
algorithm can be allowed to manipulate the configuration of a real chip without the need for any legality constraint checking. Xilinx also made the architecture of these chips public, generating more interest in the field of evolvable hardware systems. Earlier research before the Xilinx 6200 series FPGAs was mostly concentrated on the extrinsic evolution strategy. In 1998, Xilinx stopped production of the 6200 series FPGAs and introduced their next generation Virtex series FPGAs [131]. With these devices Xilinx reverted back to the classic FPGA device layout with CLBs and a multidirectional routing structure. This made the device unsafe for random bitstream configurations as the outputs could be shorted together in this architecture. Also the detailed architecture of these devices was not publicly available, since Xilinx aimed at mass-production of these devices. This also ensured that circuits couldn’t be reverse-engineered from the bitstreams. Thus for intrinsic evolution, the evolutionary algorithms needed to include the Xilinx place and route tools in their loop. However, other researchers have proposed alternative strategies using JBits. JBits comprises Java classes that provide an application programming interface (API) into the Xilinx FPGA bitstreams. JBits provides the capability of designing and dynamically modifying circuits in Xilinx FPGAs. Hollingworth, Smith, and Tyrrell demonstrated safe intrinsic evolution on Xilinx Virtex devices using JBits [132].

This section provides a brief summary of reported publications in the evolvable hardware field. Section 3.2.1 surveys various EHW chips grouping them by their target applications. Section 3.2.2 surveys developed EHW platforms for research and custom evolutionary algorithms. [2, 133-137] discuss various EHW fundamentals and also have
reviews of EHW systems. More formal classification and comparison with bio-inspired systems can be found in [138].

3.2.1 EHW Chips and Applications

EHW systems use off-the-shelf hardware (such as FPGAs) as well as custom-built EHW chips to implement digital, analog, or mixed-signal evolutionary circuits. These chips enable one or more of the evolutionary techniques, gate-level, transistor-level, and functional-level evolution, to be implemented. EHW systems have been successfully applied in many application areas such as neural hardware, signal and image processing, control applications, analog electronics, and navigation systems. The review presented here groups the EHW implementations by their application fields. An interesting feature of many EHW systems is a degree of inherent fault tolerance due to the evolutionary design approach. In theory, previously developed hardware circuits can be re-evolved in the event of a fault to effectively ‘bypass’ the faulty component or section of the chip. In practice, the degree of fault tolerance achievable varies and is the subject of research. EHW systems also have applications in extreme temperature electronics. Stoica et al. demonstrated fault tolerant electronic circuit designs using adaptive intrinsic circuit redesign/reconfiguration during operation in extreme environments [139]. Their approach is demonstrated on a prototype chip that can recover functionality at 250°C.
3.2.1.1 EHW Systems for Neural Hardware

The EHW systems listed here have been used for implementing evolutionary artificial neural networks. The goal is to provide autonomous reconfiguration capability to neural networks for intrinsic evolution. These implementations relate directly to the research work presented in this manuscript. A discussion of how they compare with the research work in this dissertation is at the end of this chapter in section 3.3.

A well known EHW project was the ATR’s CAMBrain machine (CBM) [140-146]. Jointly developed by ATR laboratories and Genobyte, the first prototype was available in 1999. CBM used Xilinx's XC6264 FPGAs to build and evolve 3D cellular automata (CA) based neural network modules directly in hardware. The neural network implemented is CoDi (Collect and Distribute) that uses single bit signaling. The output spike-trains of these single bit neurons are converted to analog waveforms that can be compared to target waveforms for fitness calculation during evolution. Early experiments on the CBM targeted applications such as frequency dividers, moving line detection, and pattern recognition. The goal of the project was to build an artificial brain with millions of neurons that can be evolved to control the behaviors of robots.

The GRD (Genetic Reconfiguration of DSPs) chip by Murakawa et al. [90] is an evolvable hardware chip designed for neural network applications. It was developed at the MITI's Electrotechnical Laboratory as part of the Real World Computing (RWC) project. The GRD chip is a building block for the configuration of a scalable neural network hardware system. Both the topology and the hidden layer node functions of a
neural network mapped on the GRD chips are dynamically reconfigured using a genetic algorithm (GA). Thus, the most desirable network topology and choice of node functions (e.g., Gaussian or sigmoid function) for a given application can be determined adaptively. The GRD chip consists of a 32-bit RISC processor and fifteen 16-bit DSPs connected in a binary-tree network. The RISC processor executes the GA code and each of the DSPs can support computations of up to 84 neurons. Thus each GRD chip can support 1260 neurons. Multiple GRD chips can be connected for a scalable neural architecture.

3.2.1.2 Applications in Signal and Image Processing

Although deGaris introduced and classified EHW, Thompson illustrated its promise by developing the first intrinsically evolvable hardware system [147, 148]. He used a Xilinx XC6216 chip to distinguish between two square wave inputs of 1 kHz and 10 kHz. The circuit was evolved intrinsically so that the output would be 0 volt for the 1 kHz input, and 5 volts for the 10 kHz input. The evolved circuit was specific to the particular chip used in the evolution process.

As part of the RWC project at the MITI Electrotechnical Laboratory (under which GRD discussed above was developed), an EHW chip for a data compression application in electrophotographic printers [149] and an IF filter chip for use in cellular phones were also developed [150]. A pattern recognition system built using EHW hardware is presented by Iwata et al. in [151]. Higuchi et al. [152] and Sakanashi et al. [153] give the
overview of the EHW projects developed at the MITI's Electrotechnical Laboratory as part of the Real World Computing (RWC) project.

Koza et al. give a survey of problems from cellular automata and molecular biology in which genetic programming evolved a computer program that produced results that were slightly better than human performance for the same problem [154]. They also show three examples in electronic synthesis (lowpass filter, an amplifier, and an asymmetric bandpass filter) where circuit evolution using genetic programming generated better circuit designs.

Hounsell and Arslan demonstrate an evolvable hardware platform for the automated design and adaptation of digital filters on a programmable logic array (PLA) [155]. Investigation of the fault tolerance behavior of their system showed that the circuit functionality was maintained despite an increasing number of faults covering up to 25% of the PLA area. Zhang, Smith, and Tyrrell also demonstrate an intrinsic EHW system for digital filters [156].

### 3.2.1.3 Applications in Analog Electronics

Hereford and Pruitt describe a system robust to input sensor failure using evolvable hardware on a field programmable analog array (FPAA) [157]. The circuit averages sensor inputs connected to the FPAA. In the event of a sensor input failure, the failure is detected by the controller and it triggers a circuit reprogramming. The system is
shown to be robust to several different sensor failure modes such as open circuit, short circuit, multiple sensor failures, and FPAA input amplifier failure.

Bennet et al. used genetic programming to evolve the topology and sizing of each component of an op-amp [158]. The resultant 22 transistors amplifier has almost no bias or distortion and gives a 60 decibel DC gain with good frequency generalization.

Subbiah and Ramamurthy demonstrate an intrinsically evolvable hardware implementation of a process sensor controller with a neural estimator based fault detection mechanism to take care of sensor failures [159].

3.2.1.4 Applications in Digital Logic Circuits

Sekanina et al. show extrinsic simulations and intrinsic evolution in FPGAs of multifunctional digital circuits using polymorphic gates [160-162]. They implement GA in the FPGA and use a virtual reconfigurable circuit of polymorphic gates for evolution.

Heng, Miller, and Tyrrell demonstrate an intrinsic EHW implementation for a 2-bit fault tolerant multiplier that can recover from transient faults [163]. Simulation experiments for fault tolerance of evolved circuits by Hartmann and Haddow demonstrate a graceful degradation in performance in 2-bit adder and a multiplier circuit [164]. Their analysis demonstrates tolerance to increasing noise and gate failures.
3.2.1.5 Control and Navigation Applications

Gwaltney and Ferguson demonstrated intrinsic EHW techniques to evolve an analog controller for the control of the shaft speed of a DC motor using a second generation Field Programmable Transistor Array (FPTA2) [165]. Performance comparison of the evolved controller to that of a conventional proportional-integral (PI) controller showed that hardware evolution is able to create a compact design that provides good performance, while using considerably less functional electronic components.

Kajitani et al. have developed a gate-level EHW chip used for prosthetic hand controllers [84]. Keymeulen et al. have developed an EHW chip for an adaptive mobile robot navigation system [166]. Both of these were part of the MITI RWC project.

3.2.2 EHW Algorithms and Platforms

One widely recognized problem with EHW is the time and space required for genetic evolution and the genotype-phenotype mapping. To address this issue many different flavors of evolutionary algorithms have been reported in the literature such as the compact GA [167, 168], increased complexity evolution [169], bi-directional incremental evolution [170], generalized disjunction decomposition algorithm (GDD) [171-174], and fast evolutionary algorithm (FEA) [175]. Many researchers believe that the classical usage of evolutionary algorithms in EHW systems centered on the best individual is a constrained view. There is rich information in a population which can and
should be exploited. A truly population-based approach that emphasizes population rather than the best individual can often yield several important benefits to evolvable hardware, including efficiency, accuracy, adaptiveness, and fault-tolerance. A number of examples have been presented in [176] to illustrate how a population of cooperative specialists, evolved by fitness sharing or trained by negative correlation, can achieve better performance in many aspects than the best individual in the population.

Many custom platforms have been built to further research into EHW systems. The rest of this section surveys some custom built intrinsic EHW platforms reported.

Tempesti et al. have developed a BioWall [177]. It is a giant reconfigurable computing tissue developed to implement embryonics machines. It is structured as a two-dimensional tissue composed of units representing molecules. Each unit consists of an input element (a touch-sensitive membrane), an output element (an array of $8 \times 8 = 64$ two color LEDs), and a programmable computing element (a Spartan XCS10XL Xilinx FPGA). The BioWall contains 3200 units, arranged as 20 rows of 160 units. The BioWall is used for research into EHW applications that range from Embryonics' ontogenetic systems, through epigenetic artificial neural networks, to phylogenetic evolving hardware.

Sipper et al. used Xilinx 4000 series of programmable chips to build a system capable of evolving the hardware, measuring the fitness, and performing the evolutionary algorithm all on a single printed circuit board (PCB) [138]. They proposed a partition of
the space of bio-inspired hardware systems based on nature’s classification along three axes: phylogeny, ontogeny, and epigenesis. The phylogenetic level concerns the temporal evolution of the genetic programs within individuals and species, the ontogenetic level concerns the developmental process of a single multicellular organism, and the epigenetic level concerns the learning processes during an individual organism’s lifetime.

Other EHW platforms of interest are the MorphoSys EHW platform developed by Guangming et al. [178] and the ‘Processing Integrated Grid’ (PIG) self-reconfigurable scalable EHW chip developed by Macias [179, 180]. Tufte and Haddow reported a platform for complete hardware evolution (implementing GA in hardware along with the reconfigurable circuit) [181]. They demonstrate an evolution of a 4 by 1 multiplexer using their platform.

### 3.3 Summary

This chapter presents a review of EHW systems and its reported applications. These systems use evolutionary algorithms to evolve hardware circuitry with specific fitness goals such as correct functionality, circuit size, and power. EHW systems can be classified into extrinsic and intrinsic EHW systems. The former uses a software model of the underlying hardware architecture and performs offline evolution. The latter includes the hardware in the evolution loop and performs online evolution. EHW systems can be used in many applications ranging from bio-inspired hardware, signal and image processing, analog and digital electronics, to process control. Section 3.2.1 discussed two
EHW neural hardware applications that are closely related to the research work presented here. Both of the reported EHW neural hardware chips, the CAMBrain machine (CBM) and GRD are custom-built on silicon. The CBM project custom built a network of evolvable CoDi 1-bit neural modules that are evolved using evolutionary algorithms. The GRD chip uses a binary network of 16-bit DSPs that support multiple neural computations. It can implement sigmoid neural nodes (as in Multi-layer Perceptrons) as well as Gaussian neural nodes (as in Radial Basis Function networks). The FPGA platform developed and reported in this work is an intrinsic EHW system for neural hardware applications. The neural network topology implemented is called block-based neural networks (BbNNs) [23]. BbNNs use evolutionary algorithms to evolve network structure and synaptic weights of the network. The developed EHW platform uses functional-level evolution and is implemented using off-the-shelf available FPGAs.
4 BLOCK-BASED NEURAL NETWORKS

4.1 Introduction

Inspired from the initial perceptron model of a neuron, many different artificial neural network topologies have been explored in the literature. Some of the well-known models include fully and partially connected feedforward multilayer perceptron models, radial-basis function networks, self-organizing maps, cellular neural networks, and fully and partially connected recurrent neural network models. These use different learning paradigms such as supervised, unsupervised, and reinforcement learning techniques. This work explores implementation of evolvable block-based neural networks on reconfigurable hardware. This chapter introduces block-based neural networks.

A block-based neural network (BbNN) is a flexible neural network of neuron blocks interconnected in the form of a grid as shown in Figure 7 [4-6, 23, 49, 182-186]. Each neuron block is the basic information processing element of the network and can have one of four possible internal configurations depending on the number of inputs and outputs as listed below and shown in Figure 8.

- 1-input, 3-output (1/3),
- 2-input, 2-output (2/2) (left side output),
- 2-input, 2-output (2/2) (right side output), and
- 3-input, 1-output (3/1).
Figure 7  Block-based Neural Network topology

Figure 8  Four different internal configurations of a basic neuron block
(a) 1/3 (b) 2/2 (left) (c) 2/2 (right) (d) 3/1 configurations
Each individual neuron block computes outputs that are a function of the summation of weighted inputs and a bias as shown in equation 3.

\[ y_k = g \left( b_k + \sum_{j=1}^{J} w_{jk} x_j \right), \quad k = 1, 2, \ldots, K \] (3)

where,

- \( y_k \): \( k^{th} \) output signal of the neuron block
- \( x_j \): \( j^{th} \) input signal of the neuron block
- \( w_{jk} \): Synaptic weight connection between \( j^{th} \) input node and \( k^{th} \) output node
- \( b_k \): Bias at \( k^{th} \) output node
- \( J, K \): Number of input and output nodes respectively of a neuron block.
- \( g(\bullet) \): Activation function

A neuron block can have up to six synaptic weights and biases, three inputs, and three outputs depending on the internal configuration of the block. A 2/2 neuron block has 6 synaptic weights and biases, 2 inputs, and 2 outputs. Similarly, a 1/3 block has 3 synaptic weights and biases, 1 input, and 3 outputs. The activation function \( g(\bullet) \) can be linear (e.g., ‘purelin’) or a nonlinear function (e.g., ‘logistic sigmoid’). Signal flow in the network from input to output is determined by the internal configurations of blocks used in the network. This determines the network structure. Figure 9 shows two different unique BbNN networks structures.
4.2 Evolving BbNNs Using Genetic Algorithms

To find a suitable BbNN for a particular problem, both the network structure and the internal weights and biases need to be tuned. Thus the learning process for a BbNN is a multi-parametric optimization problem. Due to the multimodal non-differentiable search space, it is difficult to use regular gradient descent based learning algorithms such as the backpropagation algorithm. These will be very inefficient and may not converge at all, getting repeatedly trapped in local minima. A global optimization approach such as genetic algorithms is more likely to find an answer [187]. Goldberg’s book on genetic algorithms is a classic reference for the subject [188].

In genetic algorithms a population of candidate solutions (individuals or phenotypes) of a problem, encoded in abstract representations (called chromosomes or the genotype), are evolved over multiple generations towards better solutions. The algorithm follows the Darwinian evolution model keeping the fittest individuals and getting rid of the unfit individuals in the population. The genetic evolution process...
involves selection of random (or biased random) individuals from the current population for genetic crossover and mutation to produce the next generation. The selection strategy used may be biased towards selecting individuals with higher fitness and use different techniques such as the tournament selection or roulette wheel selection strategy. The initial population is randomly initialized. A fitness function evaluates the fitness of every individual in the population. With a biased selection strategy, individuals with higher fitness are more likely to be selected for genetic reproduction (crossover and mutation) to produce new populations. The fitness of newly generated individuals in the population is evaluated using the fitness function and the evolution process proceeds, further producing newer generations. The goal is to find an individual among the population with fitness equal to or greater than the target fitness [188]. Figure 10 shows a flowchart for the genetic evolution process described above.
Figure 10  Flowchart depicting genetic evolution process
4.2.1 Genetic Operators

Operators in genetic algorithms are used to produce offspring to form new generations. These are discussed in detail below.

4.2.1.1 Selection

Selection is a process in which a proportion of the existing population in each successive generation is selected to breed a new generation. Individual solutions are selected through a fitness-based process, where fitter solutions (as measured by a fitness function) are typically more likely to be selected. The selection process is stochastic and designed to also select a small proportion of less fit solutions to maintain population diversity and prevent premature convergence of poor solutions. In tournament selection, a group of randomly chosen individuals from the population are pitted against each other and a winner (best fit individual) is selected for crossover. Selection pressure can be adjusted by varying the tournament group size. In roulette wheel selection (also called fitness proportionate selection); all the individuals in the population are ranked according to their fitness, assigning each one a probability. The chance of an individual to be selected is proportional to its rank. While candidate solutions with a lower fitness will be more likely to be eliminated, there is still a chance that they may be selected.
4.2.1.2 Crossover

Crossover is a genetic process used to vary the programming of a chromosome(s) from one generation to the next. It is analogous to biological crossover and reproduction. Two parent chromosomes swap genetic information to produce two offspring. Many crossover techniques exist such as one-point crossover, two-point crossover, and the cut and splice strategy. For example, in a two-point crossover strategy if ‘S1=000000’ and ‘S2=111111’ are two chromosomes, then a crossover between the two using a randomly selected crossover site (in this example after bit 2) could produce two offspring ‘S1’=110000’ and ‘S2’=001111’.

4.2.1.3 Mutation

In mutation, the bits of the candidate are randomly flipped based on some low probability. The purpose is to maintain population diversity and induce a random walk through the search space of possible solutions.

The genetic evolution process described above works well with a single dimensional search space, but needs modification for multiparametric optimization problems. The search space for our BbNN evolution problem poses a two-dimensional optimization problem (simultaneous structure and weight optimization). Thus we need to modify the genetic algorithm for it to work with the problem at hand. The learning process uses a supervised training approach. The modified genetic algorithm is described below.
4.2.2 BbNN Encoding

The structure and weight of the BbNN need to be encoded as a single chromosome. The network structure is encoded as a gene using a sequence of binary numbers representing the signal flow through the BbNN. Any connection between the blocks is represented with either a binary 0 or a binary 1. A binary 0 denotes down (↓) and left (←) signal flow directions, and a binary 1 indicates up (↑) and right (→) signal flows. The number of bits required to represent the signal flow of an \(m \times n\) BbNN is \((2m-1)n\). This is the case for a recurrent BbNN network where a signal flow from a lower layer neuron block to an upper layer block (↑) is a valid network structure. In the case of feedforward networks, a feedback as in the earlier case results in invalid structures. Since the signal flow in feedforward neurons is restricted from top to bottom, we do not need to encode that structure information as it is implied. Thus in a feedforward network binary 0 denotes left (←) signal flow direction, and a binary 1 indicates right (→) signal flow. Thus the number of bits required to represent the signal flow of an \(m \times n\) block-based neural network is \(mn\). Figure 11 illustrates recurrent BbNN network structure encoding and Figure 12 shows a feedforward network structure encoding. Synaptic connection weights of each neuron block in a network are encoded as real values in an array. The arrays of all the blocks are concatenated sequentially to form a weight gene. The weight gene along with the structure gene forms the BbNN chromosome. Figure 13 shows the weight gene encoding and Figure 14 shows the complete encoding of a BbNN chromosome for a \(2 \times 2\) network.
Figure 11  Recurrent BbNN network structure encoding (a) BbNN (b) Structure encoding

Figure 12  Feedforward BbNN network structure encoding (a) BbNN (b) Structure encoding
Figure 13  BbNN weight gene encoding (a) Neuron block (b) Weight encoding

Figure 14  BbNN chromosome encoding for a 2 x 2 network
4.2.3 Fitness Function

The training approach is a supervised training algorithm with training data composed of corresponding input – output pairs. The fitness function used is derived from the total mean squared error between target and actual outputs of the network. Equation 4 shows the fitness function used.

\[
\text{Fitness} = \frac{1}{1+e}
\]  

(4)

\[
e = \frac{1}{Nn_o} \sum_{j=1}^{N} \sum_{k=1}^{n_o} e_{jk}^2
\]  

(5)

\[
e_{jk} = d_{jk} - y_{jk}
\]  

(6)

where,

- \(N\) number of training data samples
- \(n_o\) number of actual output nodes
- \(e_{jk}\) error between desired and actual outputs of the \(k^{th}\) output block referred to \(j^{th}\) pattern
- \(d_{jk}\) and \(y_{jk}\) desired and actual outputs of the \(k^{th}\) output block referred to \(j^{th}\) pattern.
4.2.4 Genetic Evolution

The 2-dimensional genetic evolution is similar to the one described above. A population of BbNN chromosomes is randomly initialized and their fitness is evaluated. A selection strategy (tournament or roulette wheel) selects individuals for genetic crossover operations with selection pressure against the least fit individuals. The crossover operator randomly swaps portions of the structure genes of the two parent chromosomes based on a crossover probability. The offspring are added to the new population. The mutation operator operates on the newly created individuals and has two stages. First the structure mutation stage randomly flips structure gene bits based on a low structure mutation probability. Second the weight mutation stage adds Gaussian noise with zero mean and unit variance to the weights based on a low weight mutation probability. The newly generated population is evaluated for fitness and the evolution proceeds further with the new generation until an individual with fitness greater than or equal to the target fitness is found or the maximum number of generations has been reached. Figure 15 illustrates the structure crossover operation. The dotted lines shown in the two parents are the structure crossover sites. The structure gene is sliced at these lines and the sliced portions are swapped to produce two offspring as shown. Figure 16 illustrates the structure mutation operation in BbNNs. A bit is chosen randomly based on a low mutation probability from the structure gene and flipped. The new structure gene obtained and its corresponding BbNN network is shown in the figure.
Figure 15 Structure crossover operation in BbNN
Figure 16  Structure mutation operation in BbNN
4.3 Summary

This chapter introduced BbNNs and multi-parametric genetic evolution algorithms used to evolve the network structure and weights of the BbNNs. A BbNN is a network of neuron blocks interconnected in the form of a grid. Due to the regular structure of these networks they are well suited for custom implementations in digital hardware such as field programmable gate arrays (FPGA) and application specific integrated circuits (ASIC). Network structure regularity facilitates scaling the network in custom implementations with ease. The internal configuration of the neuron blocks remains the same (one out of the four described in section 4.1) as a result of scaling the network size. The number of synaptic connections between the neuron blocks also grows linearly as a result of scaling network size. This is unlike the popular multilayer perceptron (MLP) networks. MLPs are fully connected networks of neurons with a synaptic connection between each pair of neurons in the adjacent layers. Thus, growth in network size adds many new synaptic connections to the network. Each new synaptic connection adds a new stage to the multiplier and accumulator circuit of the neuron to which it serves as an input. The multiplier and accumulator circuit in the neurons is used in calculating the output which is a function of the weighted summation of the inputs and a bias. This makes scaling the network structure difficult in hardware implementations for networks such as MLPs. Thus, the regular network structure of BbNNs facilitates hardware implementations. A disadvantage of the partial connectivity in network architectures such as BbNNs is the possibility of requiring more equivalent neurons to solve the same problems as would be required in the case of an MLP. The BbNNs can be trained using
genetic algorithms introduced in this chapter. The training is a multi-parametric optimization problem involving simultaneous evolution of network structure and the synaptic weights. Due to the multimodal non-differentiable search space it is difficult to use regular gradient descent based learning algorithms such as the backpropagation algorithm. These will be very inefficient and may not converge at all, getting repeatedly trapped in local minima. A global optimization approach such as genetic algorithms is more likely to find an answer [187]. But the disadvantage of using global training approaches such as GA are longer training times than the directed gradient descent search algorithms such as the backpropagation algorithm. Hybrid training algorithms for BbNNs have been investigated that take the advantages of global sampling of GAs and fast convergence of gradient descent techniques for efficient training of BbNNs. More information on these can be found in [4, 5]. This dissertation uses the regular GA approach presented in section 4.2. Moon and Kong proved that a BbNN of size $m \times n$ can successfully represent the input – output characteristics of any MLP network for $n \leq 5$ [23]. BbNNs have been applied to mobile robot navigation [23], multivariate gaussian distributed pattern classification [182], chaotic time series prediction [183], and ECG signal classification [4-6].
Many custom artificial neural network implementations have been reported in hardware. Section 2.5 presents a review of these implementations. Most implementations rely on an offline neural network learning in software simulations, with the resultant network being custom-built either in fixed ASICs or reconfigurable FPGAs. Thus, only the recall stage benefits from custom implementation speedups. Every new application of these networks needs a new custom design built and configured on the FPGAs or ASICs. The design goal here is to build an online neural network learning platform that can be trained and adapted intrinsically in hardware. This platform is an intrinsically evolvable hardware system performing functional-level evolution. The evolving functional modules and their interconnections are artificial neurons and their synaptic connections. The neural network implemented is the feedforward block-based neural network (BbNN) discussed in chapter 4. The following sections give the design details for the BbNN platform.

5.1 BbNN FPGA Design Details

The design was implemented for a Xilinx Virtex-II Pro (XC2VP30) FPGA [189] housed on a Xilinx University Program (XUP) FPGA development board [190] or an Amirix AP130 FPGA development board [191]. This particular FPGA includes 2 on-chip PowerPC 405 embedded processor cores, 30,816 logic cells, 136 built-in 18×18
multipliers, and 2448 KBits (306 KBytes) of on-chip block RAM. These multipliers will be used to build the multiplier and accumulate circuits in the FPGA units for neuron block processing and the available on-chip block RAM will be used to store the activation functions. The PowerPC will be used for the genetic algorithm and control operations in our design. These will be discussed in details in section 5.1.

For on-chip learning the network design has to be flexible to accommodate dynamic changes in network structure and internal parameters (synaptic weights and biases). As discussed in section 2.5.2.2 the time taken for each FPGA reconfiguration cycle is on the order of milliseconds. This poses a bottleneck for an online evolution system that relies heavily on FPGA reconfigurations for changes in network structure and internal parameters. Thus we need to minimize any reconfiguration cycles that would be required during the learning stage for better performance. In the case of BbNNs, the following dynamic updates have to be accommodated for an on-chip learning capability.

- **Dynamic updates to network structure**

  Network structure and internal configurations of neuron blocks is dictated by the structure gene. Any change in the structure gene changes the internal configurations of the neuron blocks in the grid, thus modifying the dataflow through the network. To accommodate this dynamically, we need a neuron block design that can dynamically emulate any of the four internal configuration modes without requiring an FPGA reconfiguration.
Addition/deletion of row(s) / column(s)

The genetic evolution process could potentially add / delete rows and columns to / from the BbNN grid. Accordingly, it either increases or shortens the length of the structure and weight genes in the BbNN chromosome. From the hardware design perspective, any addition of a row or column to the existing network grid adds new neuron blocks and a few new nets (connections) between the old and new neuron blocks. This is difficult to accommodate dynamically in FPGAs and may require a reconfiguration cycle. The design presented here minimizes the overhead of reconfiguration cycles as will be evident from the design of the neuron block and the dataflow architecture.

Dynamic updates to synaptic weights and biases

Synaptic weights and biases are stored in digital registers and can be dynamically updated without requiring any FPGA reconfigurations.

Other requirements and considerations for the design include the following.

- Data representation and precision
- Activation function implementation
- Internal neuron block configurations
- Dataflow implementation
- Area, speed, and power
- Design scalability and real-time processing support
These design considerations and the resulting decisions are discussed below.

### 5.1.1 Data Representation and Precision

The inputs, outputs, and internal parameters such as synaptic weights and biases are all real-valued variables. Representing and storing them in digital hardware can be either done using floating point or fixed point number representation. Floating point representation will have a significantly wider range and higher precision as compared to fixed point representations. However, floating point arithmetic circuits are complicated to build, have much larger footprint in silicon, and are significantly slower as compared to those required for fixed point arithmetic. Our design is targeting FPGA devices. The device capacities of current generation FPGAs are significantly smaller as compared to comparable ASICs. Building custom or single precision floating point arithmetic circuits has started becoming feasible with the device capacities of current generation FPGAs [192-195]. To be able to fit as many neuron blocks as possible on a single FPGA chip, the area occupied by each block should be as small as possible. Holt and Baker [44] and Holt and Hwang [45] investigated the minimum precision problem for neural networks with benchmark classification problems. According to their analysis, 16 bit fixed-point representation is sufficient for correct classification and training of the neural networks. Also, in our analysis of the applications considered here 16 bit precision is sufficient. Thus, all the internal parameters as well as inputs and outputs are represented as 16 bit fixed point numbers.
5.1.2 Activation Function Implementation

Activation functions are typically non-linear monotonically increasing sigmoid functions. Implementation choices include a circuit implementation for a piece-wise linear approximation of the function versus implementing a lookup table with preloaded \( f(x) \) values for the corresponding \( x \) input value. Direct circuit implementations of the activation function are significantly smaller in silicon footprint as compared to the LUT approach. The size of the LUT increases exponentially with the size of input. However, the direct circuit implementations are more complicated to design and may require redesign for each different activation function. In the case of an LUT-based approach, new values can be reloaded for a different activation function when required during the on-chip training process. As for the disadvantage of the required silicon area, the LUTs were implemented using the block RAMs in the Xilinx FPGAs. Since these block RAMs are already present on the die as hard-macros whether they are used or not, it made sense to use them to our advantage. Thus, minimal reconfigurable logic resources are used for activation function implementation. Port A of the on-chip dual port block RAM is configured as a read/write port. It is used to load the values into the lookup table. Port B is configured as a read only port and is used to interface with the neuron blocks. The size of the lookup table required is directly associated with the data widths used. A 16-bit fixed point representation requires a LUT that is 16 bits wide and \( 2^{16} \) deep. This requires a total of 128 KBytes per LUT. It would be desirable to use a separate LUT for every neuron block in the network so that all the neuron blocks are completely independent of each other. However, using a separate LUT for every neuron block can severely limit the number of blocks that can be implemented on a single FPGA chip. In our case, we can
implement only 2 neuron blocks on the Xilinx XC2VP30 FPGA chip before we run out of block RAMs. Sharing the LUT between all the neuron blocks requires serializing the access to the LUT of the neuron blocks using a FIFO, consequently slowing down the computational speed. Keeping in mind the dataflow implementation technique used here, only one neuron block in a column can ‘fire’ (process input data and producing outputs) in any computational time unit (this will be explained in further detail in the dataflow implementation section). Hence, a design decision was made to share a LUT between neuron blocks in a single column instead of all the blocks in the network. Thus there will be one LUT per column of neuron blocks in the network. This choice does increase the number of blocks that we can use in the network, but puts a constraint on the number of columns that can be implemented before the available block RAM become a bottleneck. The number of columns that can be implemented on our current FPGA chip would still be just two columns, severely limiting the network ability to solve any interesting problems. So, to further optimize the size of the LUT so that larger network grid sizes can be implemented on our FPGA chip, we implemented a LUT that was 16 bits wide but only $2^{12}$ deep. This reduces the size of the LUT to 8 Kbytes per LUT. This was done taking into consideration an observation that almost all of the activation functions that are used for artificial neurons are monotonically increasing saturating functions such as hyperbolic tangent and the logistic sigmoid functions. That is, the outputs taper off to a constant value beyond a certain input value. Thus there is no need to store the values greater than the maximum saturated output value repeatedly, in effect chopping off the activation function beyond the saturated values. Hence, the number of LUTs and hence
columns that can be implemented on the FPGA would be larger, not posing as a bottleneck for this implementation. This idea is illustrated in Figure 17.

### 5.1.3 Smart Block-based Neuron Design

One of the challenges here is to design a neuron block that can dynamically emulate all the various internal configuration modes. Kothandaraman designed a library of the various internal neuron block configurations for implementation on FPGAs [49]. The simplest approach for a dynamic neuron block would be to combine the library of designed blocks in a “super block” and use a multiplexer to select each depending on the structure gene. But the problem with this approach is that the silicon area required for such a super block will be four times that required by a single block, making this brute-force approach very inefficient. Instead a smarter block was designed that could dynamically emulate all the four internal configurations, but was less than a third the size.
of the brute force “super block” approach. This block design is called the ‘Smart Block-based Neuron’ (SBbN). The SBbN emulates any of the internal configuration modes depending on the values loaded in an internal configuration register called the ‘Block Control and Status Register’ (BCSR). This is a memory-mapped 16-bit internal block register in the internal configuration logic module of the neuron block that defines the state and mode of the neuron block. Also included is the support for deactivating a particular SBbN. In this state the inputs are just passed on to the outputs without modifications, essentially bypassing the neuron block. This was an important design choice to successfully implement an evolvable system as will be evident later. Figure 18 illustrates the idea of a smart block and Figure 19 shows the bit fields of the BCSR register. The BCSR register bits 7 through 4 that define the node directions are loaded automatically by the gene translation logic. This combinational logic circuit reads the structure gene register and loads the internal BCSR register inside each neuron block, thus setting their emulation modes depending on the corresponding value in the structure gene and the block’s position in the grid. This is illustrated in Figure 20. The sum of product pipeline has been implemented using the built in 18x18 multipliers in the Xilinx Virtex-II Pro FPGA.
Figure 18  Smart Block-based Neuron to emulate all internal neuron block configurations
**BCSR - Block Control and Status Register**

<table>
<thead>
<tr>
<th>Bits</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>15-12</td>
<td>reserved</td>
</tr>
<tr>
<td>11</td>
<td>AF1  Node 1 Activation function enable ('0' - Purelin / '1' - LUT AF)</td>
</tr>
<tr>
<td>10</td>
<td>AF2  Node 2 Activation function enable ('0' - Purelin / '1' - LUT AF)</td>
</tr>
<tr>
<td>9</td>
<td>AF3  Node 3 Activation function enable ('0' - Purelin / '1' - LUT AF)</td>
</tr>
<tr>
<td>8</td>
<td>AF4  Node 4 Activation function enable ('0' - Purelin / '1' - LUT AF)</td>
</tr>
<tr>
<td>7</td>
<td>ND1  Node 1 direction (hardcoded as '0' - Input)</td>
</tr>
<tr>
<td>6</td>
<td>ND2  Node 2 direction ('0' - Input / '1' - Output)</td>
</tr>
<tr>
<td>5</td>
<td>ND3  Node 3 direction ('0' - Input / '1' - Output)</td>
</tr>
<tr>
<td>4</td>
<td>ND4  Node 4 direction (hardcoded as '1' - Output)</td>
</tr>
<tr>
<td>3</td>
<td>DACT  Deactivate block</td>
</tr>
<tr>
<td>2</td>
<td>reserved</td>
</tr>
<tr>
<td>1</td>
<td>CB  Configuration busy signal</td>
</tr>
<tr>
<td>0</td>
<td>FM  Neuron fire mode signal</td>
</tr>
</tbody>
</table>

*Figure 19  Bit fields of Block Control and Status Register (BCSR) of SBBN*
Figure 20  Dynamic gene translation logic for internal configuration emulation
5.1.4 Dataflow Implementation

An issue with implementing data flow architectures like this one in hardware is to determine stable outputs and latch them. The problem is more pronounced when feedback is involved in the network structure. This work implements only feedforward BbNN networks. To solve the problem of latching the correct outputs, we implemented a control structure inspired by the Petri net model architecture. A Petri net (also known as a place/transition net or P/T net) is one of several mathematical representations of discrete distributed systems. As a modeling language it graphically depicts the structure of a distributed system as a directed bipartite graph with annotations. As such, a Petri net has place nodes, transition nodes, and directed arcs connecting places with transitions [196-198].

At any time during a Petri net's execution, each place can hold zero or more tokens. Unlike more traditional data processing systems that can process only a single stream of incoming tokens, Petri net transitions can consume tokens from multiple input places, act on them, and output tokens to multiple output places. Transitions act on input tokens by a process known as firing. A transition fires once each of the input places has one or more tokens. While firing, it consumes the tokens from its input places, performs some processing task, and places a specified number of tokens into each of its output places. It does this atomically, namely in one single, non-preemptible step.
The BbNN dataflow can be represented using an acyclic Petri net. Each of the blocks can be represented by an equivalent Petri net model as shown in Figure 21. The input and output registers can be represented by places. When each of the input registers (input places) have a valid input (a token), the BbNN fires and computes the outputs. Each of the output places will now get a token after the BbNN fires and the tokens at the input places are consumed. Thus the dataflow through a BbNN network can be represented using an equivalent Petri net network model (replacing each block with equivalent Petri net model as shown in Figure 21) for the entire BbNN network structure. Figure 22 shows the firing sequence for a particular BbNN network example. The side inputs have been hard-coded to be zero and have a valid token (shown as a ‘●’) until consumed by firing. When the top inputs are applied the input places get tokens and they fire, computing the outputs. As can be seen, only the blocks with valid input tokens fire and generate the corresponding input tokens for the neighbors, which in turn fire next. Figure 23 shows a logical block diagram of a SBbN block.
Figure 21 Equivalent Petri Net models for BbNN blocks
(a) 1/3 (b) 2/2 (c) 3/1
Figure 22 An example 2 x 2 BbNN firing sequence
Figure 23  SBbN neuron logical block diagram
5.2 Embedded Intrinsically Evolvable Platform

Block-based neural networks are evolved using genetic algorithms to find a suitable network for input – output mapping of training data. The details of the genetic evolution process are described in section 4.2. Section 5.1 gives details on the digital hardware design of the block-based neural network. The structure and internal parameters of the designed network can be dynamically updated without relying on FPGA runtime reconfigurations. The design is implemented on Xilinx Virtex-II Pro FPGA development boards. The implementation goal is to design an embedded, intrinsically evolvable platform for online evolution of BbNNs. This requires close coupling of the genetic evolution algorithm with the designed network. Multiple design choices were carefully considered for implementation, the details of which are given below.

a) Implementing Genetic Algorithms on a Host Computer

Here the GA is implemented as a software program running on a host computer that communicates with an FPGA configured with the neural network hardware via a serial link or bus interface such as PCI. The fitness evaluation is done on the FPGA configured with the hardware design of BbNNs. The problem with this choice is that the system is difficult to deploy as a standalone embedded system and would be bulky if implemented with embedded single board computers.
b) Implementing Genetic Algorithms in Hardware

Implementing GAs in hardware along with the BbNN network was the most obvious choice. Hardware implementations of different flavors of compact GAs have been reported in the literature [161, 162, 167, 168, 199], but it comes at a cost of significant resources on the FPGA. An on-chip GA implementation would require a memory bank to hold the population of chromosomes. It will also require a Gaussian random number generator implementation for mutation operation which again will require a memory bank to store lookup table values for a compact implementation using a uniform random number generator or a large logic implementation [200]. These required memory banks can be implemented in internal block RAMs available in the Virtex-II Pro FPGAs, but most of the block RAMs are tied up activation function LUT implementation. Building memory out of the rest of the reconfigurable fabric would be area inefficient and the resulting circuit slower limiting the size and performance of ANNs that can be implemented in hardware.

c) Implementing Genetic Algorithms on Embedded PPC405

Another choice is an approach similar to the first one, where the GA evolution is done in software running on a host processor. But in this case, the processor is an embedded processor on-chip in the Virtex-II Pro FPGA. The fitness evaluation, the most time consuming computation, is still implemented in the FPGA reconfigurable fabric. The advantage of this approach is that it uses the on-chip, embedded PowerPC 405 processor located on the same die as the rest of the reconfigurable fabric in the Virtex-II Pro FPGA. Thus, the system can be deployed as a compact, embedded, evolvable
platform in real-world applications. The fitness evaluation, which is the bottleneck in GA evolution strategy discussed here, is accelerated using the custom logic circuitry in the FPGA.

After comparing the pros and cons of the above approaches it was decided to implement the GA evolution on the PowerPC 405 embedded processor.

5.2.1 PSoC Platform Design

The BbNN platform was developed as a programmable System On-Chip (PSoC) architecture. Taking advantage of increased chip capacities, current-generation FPGAs have a number of on-chip hard macros such as embedded processors, memory, multipliers, and accumulator units. These available hard / soft cores with synthesizable local and peripheral bus systems can be used to build a powerful design platform on a single chip. These systems include one or more hard/soft processors and the associated local and peripheral bus systems with connected peripheral I/O cores on a single die. This platform is aptly called a System on a Chip (SoC). These platforms synthesized on FPGAs can be reconfigured and hence are called as programmable SoC (PSoC) architectures. The embedded processors use internal FPGA RAMs for implementing instruction and data memories. The embedded processor interfaces to on-chip memory controllers via a local system bus. Peripherals like UART, ethernet MACs and other custom user cores communicate with the processor via the local system bus or the peripheral bus. The peripheral bus communicates with the local system bus via a bridge.
The on-chip memory controllers can interface to on-chip or off-chip memory systems which are mapped to the embedded processor’s address space. The processor powers up and executes a bootstrap routine initialized in its instruction memory, which can make calls to user programs resident either in internal on-chip or external off-chip memory locations. These user programs can be simple self test codes for various connected peripherals or even a real-time operating system that can boot up to a command prompt. Many real-time operating system vendors such as VxWorks [201], Timesys Linux [202], and Montavista Linux [203] have support for various PSoC platforms. Figure 24 shows a logical diagram of a typical SoC design. PSoC platforms can also be efficiently used as test platforms for user cores. User cores can communicate with the embedded processor via the peripheral bus system. The processor can be used to send test vectors to the user design and receive and analyze the results.

The PSoC platform for BbNN is designed using the Xilinx Embedded Development Kit (EDK). It includes a PPC405 processor along with on-chip local memory communicating via Processor Local Bus (PLB). Other peripherals such as a UART for serial communication can be connected as slaves on an On-Chip Peripheral Bus (OPB). The BbNN hardware network is memory-mapped to the PPC 405 and interfaced via the OPB bus. It raises an interrupt on task completion that is connected through the OPB interrupt controller to the PPC interrupt mechanism. Interrupt-driven I/O programming helps in facilitating the real-time processing and scheduling often required in many embedded applications of the evolvable neural network platform. The platform is shown in Figure 25. The fixed point GA code runs on the on-chip PowerPC
Figure 24 Programmable System on a Chip - logical diagram
processor. The BbNN hardware design is used for fitness evaluation. Internal network parameters, such as the structure and weight genes, network inputs, and outputs are memory-mapped to the processor. The activation function LUT also is memory mapped in the address space of the PPC405.

5.3 Fixed Point BbNN Software for Genetic Evolution

The fixed point GA evolution software is written in the C programming language. The on-chip PPC405 only has a fixed point datapath. Any floating point operations have to be performed using emulated floating point software libraries which are slow. Care has been taken to minimize the required floating point operations. All the real values have been stored as 16-bit fixed point values. The genetic operators of selection, crossover, and mutation have been implemented as detailed in chapter 4. Genetic evolution
parameters such as the maximum number of generations, structure / weight crossover and mutation probabilities, step size for weight mutation, target fitness, elitist mode genetic evolution selection, number of offspring in each new generation, activation function selection (tansig, logsig, satlin, purelin, hardlim), selection algorithm (roulette, ranking, tournament, proportion), and network grid sizes to evaluate can be set in a header file. The software is cross-compiled to PPC 405 object code and can be loaded in the onboard program flash. Fixed point BbNN fitness evaluation software routines have also been programmed for use in a fixed point BbNN software simulator compiled for PC. These routines also help in exhaustive BbNN FPGA design testing. The code appears in the appendix.

5.4 Performance and Device Utilization Summary

The post-synthesis timing analysis of the design reports a clock frequency of 245MHz on the Xilinx Virtex-II Pro FPGA (XC2VP30). Each block takes at the most 10 CLK cycles to complete processing the inputs and produce an output. The number of clock cycles depends on the internal block configuration and the number of output nodes using the activation function LUT. Each block computation processes 6 synaptic connections. Thus, each block has a peak connection per second speed of 147 MCPS per block for a 16 bit data width. With generally more than one block computing at a time, depending on the network structure the peak CPS would be \( (n \text{ computing blocks}) \times (147 \text{ MCPS} / \text{ block}) \) processing speed. Considering an \( m \times n \) BbNN grid the processing speed can vary between 147 MCPS to 147\( n \) MCPS, depending on the network structure.
The minimal platform excluding the BbNN network needs about 13% of the Xilinx Virtex-II Pro FPGA (XC2VP30) resources. Table 2 shows the post-synthesis device utilization summaries for various BbNN network sizes excluding the rest of the platform. According to the utilization summaries we can fit around 20 neuron blocks on a single FPGA chip along with the rest of the platform. Table 3 shows the post-synthesis device utilization summary for a larger FPGA device (XC2VP70) in the Xilinx Virtex-II Pro family, widely used in many commercially available FPGA boards. This device can hold around 48 neuron blocks.

5.5 Design Scalability

An important consideration in design decisions is that of design scalability issues. There is a physical limitation on the number of neurons that can fit on a single FPGA. So the question arises on how to support applications requiring larger network sizes? BbNN hardware was designed taking into consideration scenarios for design scalability. The P/T net-based dataflow implementation strategy ensures reliable asynchronous communication between neuron blocks. This is important for scalability as will be evident in the following discussion of scalability scenarios. The design supports these scenarios, but their implementation is left as future work.
Table 2  Device Utilization Summary on Xilinx Virtex-II Pro FPGA (XC2VP30)

<table>
<thead>
<tr>
<th>Network Size</th>
<th>Number of Slice Registers</th>
<th>Number of block RAMs</th>
<th>Number of MULT18x18s</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Used</td>
<td>Utilization</td>
<td>Used</td>
</tr>
<tr>
<td>2 x 2</td>
<td>2724</td>
<td>19%</td>
<td>8</td>
</tr>
<tr>
<td>2 x 4</td>
<td>4929</td>
<td>35%</td>
<td>16</td>
</tr>
<tr>
<td>2 x 6</td>
<td>7896</td>
<td>57%</td>
<td>24</td>
</tr>
<tr>
<td>2 x 8</td>
<td>10589</td>
<td>77%</td>
<td>32</td>
</tr>
<tr>
<td>2 x 10</td>
<td>12408</td>
<td>90%</td>
<td>40</td>
</tr>
<tr>
<td>3 x 2</td>
<td>3661</td>
<td>26%</td>
<td>8</td>
</tr>
<tr>
<td>3 x 4</td>
<td>7327</td>
<td>53%</td>
<td>16</td>
</tr>
<tr>
<td>3 x 6</td>
<td>11025</td>
<td>80%</td>
<td>24</td>
</tr>
<tr>
<td>3 x 8</td>
<td>14763</td>
<td>107%</td>
<td>32</td>
</tr>
<tr>
<td>3 x 10</td>
<td>18456</td>
<td>134%</td>
<td>40</td>
</tr>
<tr>
<td>4 x 2</td>
<td>4783</td>
<td>34%</td>
<td>8</td>
</tr>
<tr>
<td>4 x 4</td>
<td>9646</td>
<td>70%</td>
<td>16</td>
</tr>
<tr>
<td>4 x 6</td>
<td>14587</td>
<td>106%</td>
<td>24</td>
</tr>
<tr>
<td>4 x 8</td>
<td>19508</td>
<td>142%</td>
<td>32</td>
</tr>
<tr>
<td>4 x 10</td>
<td>24461</td>
<td>178%</td>
<td>40</td>
</tr>
</tbody>
</table>
Table 3  Device Utilization Summary on Xilinx Virtex-II Pro FPGA (XC2VP70)

<table>
<thead>
<tr>
<th>Network Size</th>
<th>Number of Slice Registers</th>
<th>Number of block RAMs</th>
<th>Number of MULT18x18s</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Used</td>
<td>Utilization</td>
<td>Used</td>
</tr>
<tr>
<td>2 x 2</td>
<td>2497</td>
<td>7%</td>
<td>8</td>
</tr>
<tr>
<td>2 x 4</td>
<td>4929</td>
<td>14%</td>
<td>16</td>
</tr>
<tr>
<td>2 x 6</td>
<td>7390</td>
<td>22%</td>
<td>24</td>
</tr>
<tr>
<td>2 x 8</td>
<td>9915</td>
<td>29%</td>
<td>32</td>
</tr>
<tr>
<td>2 x 10</td>
<td>12403</td>
<td>37%</td>
<td>40</td>
</tr>
<tr>
<td>3 x 2</td>
<td>3661</td>
<td>11%</td>
<td>8</td>
</tr>
<tr>
<td>3 x 4</td>
<td>7327</td>
<td>22%</td>
<td>16</td>
</tr>
<tr>
<td>3 x 6</td>
<td>11025</td>
<td>33%</td>
<td>24</td>
</tr>
<tr>
<td>3 x 8</td>
<td>14788</td>
<td>44%</td>
<td>32</td>
</tr>
<tr>
<td>3 x 10</td>
<td>18461</td>
<td>55%</td>
<td>40</td>
</tr>
<tr>
<td>3 x 12</td>
<td>22233</td>
<td>67%</td>
<td>48</td>
</tr>
<tr>
<td>3 x 14</td>
<td>25652</td>
<td>77%</td>
<td>56</td>
</tr>
<tr>
<td>3 x 16</td>
<td>29254</td>
<td>88%</td>
<td>64</td>
</tr>
<tr>
<td>4 x 2</td>
<td>4783</td>
<td>14%</td>
<td>8</td>
</tr>
<tr>
<td>4 x 4</td>
<td>9646</td>
<td>29%</td>
<td>16</td>
</tr>
<tr>
<td>4 x 6</td>
<td>14561</td>
<td>44%</td>
<td>24</td>
</tr>
<tr>
<td>4 x 8</td>
<td>19534</td>
<td>59%</td>
<td>32</td>
</tr>
<tr>
<td>4 x 10</td>
<td>24470</td>
<td>73%</td>
<td>40</td>
</tr>
<tr>
<td>4 x 12</td>
<td>29221</td>
<td>88%</td>
<td>48</td>
</tr>
<tr>
<td>4 x 14</td>
<td>34389</td>
<td>103%</td>
<td>56</td>
</tr>
</tbody>
</table>
5.5.1 Scaling BbNN Across Multiple FPGAs

An obvious choice to scale the network sizes is to distribute smaller sub-networks of the BbNN network across multiple FPGAs to execute in parallel. But this is not trivial to achieve due to the inter-neuron block synaptic communications within the network. These communications will have to be performed across multiple FPGA chips. This will require taking into consideration delay times associated with the communication links between the FPGAs. The FPGAs could be connected directly via dedicated inter-communication channels or may have to go through the host processor and use communication links such as Ethernet existing between the host machines. These issues were considered during the design stage of the BbNN hardware implementation. The choice of using the P/T net-based reliable, asynchronous inter-neuron block communication was made to address the scalability issues. Asynchronous communication ensures reliable performance irrespective of the delays associated with the communication links. This makes the design portable and scalable across a heterogeneous mixture of reconfigurable computing resources and their intercommunication channels.

5.5.2 Scaling via Time Folding

BbNNs can also be scaled via time-multiplexing. A single BbNN FPGA implementation can be used to execute sub-networks of a larger BbNN at different instances of time. The intermediate sub-network states (intermediate inputs and outputs of the sub-network, sub-network structure, and internal parameters) can be saved in buffer memory between the execution cycles. The intermediate sub-network states saved
in the buffer memory can be loaded on the BbNN FPGA implementation in appropriate 
execution cycles to compute sub-network outputs that are input to other sub-networks. 
Scaling the BbNN in time has the disadvantage of serializing the sub-network execution. 
Thus, it requires longer execution times but lesser hardware resources.

5.5.3 Hybrid Implementation

A hybrid approach employing both time and space scaling techniques can also be 
used for large networks. It is a problem of reliably mapping and scheduling sub-networks 
across FPGA resources. It involves development of efficient partitioning and scheduling 
algorithms for optimal usage of available resources and minimizing execution runtimes.

5.6 Applications

BbNNs can be applied to many applications suitable for neural networks. We 
tested our on-chip training approach with a few example applications and the results are 
discussed below.

5.6.1 N-bit Parity Classifier

A parity bit is a binary bit that indicates whether the number of bits with value of 
one in a given set of N-bits is even or odd. The N-bit parity technique is widely used for 
error detection in real world applications such as serial data transmission, SCSI bus, 
microprocessor caches, and redundant arrays of inexpensive disks (RAID). The BbNN
The platform solves the $N$-bit parity computation problem using on-chip genetic evolution. The results of the genetic evolution process are as follows. Table 4 shows the genetic algorithm parameters used for evolution. A population size of 30 chromosomes per generation was used with crossover and mutation probabilities of 0.7 and 0.1 respectively. Tournament selection was used for choosing candidates for crossover operation to produce offspring. A logistic sigmoid function was used as an activation function for the neuron block outputs. Figure 26 shows the average and maximum fitness values for each generation for the 3-bit and 4-bit parity examples. As can be seen from the curves the target fitness of 1.0 is reached after 132 generations in the case of the 3-bit parity example and 465 generations for the 4-bit parity example. The fitness functions used for genetic evolution are the same as shown in section 4.2.3. Figure 27 shows the dominant structure evolution trends for the 3-bit and 4-bit parity examples. Each color shows the evolution trend of a unique structure. Each curve shows the number of chromosomes per generation that has that structure. Figure 28 shows the evolved networks for the 3-bit and the 4-bit parity examples.

<table>
<thead>
<tr>
<th>Genetic Algorithm Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Population size</td>
<td>30</td>
</tr>
<tr>
<td>Target Fitness</td>
<td>1.0</td>
</tr>
<tr>
<td>Structure crossover probability</td>
<td>0.7</td>
</tr>
<tr>
<td>Structure and weight mutation probabilities</td>
<td>0.1</td>
</tr>
<tr>
<td>Activation Function</td>
<td>Logistic sigmoid</td>
</tr>
<tr>
<td>Selection Strategy</td>
<td>Tournament selection</td>
</tr>
</tbody>
</table>
Figure 26 Fitness evolution trends for (a) 3-bit and (b) 4-bit parity examples
Figure 27  Structure evolution trends for (a) 3-bit and (b) 4-bit parity examples
Figure 28 Evolved networks for (a) 3-bit and (b) 4-bit parity examples
The selection, crossover, and mutation genetic operators used to produce new generations execute on the on-chip PowerPC processor. The execution time to execute the assembly instructions to produce each generation depends on the population size, the number of new offspring produced per generation, and the crossover and mutation probabilities. For the case of the $N$-bit parity example, the average time it takes to produce a new generation on the PPC405 processor running at 300MHz is 11 $\mu$s. The population fitness evaluation speed depends on the population size, network structure of individuals in the population, designated output nodes, and number of input patterns. For the $N$-bit parity example, the fitness processing speed ranges from 147 MCPS to 294 MCPS.

### 5.6.2 Iris Plant Classification

Plant classification is the identification of the plant by observing some unique attributes such as shape or area of the leaves. Specific shape measurements such as length and width of the leaves or their area are typically used to automate the classification using machine learning techniques such as neural networks. The Iris plant classification problem addressed here is a widely used benchmark for neural classifiers originally compiled by R.A Fisher [204]. The Iris plant database has data for three classes of Iris plants, Iris Setosa, Iris Versicolour and Iris Virginica. The dataset has a total of 150 samples, with 50 samples per class instance. The dataset attributes are sepal length, sepal width, petal length, and petal width for the three classes of the Iris plants. The Iris Setosa class is linearly separable from the other two classes, Iris Versicolour and Iris Virginica.
The latter are not linearly separable from each other. BbNN was used to classify the plants in this dataset. The results show less than a 1.5% misclassification rate (see Figure 29). For this BbNN genetic evolution, the entire set of 150 samples was used as the training dataset. The inputs for the network are the sepal area and the petal area calculated by multiplying the sepal width with the sepal length, and the petal width with the petal length, respectively. The population size of 80 chromosomes was used for evolution over 10,000 generations. The structure crossover and mutation probabilities were set at 0.7 and 0.1, respectively. The weight mutation probability was set at 0.1. Table 5 shows the various genetic evolution parameters used. Figure 30 shows the average and maximum fitness trends of the genetic evolution process. Maximum fitness of 0.99 was achieved after 9403 generations. Figure 31 shows the top few structure evolution trends. As before, each color is a unique BbNN structure. The values of the curves indicate the number of chromosomes with the same structure in the particular generation. Figure 32 shows the evolved network. In the case of the Iris plant classification example, the average time it takes to produce a new generation on the PPC405 processor running at 300MHz is 23 µs. As discussed above, the population fitness evaluation speed depends on the population size, network structure of individuals in the population, designated output nodes, and number of input patterns. The fitness processing speed for the Iris plant classification example ranges from 147 MCPS to 441 MCPS.
Table 5 Genetic evolution parameters used for Iris classification problem

<table>
<thead>
<tr>
<th>Genetic Evolution Parameters</th>
<th>Values</th>
</tr>
</thead>
<tbody>
<tr>
<td>Population size</td>
<td>80</td>
</tr>
<tr>
<td>Maximum generations</td>
<td>10,000</td>
</tr>
<tr>
<td>Target Fitness</td>
<td>1.0</td>
</tr>
<tr>
<td>Structure and weight crossover probabilities</td>
<td>0.7</td>
</tr>
<tr>
<td>Structure and weight mutation probabilities</td>
<td>0.2</td>
</tr>
<tr>
<td>Activation Function</td>
<td>Tangent sigmoid</td>
</tr>
<tr>
<td>Selection Strategy</td>
<td>Tournament selection</td>
</tr>
</tbody>
</table>

Figure 29 BbNN training error for Iris plant classification database. Results show less than 1.5% misclassification rate
Figure 30  Fitness trends was Iris plant classification using BbNN

Figure 31  Structure evolution trends for Iris plant classification using BbNN
Figure 32  Evolved BbNN network for Iris plant classification database
5.7 Summary

This chapter presents the FPGA design details of the evolvable BbNN platform. The design was targeted for a Xilinx Virtex-II Pro FPGA (XC2VP30) housed on a Xilinx University Program (XUP) FPGA development board or an Amirix AP130 FPGA development board. The implementation is an intrinsically evolvable, functional-level EHW platform. The functional units are the neuron blocks of the BbNN.

BbNNs are evolved using genetic algorithms to learn the characteristics of the training input patterns. The evolution is a multi-parametric optimization problem requiring simultaneous network structure and synaptic weight optimizations. The network structure defines the dataflow through the network from the inputs to the outputs and the internal configurations of the neuron blocks. Each neuron block can have one of the four possible internal configurations depending on the positions of the inputs and the outputs. The SBBN implementation presented dynamically adapts to different internal neuron block configurations based on the network structure specified in the BbNN chromosome. The synaptic weights and biases have been implemented as registers and can be updated dynamically. Thus, the implementation of the BbNNs presented here can be evolved intrinsically on the FPGA and does not require any runtime FPGA reconfiguration cycles. This saves the overheads of FPGA reconfiguration times that are typically in millisecond range (see section 2.5.2.2). The dataflow between the neuron blocks is handled asynchronously using a P/T dataflow network model. This enables larger networks to be scaled across multiple FPGAs and evolve in parallel or to use the same FPGA network in
a time-multiplexed manner for larger networks that cannot be accommodated on a single FPGA. The genetic algorithm used to evolve the BbNNs runs on the on-chip PowerPC processor in the Virtex-II Pro FPGA. The population fitness evaluations are performed directly on the BbNN hardware. Thus, the system can be deployed as a compact, embedded, evolvable platform in real-world applications.

Chapter 6 introduces the online learning with the BbNNs and presents an application that demonstrates the intrinsic online evolution capability of the design.
BbNNs can be used for applications of artificial neural networks such as pattern classification, signal prediction, function approximation, process control and feature recognition. In the past, BbNNs have been applied to mobile robot navigation [23], multivariate gaussian distributed pattern classification [182], chaotic time series prediction [183], ECG signal classification and heart beat monitoring [4, 5], and Iris plant classification [186]. The on-chip training capability of the developed BbNN platform extends its capabilities to a number of different applications in dynamic environments.

A recurring concern of using artificial neural networks in practical applications is its ability to generalize and apply its training knowledge satisfactorily. A training dataset that is a good representative set of the actual data that the network may be exposed to in practice is important for good generalization. But this is difficult to achieve, especially in dynamic or unpredictable environments requiring retraining of structure and parameters of the network. Under such circumstances the ability of online training is important to maintain reliable system performance. The on-chip training capability of the developed BbNN platform is ideally suited for applications in dynamic environments. This chapter presents an online training approach for BbNN platform and an application to demonstrate its capabilities.
6.1 Online Training Approach

With the advantage of on-chip training capability, the developed BbNN platform can be deployed in dynamic environments and programmed to adapt to variances in environmental stimuli. The network can be deployed in an actor-critic fashion with the network in the active mode performing the actor’s role and a critic analyzing the responses of the network to the environmental stimuli. There are three online evolvable system deployment scenarios envisioned.

1. The deployed network is in active mode producing the outputs to input stimuli from the environment. The critic constantly analyzes the network’s performance and on recognizing deviations beyond a certain threshold either in the expected network outputs, the inputs, or performance, can trigger a network retraining cycle to adapt to the variances in the environment. In this scenario the network is switched between the training and the active modes as dictated by the critic.

2. In the second scenario, the network can be scheduled to automatically switch between the training and the active modes in a time-multiplexed approach. The critic, on detecting deviations in performance beyond the threshold, can deploy the last known fittest network obtained in the training mode to the active mode to improve the system performance. This is illustrated in Figure 33.
Figure 33  Single network scheduled to switch between training and active modes
3. Instead of switching a single network between training and active modes, two networks could be used simultaneously, with one in the active mode and the other in the background training mode. As before, the critic can load the last known fittest network from the training mode to the active mode to improve system performance to the variances in the environmental stimuli. This is illustrated in Figure 34.

In each of the above scenarios, the network is expected to be trained online. In the genetic evolution approach discussed in section 4.2 and used to evolve BbNNs, genetic operators such as selection, crossover, and mutation are used to produce offspring for the new generation. The new population is ranked using the computed fitness levels of the individuals. The rankings are used in the selection process to choose mates for the genetic crossover. The fitness of each individual in the generation is determined by evaluating the outputs of the network to the input training patterns. The computed outputs are compared with known target outputs to determine the mean squared error. The fitness level of the network is proportional to the computed mean squared error. This approach is convenient for offline training in supervised mode with known target outputs for the input training patterns. In the case of online training, target outputs for incoming input patterns are generally not known. This makes determining the fitness of the population difficult. In such scenarios, population fitness has to be estimated from actual or estimated environmental responses to computed outputs. This is illustrated in the equations below.
Figure 34 Two networks scenario. One in active mode and the other in training mode
Network output is a function of the inputs, the current environmental state, and the network structure and parameters. Thus, if the inputs are $X_t$, the current environmental state is $S_t$, and $K_n$ represents the network parameters, then the network output is a function of these variables as shown below.

$$Y_t = f(X_t, S_t, K_n)$$

(7)

The new state $S_{t+1}$ of the environment is a function of the previous state $S_t$ and the outputs $Y_t$ as shown below.

$$S_{t+1} = f(Y_t, S_t)$$

(8)

The estimated fitness is the function of the new state $S_{t+1}$ and the desired state $S_{t+1}^\wedge$ of the environment.

$$F_n = f\left(S_{t+1}, S_{t+1}^\wedge\right)$$

(9)

If the fitness can be estimated with reasonable confidence level, the genetic algorithm approach used in the offline supervised evolution can be used for online evolution.
6.2 Online Evolution of BbNNs

The intrinsically evolvable BbNN platform (see chapter 5) can be adapted in-field via online evolution. This capability vastly enhances BbNN system performance and usability for applications in dynamic environments. This section gives details of the online evolution model that can be used with BbNNs.

Consider two system models with states $S_1$ and $S_2$ as shown in Figure 35. The outputs $y_t$ of the system $S_1$ control the behavior of the system $S_2$ as shown. Outputs $y_t$ are a function of the inputs $x_t$ to the system $S_1$ and parameters $m_k$ of system $S_1$ as shown below.

$$y_t = f(x_t, m_k)$$  \hspace{1cm} (10)

The inputs $x_t$ to system $S_1$ can be computed by observing the current state of system $S_2$. The goal is to keep system $S_2$ in a desired state $\hat{S}_2(t)$ by controlling its behavior using signal $y_t$. The system state of $S_2$ is deterministic and depends on control
input $y_t$ and the current value of an input time-varying signal $u(t)$ to system $S_2$. $u(t)$ signal behavior depends on external factors that may not be controllable by our system models. To maintain system $S_2$ in the desired state at all times, it is essential to predict the future behavior of signal $u(t)$ in advance to adjust $S_1$ model parameters $m_k$ that control the $S_2$ system inputs $y_t$.

We can use online evolution with the BbNNs to predict the future values of the signal $u(t)$ from its current and past values. The current value of the signal $u(t)$ can be determined as shown below.

$$u(t) = f(\tilde{S}_2(t), \bar{S}_2(t), \bar{y}(t))$$

The expected system state at time $t$, $\bar{S}_2(t)$ is a function of control inputs $y_t$ to the system $S_2$ as shown below.

$$\bar{S}_2(t) = f(y_t)$$

The current value of $u(t)$ can be computed from the observed state $S_2(t)$, the expected state $\bar{S}_2(t)$, and the predicted $\bar{u}(t)$.

$$u(t) = f\left(S_2(t), \bar{S}_2(t), \bar{u}(t)\right)$$
Thus, recent history of the $u(t)$ signal values can be used to train the BbNNs online. This signal prediction technique is called a time delayed neural network (TDNN) as is illustrated in Figure 36 [3]. The overall system performance can be determined from observed and target system states by computing mean squared error as shown below.

\[
E = \frac{1}{N_s} \left( S_2(t) - \hat{S}_2(t) \right)^2
\]  

(13)

\[
P = \frac{1}{1 + E}
\]  

(14)

Where, $N_s$ and $P$ are the number of state parameters and system performance respectively. On analyzing error signal $E$ the critic can choose to trigger an online re-train cycle (as in scenario 1 in section 6.1) or load the last known fittest network from the training mode to the active mode (as in scenarios 2 and 3 in section 6.1) to improve the system performance.

The above described general system model is applicable to many real-world application scenarios such as cruise control systems in automobiles, industrial process
control, prediction of solar radiation dosage levels, or guidance systems in aircraft. The following section demonstrates online evolution of BbNNs using an example application.

6.3 Case Study: Adaptive Neural Luminosity Controller

An important issue facing this generation is the global climate change due to the effects of greenhouse gas emissions and increased energy consumption. Conservation of energy is of prime importance to check the greenhouse gas emissions and conserve depleting resources. According to the Clinton Climate Initiative (CCI) program of former US president William J. Clinton, 75% of the global emissions of greenhouse gases come from the cities and 50% of the city’s emissions are generated by its buildings. The CCI program is fervently promoting a Global Energy Efficiency Building Retrofit Program to reduce energy consumption in a city’s buildings [205]. The benefits of energy conservation in buildings not only helps fight global climate change but also results in considerable savings in energy costs. This application is motivated by the needs of energy conservation and reducing the energy costs.

A huge portion of the energy consumption in a building is the lighting. Most people prefer illuminated corridors and well lit rooms and hallways in the buildings. Our aim is to control the lumen outputs of the lamps in the buildings to maintain a sufficient illumination as per requirements at different times of the day. The amount of illumination in a room varies depending on the ambient light intensity, which is dependent on factors such as time of day, windows, shades and curtains, and object shadows. These factors are
time and space variant and hence the amount of illumination in a room varies with the ambient light intensity levels. To provide the target illumination levels we need to intelligently control the lumen outputs of the lamps illuminating a room depending on the ambient light intensity levels.

This application fits the system model described in section 6.2. Signal $y_t$ corresponds to the control inputs to the electronic ballasts used to regulate the light intensity outputs of the lamps. Signal $x_t$ can be obtained by observing the current light intensity levels, i.e. the outputs of the light sensors in the room. The time varying signal $u(t)$ is the ambient light intensity and the desired target state $\hat{S}_2$ is the target light intensity level. If the ambient light intensity levels can be predicted we can control the luminosity levels in the room by adjusting the control inputs to the electronic ballasts. To predict the ambient luminosity levels in the room we used online evolution with BbNNs.

The following discussion lays out the simulation experimental setup and the approach.
6.3.1 Simulation Experimental Setup

Figure 37 shows a layout (top view and front view) of a room with area $30' \times 10'$ used as the reference room for our simulation experiment. The room has 7 fluorescent light fixtures and 2 light sensors attached to the ceiling as shown. The reference illumination surface is an oblong conference table shown in the figure. The distances between light and sensor placements as well as the reference surface are as shown in Figure 37. The room has a large window (not shown in the front view) on the wall opposite to that of the door. Each light fixture has associated electronic ballast used to control lumen output of the lights. The ballasts are assumed to be similar to Lutron Eco-10™ TVETM, fluorescent dimming ballast from Lutron Electronics Co [206]. The ballasts support continuous, flicker-free dimming from 100% to 10% of measured relative light output with control inputs ranging from 0-10VDC. Further, the ballasts have a linear dimming curve with respect to control input voltage as shown in Figure 38 [206]. For the sake of our simulation we will assume that all the fluorescent lamps are identical in terms of their lumen outputs and corresponding power consumption. The contribution to the light intensity levels on the reference surface by the lamps will be governed by the inverse square law. This means, if a lamp lumen output is $L$ foot-candles (FC) then the light intensity at a point at a distance $d$ from the lamp source will be $L / d^2$. The light sensors used are linear photodiode sensors similar to commercial sensors available from PLC Multipoint Inc. [207]. These are low voltage light sensors with linear voltage signal characteristics with respect to the measured light intensity. The plot in Figure 39 illustrates the linear output characteristics of the photodiode sensors.
Figure 37  Layout of the reference room used for simulation
Figure 38  Plot of measured relative light output (%) versus ballast control input

Figure 39  Plot of sensor signal output (V) versus measured light intensity (in percent of calibrated peak intensity)
The sensors can be calibrated via a potentiometer to change the sensitivity or foot-candles/volt to adjust the range of sensed light intensity. For simplification we will ignore various lumen losses and lumen output variations due to ambient temperature variations, ballast factor loss, and other optical obstruction factors such as light fixtures, or dust in our calculations. We will also assume that the power consumption of fluorescent lamps is linear with respect to measured light output. This is a fair assumption to make in the case of fluorescent lamps [208]. Table 6 gives the specifications of the lights and sensors used in the test room.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Number of lights</td>
<td>7</td>
</tr>
<tr>
<td>Number of sensors</td>
<td>2</td>
</tr>
<tr>
<td>Cost function factor weights ($q_1,q_2,q_3$)</td>
<td>1.0</td>
</tr>
<tr>
<td>Ballast dimming range</td>
<td>10% – 100% RLO</td>
</tr>
<tr>
<td>Ballast control signal range</td>
<td>0 – 10 V DC</td>
</tr>
<tr>
<td>Slope of ballast curve</td>
<td>756</td>
</tr>
<tr>
<td>Calibrated sensor range</td>
<td>0 – 420 FC</td>
</tr>
<tr>
<td>Sensor output range</td>
<td>0 – 9V DC</td>
</tr>
<tr>
<td>Sensor sensitivity</td>
<td>0.02 V/FC</td>
</tr>
<tr>
<td>Lamps per fixture</td>
<td>3</td>
</tr>
<tr>
<td>Lamp power rating</td>
<td>32 W / lamp</td>
</tr>
<tr>
<td>Max lumen output of the lamp</td>
<td>2800 lm / lamp</td>
</tr>
<tr>
<td>Lamp efficacy</td>
<td>87.5</td>
</tr>
<tr>
<td>Peak illumination capacity (at 0% ambient intensity)</td>
<td>420 FC</td>
</tr>
<tr>
<td>% Relative light output at zero ballast control input</td>
<td>10%</td>
</tr>
<tr>
<td>Distances between lamps and surface reference points</td>
<td>Calculated using data in Figure 37</td>
</tr>
<tr>
<td>Re-training trigger threshold</td>
<td>5 FC</td>
</tr>
</tbody>
</table>
6.3.2 Adaptive BbNN Predictor

As discussed in section 6.2, we will use collected history of the ambient light intensity levels during the course of the day to train the BbNNs using genetic algorithms for predicting the future ambient light intensity levels. Ambient light intensity level at the current time step ‘t’ can be estimated from the current luminosity readings of the reference surface by the light sensors and the expected light intensity levels at the reference surface due to the lamp outputs. For our simulation example we will assume the identical ambient light intensity levels throughout the entire reference surface.

\[
L_A = L_{S_j} - \sum_{i=1}^{N} \frac{L_i}{d_i^2}
\]

(15)

where,

- \(L_{S_j}\) Light intensity at reference surface of sensor \(S_j\)
- \(L_i\) Lumen output of light fixture \(i\)
- \(N\) Total number of light fixtures
- \(d_i\) Distance in feet between the light fixture \(i\) and reference surface
- \(L_A\) Ambient light intensity at reference surface

For our simulation purposes we will assume the ideal ambient light intensity varies at different times of day (time step = 10 mins) as shown in Figure 40. The luminosity levels in the plot are % of the peak light intensity at the reference surface provided by all the light fixtures running at full capacity and 0 foot-candle ambient light levels. This is about 420 foot-candles for our test room as calculated from maximum lamp lumen outputs and the distances between reference surface and the lamps. This
value is given in the specifications chart in Table 6 above. The following are the simulation experimental steps.

### 6.3.2.1 Step 1: Pre-training the BbNN

The BbNN predictor is first pre-trained using offline genetic evolution with the ideal values of the ambient light intensity levels. Figure 41 shows the training results and Figure 42 shows the prediction error. As can be seen the peak error is less than 0.6%. Figure 43 shows the fitness trends over generations. Only the first 500 generations have been shown in the figure to highlight the population fitness improvements in the first 100 generations. The maximum fitness of 0.99 was achieved in 1557 generations. Figure 44 shows the corresponding evolved BbNN network. Table 7 shows the GA evolution parameters used.

![Ideal ambient and target luminosity levels](image)

**Figure 40  Ideal luminosity levels in the test room**
Figure 41  Results of the BbNN pre-training. Plot shows the actual and the predicted ambient luminosity values as learnt by BbNN

Figure 42  Prediction error for the offline evolution
Figure 43  Average and maximum fitness values over generations (offline evolution)

Table 7  Genetic evolution parameters used for BbNN predictor

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Activation Function</td>
<td>Hyperbolic tangent function</td>
</tr>
<tr>
<td>Selection Strategy</td>
<td>Tournament selection</td>
</tr>
<tr>
<td>Population size</td>
<td>80</td>
</tr>
<tr>
<td>Maximum generations</td>
<td>2000</td>
</tr>
<tr>
<td>Structure Crossover probability</td>
<td>0.7</td>
</tr>
<tr>
<td>Structure Mutation probability</td>
<td>0.3</td>
</tr>
<tr>
<td>Weight Mutation probability</td>
<td>0.3</td>
</tr>
<tr>
<td>Number of patterns</td>
<td>120</td>
</tr>
<tr>
<td>Inputs per pattern</td>
<td>4</td>
</tr>
<tr>
<td>Evolution strategy</td>
<td>Ellitist evolution</td>
</tr>
</tbody>
</table>
Figure 44  Evolved BbNN after 1557 generations
To simulate dynamic ambient light intensity behavior we will assume two cases, (i) a cloudy day with lower ambient luminosity than the ideal level shown above, and (ii) a sunny day with higher ambient luminosity levels. These are shown in Figure 45. Figure 45 also shows the target luminosity levels required in the room at different times of the day. The pre-trained BbNN network is then deployed in field to predict the ambient luminosity levels. The critic observes the BbNN’s prediction for time step ‘t’ and compares it with the ambient light intensity level observed during time step ‘t’ to judge BbNN’s performance under current conditions. On noticing a deviation of 0.05 it triggers an online re-training cycle for the BbNN predictor. The online training uses the ambient intensity values collected since the first time step (4.00) for training the network. The genetic evolution parameters are the same as the ones used for offline training shown in Table 7.

![Figure 45 Ambient luminosity test cases and expected target luminosity](image.png)

**Figure 45** Ambient luminosity test cases and expected target luminosity
6.3.2.2 Step 2: Simulating BbNN Predictor Operation (Cloudy day)

Figure 46 shows the ambient luminosity pattern learned by the BbNN during offline training and the current ambient luminosity pattern. The BbNN predicts the ambient light reasonably well until 7:50. The critic notices a deviation greater than 0.05 in the predicted ambient intensity value at time step 8:00 and triggers the first online re-training cycle. Note, Figure 46 also shows the predictions that the BbNN predictor would have made beyond 8:00 without online re-training. Figure 47 shows the improved predictions after the first re-training cycle. The critic again notices a deviation greater than 0.05 in the predicted ambient intensity value at time step 17:50 and triggers the second online re-training cycle. Figure 47 also shows the predictions that the BbNN predictor would have made beyond 17:50 without the second online re-training. Figure 48 shows the improved predictions after the second re-training cycle. Figure 49 shows the prediction errors for the pre-trained, the second re-training cycle, and the second re-training cycles, respectively. The fitness trends for the first re-training cycle, and the second re-training cycles are shown in Figure 50 and Figure 51, respectively. The evolved BbNNs for the first re-training cycle, and the second re-training cycles are shown in Figure 52 and Figure 53, respectively.
Figure 46  Pre-trained ambient luminosity predictions and the current ambient luminosity

Figure 47  Predictions improve after first re-training cycle at 8:00
Figure 48  Predictions improve after the second re-training cycle at 17:50

Figure 49  Prediction errors for pre-trained, first re-training, and second re-training cycles
Figure 50 Average and maximum fitness trends for the first re-training cycle

Figure 51 Average and maximum fitness trends for the second re-training cycle
Figure 52  Evolved network after the first re-training cycle
Figure 53  Evolved network after the second re-training cycle
6.3.2.3 Step 3: Simulating the BbNN Controller Operation (Cloudy day)

In Step 2, evolution was used to predict the ambient light intensity values. To control and maintain the luminosity levels in the test room we need to adjust the ballast control inputs. There are 7 light fixtures in the room with one ballast per fixture. Hence we have 7 ballast control inputs to adjust. Our goal is to maintain the target illumination levels and minimize the energy consumption of the lights. Another goal is to maintain all the lights at about the same intensity levels to increase the relative lifetime of all the lamps. So our cost function for this minimization problem should account for each of these factors. It can be modeled as shown below.

\[ \text{Cost Function } CF = q_1 P(x) + q_2 G(x) + q_3 U(x) \]  

(16)

where,

- \( q_1, q_2, \text{ and } q_3 \) Weights for each of the factors in the cost function
- \( P(x) \) Estimated average power consumption per lamp
- \( G(x) \) Estimated average deviation from the target luminosity level per sensor
- \( U(x) \) Factor for load distribution across the lamps
- \( x \) BbNN controller outputs

Average power consumption per lamp can be calculated from the ballast control inputs (BbNN outputs) and the reported lamp efficacy by the lamp manufacturer as shown in the equations below.

\[ P(x) = \frac{1}{N} \sum_{i=1}^{N} P(x_i) \]  

(17)
\[ P(x_i) = \frac{L_i}{E_i} \]  
(18)

where,

- \( N \) Number of lamps
- \( L_i \) Estimated lumen output of the lamp \( i \) (in % peak RLO)
- \( E_i \) Efficacy of lamp \( i \) as reported by manufacturer (in % \( L_{\text{max}}/\text{watt} \))

As per our assumption, since all the lamps are identical, \( E_i = E \). Lumen output of the lamps can be calculated from the ballast control inputs and their linear relationship with lamp lumen outputs as dictated by the plot in Figure 38.

\[ P(x_i) = \frac{k_1(x_i) + c}{E} \]  
(19)

\[ E(\% L_{\text{max}}/\text{watt}) = \frac{E(\text{lumens/watt})}{L_{\text{max}}} \times 100 \]  
(20)

where,

- \( k_1 \) Slope of the lamp output versus ballast control input curve shown in Figure 38.
- \( c \) % RLO output at \( x_i = 0 \)

Light intensity at a point on the reference surface as measured by sensor \( S_j \) is equal to the summation of projected light intensities on that point from all the lamps plus the ambient light intensity. Thus measured light intensity by sensor \( S_j \) on surface reference point can be given by the following equation:
\[ L_{S_j} = \sum_{i=1}^{N} \frac{L_i}{d_i^2} + L_A \]  
\( \text{(21)} \)

\[ L_{S_j} = \sum_{i=1}^{N} \frac{k_1 x_i + c}{d_i^2} + L_A \]  
\( \text{(22)} \)

The estimated average deviation \( G(x) \) from the target luminosity level \( L_T \) as measured by \( M \) sensors is thus given as shown in the following equation:

\[ G(x) = \frac{1}{M} \left( \sum_{j=1}^{M} \text{abs}(L_{S_j} - L_T) \right) \]  
\( \text{(23)} \)

To ensure equivalent load distribution across all the lamps we can include a load factor \( U(x) \) in the cost function as shown below.

\[ U(x) = \max(|x_i - x_k|) \]  
\( \text{(24)} \)

This is a linear problem and can be solved easily solved by a BbNN of grid size 1 x 7. Each of the 7 outputs of the BbNN can be used to control the electronic ballasts. We will refer to this BbNN as the BbNN controller in the discussion below to avoid confusion with the BbNN predictor, described above, used to predict the ambient light intensity values. At every time-step the BbNN predictor described above can feed the predicted ambient light intensity values to the BbNN controller. The controller can evolve to find optimal values for the ballast control inputs. We can use the equation below as a fitness function for GA evolution.
Table 8 shows the genetic evolution parameters used by the BbNN controller.

Figure 54 shows the complete BbNN predictor - controller system used in this case study.

Figure 55 shows the target and actual luminosity levels (in FC) in the room with pre-trained ambient prediction values. Figure 56 shows the corresponding luminosity error. The large deviation from target luminosity observed is due to poor ambient luminosity predictions in the pre-trained case. Using the online evolution vastly improves the luminosity levels in the room with little deviations from target values. This can be seen in Figure 57 which shows the target and actual luminosity levels in the room with ambient prediction values obtained with online evolution. Figure 58 shows the corresponding luminosity error. The spike observed in the luminosity error between 19:00 and 20:00 is due to the high ambient luminosity then required. The ballast control inputs during these times are at 0V, which corresponds to 10% relative light output of the lamps. This is the minimal setting for the ballasts used. So the spike observed in the luminosity error curve is actually due to the summation of 10% lamp output and the ambient light intensity.

Figure 59 shows the power consumption (in watts) by the lights for the case of pre-trained BbNN predictor. Figure 60 shows the power consumption values with using online evolvable BbNN predictor. We can see that the average power consumption increases for the case of online evolvable BbNN predictor as compared to the pre-trained results. This is because the luminosity levels for the pre-trained case are significantly lower than the required target luminosity. The lights are dimmer as the ambient intensity predictions are much higher than the actual in the pre-trained case.
### Table 8  GA evolution parameters used for BbNN controller

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Activation Function</td>
<td>Logistic sigmoid function</td>
</tr>
<tr>
<td>Selection Strategy</td>
<td>Tournament selection</td>
</tr>
<tr>
<td>Population size</td>
<td>60</td>
</tr>
<tr>
<td>Maximum generations</td>
<td>1000</td>
</tr>
<tr>
<td>Structure Crossover probability</td>
<td>0.7</td>
</tr>
<tr>
<td>Structure Mutation probability</td>
<td>0.3</td>
</tr>
<tr>
<td>Weight Mutation probability</td>
<td>0.3</td>
</tr>
<tr>
<td>Evolution strategy</td>
<td>Ellitist evolution</td>
</tr>
</tbody>
</table>

Figure 54  BbNN predictor - controller block diagram
Figure 55  Target and measured luminosity levels as recorded by the light sensors. (pre-trained case)

Figure 56  Error between target and measured luminosities (pre-trained case)
Figure 57  Target and measured luminosity levels as recorded by the light sensors (online evolution case)

Figure 58  Error between target and measured luminosities (online evolution case)
Figure 59  Power consumption (pre-trained case)

Figure 60  Power consumption (online evolution case)
The plots also show the average power consumption for the case of not using any predictors or controllers and simply turning the lights ‘ON’ at full capacity when the target intensity levels are 0.9. Using the BbNN predictor-controller saved an average of 140W throughout the day. At an average daily rate of $0.15 per KWhr, this resulted in savings of $0.42 in energy costs per room per day. For a large skyscraper the savings quickly add up. Figure 61 shows the fitness curves and evolved network of the BbNN controller for the 4:00 time step as an example of the BbNN controller module.
Figure 61  BbNN controller at time - 4:00hrs. (a) Fitness Curves (b) Evolved BbNN
6.3.2.4 Step 4: Simulating BbNN Operation (Sunny day)

Step 2 above is repeated for the case of sunny day ambient luminosity. The results are as shown below. Figure 62 shows the pre-trained predictions of ambient luminosity values along with the actual ambient luminosity values. As before, the critic compares the predicted ambient luminosity values with the observed ambient luminosity values for each time step and on noticing a deviation of more than 0.05 triggers an online re-training cycle. The BbNN predictor performs well until 7:30. The first re-training cycle is triggered at 7:40. Due to less training data the BbNN predictor couldn’t learn the steep rise in the ambient luminosity values. As a result multiple re-training cycles are triggered for this ambient luminosity dataset. In total 8 re-training cycles were triggered during the entire course of the day. Table 9 shows all the retraining cycle times for the sunny dataset case. As can be seen from the table, the BbNN predictor performs poorly for most of the steep rise due to lack of enough training data, but continuously attempts to improve its performance through online evolution. The prediction values are within the acceptable range from 9:10 onwards until 17:10, at which point the seventh re-training cycle is triggered. The last re-training cycle (eighth re-training cycle) is triggered at 19:10. Figure 63 shows the ambient light predictions by the evolvable BbNN throughout the course of the day along with the true ambient light values. The re-training cycle points are indicated by red points on the curve.
Figure 62  Actual and pre-trained predictions of ambient light intensity

Table 9  Re-train cycle times

<table>
<thead>
<tr>
<th>Time of day</th>
<th>Re-train cycle number</th>
</tr>
</thead>
<tbody>
<tr>
<td>7:40</td>
<td>1</td>
</tr>
<tr>
<td>8:00</td>
<td>2</td>
</tr>
<tr>
<td>8:10</td>
<td>3</td>
</tr>
<tr>
<td>8:40</td>
<td>4</td>
</tr>
<tr>
<td>8:50</td>
<td>5</td>
</tr>
<tr>
<td>9:10</td>
<td>6</td>
</tr>
<tr>
<td>17:10</td>
<td>7</td>
</tr>
<tr>
<td>19:10</td>
<td>8</td>
</tr>
</tbody>
</table>
Figure 63 Actual and predicted ambient light intensity values throughout the course of the day. The retrain cycle times are shown with red dots.
The plot in Figure 64 shows the prediction errors with all the re-training steps. Each curve shows the prediction error in ambient light intensity assuming the subsequent re-training cycles are not performed. The plot in Figure 65 shows the prediction errors for the pre-trained case and the eighth re-training cycle for comparison. As can be seen, although eight re-training cycles were required during the course of the day, the predictions are within our error range of 0.05 for all the time steps except the steps that triggered a re-training cycle. Figure 66 shows the average and maximum fitness curves of the eighth re-training cycle. Figure 67 shows the evolved BbNN after 1001 generations of the eighth re-training cycle.
Figure 65 The plot shows the prediction errors for the eighth re-training cycle and the pre-trained case.

Figure 66 Fitness curves for the evolves BbNN eighth re-training cycle.
Figure 67  Evolved BbNN network after eighth re-training cycle
6.3.2.5  **Step 5: Simulating BbNN controller operation (Sunny day)**

The ambient light predictions of step 4 are fed to the BbNN controller and step 3 is repeated to simulate the BbNN controller operation. The results of the simulation are as below. Figure 68 shows the target and actual luminosity levels (in FC) in the room with pre-trained ambient prediction values. Figure 69 shows the corresponding luminosity error. The large deviation from target luminosity observed is due to poor ambient luminosity predictions in the pre-trained case. Using the online evolution vastly improves the luminosity levels in the room with little deviations from target values. This can be seen in Figure 70 which shows the target and actual luminosity levels in the room with ambient prediction values obtained with using online evolution. Figure 71 shows the corresponding luminosity error. The spike observed in the luminosity error between 19:00 and 20:00 is due to the higher ambient luminosity than required. The ballast control inputs during these times are at 0V, which corresponds to 10% relative light output of the lamps. This is the minimal setting for the ballasts used. So the spike observed in luminosity error curve is actually due to summation of 10% lamp output and the ambient light intensity. Figure 72 shows the power consumption (in watts) by the lights for the case of pre-trained BbNN predictor. Figure 73 shows the power consumption values with using the online evolvable BbNN predictor. We can see that the average power consumption decreases for the sunny case by using an evolvable predictor as would be expected. The pre-trained predictions predict less ambient light than the actual intensities for the sunny case. Due to this, the lumen outputs of the lamps are higher than required, burning more power.
Figure 68  Target and measured luminosity reading for the sunny dataset - pre-trained case

Figure 69  Luminosity error for the sunny dataset - pre-trained case
Figure 70  Target and measured luminosity readings for the sunny dataset with all eight re-train cycles

Figure 71  Luminosity error for the sunny case with all eight re-training cycles
Figure 72  Total power consumption for sunny case - pre-trained case

Figure 73  Total power consumption with sunny dataset - eight re-training cycles
The plots also show the average power consumption for the case of not using any predictors or controllers and simply turning the lights ‘ON’ at full capacity for target intensity levels of 0.9. Using the BbNN predictor-controller to regulate the luminosity in the room saved on average 310W throughout the day. At an average daily rate of $0.15 per KWhr, this resulted in savings of $0.93 in energy costs per room per day.

6.4 Summary

This chapter presented the concepts of online evolution with the BbNNs and demonstrated simulation of a case study using the evolvable BbNN platform in a dynamic environment. A training dataset that is a good representation of the actual data processed by the artificial neural networks is difficult to obtain in practice. This is especially true for applications of artificial neural networks in dynamic environments. The capability of online adaptation in a dynamically changing environment significantly improves system reliability and performance as was seen in the case study. For online evolution the hardware implementing the artificial neural networks should support intrinsic training, as in the implementation demonstrated in chapter 5. Online training capability can also be used to provide a degree of fault tolerance to external component failures. For example, in response to the failure of one of the input sensors to the network in-field, the network can be re-trained to ignore the corresponding input and ‘bypass’ the failure. This ensures reliable operation of rest of the system, or at least provides graceful degradation in system performance.
This chapter presents a performance model characterizing BbNN implementations on devices across the computing space. In particular, we compare the computational throughput of BbNNs across general purpose processors and FPGAs. We explore performance metrics for quantitative comparison. The chapter is organized as follows. The concepts for characterizing the computing device space are introduced first followed by the discussion of performance metrics. Peak throughput of BBNN implementations across different computing devices is compared and model sensitivity analysis is presented. The chapter concludes with the analysis of smart block-based neuron models described in section 5.1.3.

7.1 Computational Device Space

A computational device is a machine that processes data. The technology used to build this computational machine may vary significantly and can be electronic, mechanical, bio-computing, or any other technology that can be used to implement computations. Each set of computational instructions that process data is an individual functional configuration. The ability of the computational device to support diverse functional configurations defines its functional diversity. The Computational Device (CD) space is a broad spectrum of these computational machines and includes different computational technologies such as VLSI computing, bio-computing, and nano-
computing. Advances and innovations in these technologies continuously reshape and broaden this space. The *VLSI Processing (VP) space* is the part of the *CD space* occupied by the VLSI computing devices. This encompasses the computational devices using semiconductor fabrication processes. The *VP space* can be characterized by the device support for functional configuration diversity. At one end of the space are *soft* computing devices (also called general purpose computing devices) that can support any functional configuration depending on the sequence of programmable computing instructions executed. The hardware circuitry implementing the instructions is programmed on silicon at the time of fabrication. The instructions facilitate the functional configuration diversity after fabrication. At the other end of this space are *hard* computing devices with fixed functional configurations programmed in hardware at the time of fabrication. These devices have restrictive functional diversity. The *Reconfigurable Processing (RP) space* is a subset of *VP space* and represents the reconfigurable computing devices. Devices in the *RP space* enable diversity in functional configurations using reprogrammable hardware instructions. These hardware instructions are at lower levels of abstraction than to the functional configuration sequences in *soft* computing devices. The hardware instructions remap/reconfigure the programmable hardware units and their interconnections.

In this manuscript, the use of the term ‘*computational device*’ refers to the devices in the *VP space*. Although this is a restrictive meaning of the term with reference to our discussion above, it is convenient to use for the discussion in the rest of this chapter.
The broad range of implementation options in the VP space presents many different choices to pick to implement computations. A particular implementation choice is based on the examination of various application and resource specific constraints enforced by the chosen implementation medium. Metrics such as speedup, throughput, area, power, cost, or some combination of these guide the implementation choice. Application-specific constraints tend to be unique to a particular application or a set of applications; hence they are difficult to reasonably generalize. Resource constraints on the other hand are enforced by the implementation medium and may or may not be application-specific. Never the less, resource constraints can play an important role in design decisions for a particular application. For example, an I/O data rate for a particular implementation medium may be limited by the interconnect bus speeds. Lower bus speeds may limit the achievable I/O throughput, making the device unsuitable for an I/O-intensive application such as a network router. In another case, throughput might be limited by the input data processing speeds achievable with an implementation on a particular medium. A computationally intensive application may not be served well by this computing device. To be able to make such informed design decisions, it is imperative to characterize computing devices with respect to various computational metrics of interest.

7.2 RP Space

Continued innovations in RP space in the last two decades have blurred the traditional boundaries between soft and hard computing devices. Devices in this space
are broadly categorized as field programmable logic devices (FPLDs). These offer the flexibility of post-fabrication functional configuration diversity of soft computing devices along with the custom/semi-custom design advantages of hard computing devices. The technology offers both coarse-grained as well as fine-grained logic devices. Coarse-grained logic devices such as the field programmable object array (FPOA) from MathStar can reprogram functional object behaviors and their interconnections using different functional configuration instruction streams [209]. Typical functional objects are ALUs, MACs, and the register files (RFs). Fine-grained logic devices reconfigure gate level logic circuitry using configuration bitstreams as opposed to reprogramming circuitry at the functional objects level. Current state of the art of this technology is the field programmable gate array (FPGA). These devices contain arrays of configurable logic blocks (also called logic array blocks) interconnected via a configurable interconnection network. Each logic block is a 4-bit/6-bit LUT plus a flip-flop and can be configured to emulate a 4-input/6-input logic function or a flip-flop [210]. Configuration instruction bitstreams reconfigure these logic blocks and their interconnection network providing post-fabrication functional diversity at logic circuit level. Capacities of these devices have grown from a few thousand logic blocks per chip just over a decade ago to the order of a few hundred thousand logic blocks per chip. The regular layout architecture of these devices on silicon makes them ideally suited to embrace newer fabrication processes with smaller feature sizes relatively faster as compared to their custom ASIC counterparts and general purpose microprocessors. Increasing speeds and capacities of these devices, along with on-chip hard functional cores such as embedded processors, memory, multipliers,
and accumulators make them a very attractive low-volume, low-cost custom hardware solution from a commercial-off-the-shelf product.

Despite significant advances in FPGA technology over the past decade, there is still a performance gap between FPGAs and ASICs. Kuon et al [211] have experimentally quantified this performance gap with metrics of speed, area, and power for a set of benchmark problems. They noted the performance advantages of increasing usage of hard macros in FPGA designs especially in reducing the area gap between FPGAs and ASICs. The observed performance gap is mainly due to the resources required to support functional diversity in these devices.

With increased capacities of FPGA devices and availability of programmable hard/soft cores such as embedded processors, memories, and other peripheral cores, a powerful design paradigm has emerged called the Programmable System on Chip (PSoC). PSoCs include one or more processors, memories, and peripheral devices on a single FPGA interfaced using system and peripheral buses. The platform enables execution of computations in software code running on the processor(s) and accelerated computations in dedicated custom circuitry designed on reconfigurable FPGA fabric. The design flow for such a system is complex and involves embedded software programming as well as digital hardware design for custom logic cores used in the PSoC. This tightly-coupled programmable system on a chip has many applications in embedded systems. The system spans across traditional computing boundaries and takes advantage of soft, reconfigurable, and hard computing resources simultaneously for higher performance and
flexibility. These architectures need heterogeneous design tool flows addressing design issues such as partitioning, scheduling, simulation, debugging, verification, performance prediction, and performance analysis. Newer performance metrics that can characterize this design space are needed for optimized scheduling and partitioning of algorithms as well as future architectural projections. Figure 74 illustrates the reshaping of the VP space being caused by blurring of the boundaries between traditional computing technologies.

7.3 Performance Characterization Metrics

To achieve higher performance we need to maximize the computational throughput from a unit area of the silicon chip employed. Keeping in mind the economic aspects of computing, functional diversity also plays an important role. Soft computing devices offer diversity at the algorithmic level whereas devices in RP space provide
functional diversity at a lower level of abstraction, typically at the logic circuit level. It is
generally understood that fixed functional configurations as in custom hard computing
devices such as ASICs occupy the upper bound of performance in terms of computational
throughput, power consumption, and area required on the silicon. The performance based
on the above three metrics reduces as we move across the computing space towards soft
computing devices. The metrics introduced here for our analysis compare performance as
a function of speed, area, and power required for implementing the computational task on
a computational device. Some of the concepts used have been introduced and explained
in detail in [212, 213]. These metrics can be used to characterize the computing devices
in the VP space with respect to computational tasks. They help to maximize performance
of heterogeneous computing platforms that strive to maximize performance based on
resource and application specific constraints. These also serve as a guide for future
architectural projections.

7.3.1 Computational Device Capacity

Computational device capacity is the measure of computational work per unit
time that can be extracted from a computational device structure. Thus, if a device offers
computational capacity $D_{cap}$ then it can complete $N$ computations in time:

$$T = \frac{N}{D_{cap}}$$

(26)
The above equation raises two questions:

(i) How do we characterize computations of computing tasks?
(ii) How do we characterize tasks?

Tasks are difficult to generalize and are application specific. They may be grouped into sets with common features and used for analysis. Computations are task specific. If the application tasks are grouped using types of computations as a feature, the device computational capacities can be calculated specific to a set of computational tasks. Thus, if a computing device offers computational capacity \( D_{\text{cap\_task}} \) then it can complete \( N_{\text{task}} \) computations in time:

\[
T_{\text{task}} = \frac{N_{\text{task}}}{D_{\text{cap\_task}}} \tag{27}
\]

If the computational tasks are grouped using floating point operations as a feature then the device computational capacity gives the floating operations per second (FLOPS), a metric widely used in measuring performance of computing systems.

\[
D_{\text{cap\_FLOPS}} = \frac{N_{\text{FLOP}}}{T_{\text{task}} \text{(sec)}} \tag{28}
\]

If the grouped tasks represent neuromorphic circuits, the computation of interest is synaptic connections processed. Thus, the computational capacity will indicate synaptic connections processed per second or CPS, another widely used metric used for measuring performance of neuromorphic circuits.
To calculate raw throughput of tasks on computational devices Dehon [212] suggested using a gate evaluation metric. The idea is to count the number of gate evaluations in a minimal logic circuit required to implement the computational task. Thus, if a device offers capacity $D_{cap\_ge}$ to an application task requiring $N_{ge}$ gate evaluations, the task can be completed in time:

$$T_{task} = \frac{N_{ge}}{D_{cap\_ge}}$$  \hspace{1cm} (30)
fabrication process using larger feature size. To make our calculations independent of this parameter, we normalize area in units of \( \lambda \), half the minimum feature size of the fabrication process. Thus the metric for computational density is measured in units of operations/ \( \lambda^2 \) s.

\[
F_{\text{density}} = \frac{N_{\text{ops}}}{T_{\text{task}} \times A(\lambda^2)}
\]  

(32)

Thus, in the case of general purpose computing devices such as processors, the area is the silicon area used for the implementation of instructions in the computational task. This includes the area occupied by the datapath elements, interconnections, and internal memory. In case of an ASIC, it is the chip area occupied by the logic gates and interconnections of the logic circuit used for implementation of the computational task. For an FPGA, it is the chip area occupied by the total number of logic blocks and the routing circuits used by the computational task.

### 7.3.3 Power Efficiency

Delay and area have been addressed by the device capacity and density metrics, but another important aspect of performance evaluation is power consumption. This is an important factor in HPC systems, but is critical in many high performance embedded computing systems. Dynamic power dissipation is directly related to the yielded device capacity via the cycle frequency. The higher the frequency, the higher the dynamic power
dissipation will be. Thus, it is interesting to note the device capacity per unit watt (or milli-watt) as shown below.

\[ D_{\text{cap-per-mW}} = \frac{D_{\text{cap}}}{P_d (mW)} \]  \hspace{1cm} (33)

7.3.4 Discussion

The above metrics are indicators of computational capacity and density of a computational device from a logic-centric view. They largely ignore the impact of the associated interconnect and routing costs. For computational structures implementing custom dataflow architectures the interconnect costs can substantially grow with increasing problem sizes. For example, consider a feedforward fully connected neural network implemented as a directed acyclic graph with neural processing elements as nodes on an ASIC or an FPGA. Growth in network size exponentially increases the number of synaptic interconnections, equally increasing the associated interconnect and routing costs. These effects are more pronounced with multi-dimensional networks. This can significantly affect the functional density estimates, and more so in RC implementations where logic circuits are routed via pre-fabricated multiple-length programmable routing interconnects. But these costs are difficult to generalize and quantify and they vary depending on the computing device technology used for implementation. For the purposes of our analysis here we will largely ignore these costs. In case of a 2-dimensional BbNN implementation, the topological restrictions in architecture limit the interconnect growth to linear for every additional row or column.
added to the existing grid. Hence, the effects of ignoring the interconnect costs will be
tolerable for this particular neural network topology. But the comparison with other fully
connected networks such as multilayer perceptrons (MLP) will skew our analysis as the
device capacity may not increase linearly with increases in the size of the network. Also,
ignored in the above analysis are the data I/O rates and the memory hierarchy effects.
These will impact the actual computational throughput and device capacity in practice.
Future work should address these issues.

7.4 BbNN Performance Analysis

Our goal here is to analyze and characterize BbNN implementations on different
computing structures ranging from general purpose processors to custom computing
devices. We will characterize and compare the computational capacities and densities
provided by various computational devices to BbNN architecture in units of connections
processed per second as shown in the equations above. For a BbNN, the maximum
number of connections that can be processed per block computation is 6 as in the case of
a 2-input / 2-output neuron block. Equation below shows the neuron block computation
in the case of a 2/2 block.

\[
y_k = g \left( 1b_k + \sum_{j=1}^2 w_{jk}x_j \right), \quad k = 1, 2. \tag{34}
\]
/* 16-bit fixed point multiplication. Done twice, once for each input and synaptic weight */

mullw   r_y1, r_x, r_w
szwi    r_yi, r_yi, 8
andi     r_yi, r_yi, 0xFFFF

/* Adjusting the bias for 8.8 fixed point format and the two additions */

slwi    r_D, r_D, 8
add     r_y', r_y1, r_y2
add     r_y, r_y', r_D

Figure 75  RISC assembly code for a single neuron processing

where,

\( y_k \)  \( k^{th} \) output signal of the neuron block
\( x_j \)  \( j^{th} \) input signal of the neuron block
\( w_{jk} \)  Synaptic weight connection between \( j^{th} \) input node and \( k^{th} \) output node
\( b_k \)  Bias at \( k^{th} \) output node
\( J, K \)  Number of input and output nodes respectively of a neuron block.
\( G(\bullet) \)  Linear / nonlinear Activation function

### 7.4.1 Performance Characterization on Processors

To calculate the capacity provided by a processor we consider the code shown in Figure 75. It is RISC assembly code to compute a single output in a neuron block. The code omits all the load-store instructions and just shows the main computational part. In the case of a 2/2 neuron block there are two outputs which will require the instructions
shown to compute a single output to be executed twice. Peak computational capacity provided by the processors can be calculated as shown below.

\[
D_{cap} = \frac{N_c}{m_{inst}} \times \frac{Instructions}{Issue slots} \times \frac{Issue slots}{Clock cycle} \times \frac{Clock cycles}{sec}
\]  

(35)

where,

\[
N_c \quad \text{Number of connections per block}
\]

\[
m_{inst} \quad \text{Number of instructions per block computation}
\]

Thus, assuming a CPI of 1.0, a scalar processor running at 400 MHz, such as PPC405 provides a peak computational capacity of 133 MCPS. Table 10 surveys some commercial RISC processors using the metrics described above for BbNN implementation.

It should be noted that some of these processors do support SIMD extensions and hence instructions such as multiply and accumulate. This will reduce the number of instructions required for neuron block processing by 2 as a result, skewing our capacity estimates by a factor of 1.125. We have not counted the required load instructions to bring the data in to the internal registers and the store instructions to store the data back in memory. Including these will change the results significantly. For the BbNN block computation, we need 10 load instructions to bring in the inputs, weights, and biases from memory and require 2 store instructions to store the computed outputs. This adds 12 instructions to the code shown in Figure 75, reducing our capacity estimates by a factor of 0.6.
Table 10  Peak Computational Capacity (in MCPS) and density (in CP$\lambda^2$S) of RISC processors for BbNN block computation

<table>
<thead>
<tr>
<th>Processor</th>
<th>Organization</th>
<th>Area (mm$^2$)</th>
<th>$\lambda$ (nm)</th>
<th>Area ($\lambda^2$)</th>
<th>Cycle Freq</th>
<th>$P_d$</th>
<th>$D_{cap}$ (MCPS)</th>
<th>$D_{cap}$ per mW</th>
<th>$F_d$ (CP$\lambda^2$S)</th>
</tr>
</thead>
<tbody>
<tr>
<td>MIPS 24Kc</td>
<td>1 x 32</td>
<td>10.7</td>
<td>130 nm</td>
<td>633 M</td>
<td>261 MHz</td>
<td>363 mW</td>
<td>87</td>
<td>0.24</td>
<td>0.137</td>
</tr>
<tr>
<td>MIPS 4KE</td>
<td>1 x 32</td>
<td>1.7*</td>
<td>130 nm</td>
<td>101 M</td>
<td>233 MHz</td>
<td>58 mW</td>
<td>78</td>
<td>1.33</td>
<td>0.772</td>
</tr>
<tr>
<td>ARM 1026EJ-S</td>
<td>1 x 32</td>
<td>4.2*</td>
<td>130 nm</td>
<td>248 M</td>
<td>266 MHz</td>
<td>279 mW</td>
<td>89</td>
<td>0.32</td>
<td>0.357</td>
</tr>
<tr>
<td>ARM 11MP</td>
<td>1 x 32</td>
<td>1.46*</td>
<td>90 nm</td>
<td>180 M</td>
<td>320 MHz</td>
<td>74 mW</td>
<td>107</td>
<td>1.45</td>
<td>0.591</td>
</tr>
<tr>
<td>ARM 720T</td>
<td>1 x 32</td>
<td>2.4*</td>
<td>130 nm</td>
<td>142 M</td>
<td>100 MHz</td>
<td>20 mW</td>
<td>33</td>
<td>1.67</td>
<td>0.235</td>
</tr>
<tr>
<td>PPC 405</td>
<td>1 x 32</td>
<td>2*</td>
<td>90 nm</td>
<td>246 M</td>
<td>400 MHz</td>
<td>76 mW</td>
<td>133</td>
<td>1.75</td>
<td>0.54</td>
</tr>
<tr>
<td>PPC 440</td>
<td>1 x 32</td>
<td>9.8</td>
<td>130 nm</td>
<td>580 M</td>
<td>533 MHz</td>
<td>800 mW</td>
<td>178</td>
<td>0.22</td>
<td>0.306</td>
</tr>
<tr>
<td>PPC 750FX</td>
<td>2 x 32</td>
<td>40</td>
<td>200 nm</td>
<td>1 G</td>
<td>533 MHz</td>
<td>6.75 W</td>
<td>355</td>
<td>0.05</td>
<td>0.355</td>
</tr>
<tr>
<td>PPC 970FX</td>
<td>2 x 64</td>
<td>66.2</td>
<td>90 nm</td>
<td>8.1 G</td>
<td>1 GHz</td>
<td>11 W</td>
<td>667</td>
<td>0.06</td>
<td>0.082</td>
</tr>
<tr>
<td>PA 8700+</td>
<td>4 x 64</td>
<td>304</td>
<td>180 nm</td>
<td>9.4 G</td>
<td>750 MHz</td>
<td>7.1 W</td>
<td>1000</td>
<td>0.14</td>
<td>0.107</td>
</tr>
</tbody>
</table>

* Synthesizable core area
We have also assumed in our analysis an instruction issue rate of one instruction per pipeline per clock cycle. This is usually not achievable with practical work loads due to data dependencies between instructions, and overheads of memory hierarchies, cache miss penalties and page faults.

The processor die areas marked with an (*) are synthesizable core areas. These are synthesizable processor cores which can be used in custom System-on-Chip (SoC) architectures. Thus they do not include area occupied by the I/O pads.

7.4.2 Performance Characterization on FPGAs

Figure 76 and Figure 77 show two different pipelined implementations for computing a single output of the neuron block. The implementation in Figure 76 uses a multiplier accumulator circuit to compute the sum of products and the one in Figure 77 uses two parallel multipliers. A pipelined multiplier accumulator circuit can produce an output every third clock cycle and uses only one multiplier block as shown. Using two parallel multipliers can speed up the throughput to one output every clock cycle. Most current generation FPGAs have built-in configurable hard multiplier cores that can be used to implement the required multipliers instead of using logic blocks. We will consider both the built-in hard core multipliers and LUT based multipliers in our analysis.
Figure 76  Pipelined multiplier accumulator circuit for neural processing

Figure 77  Pipelined parallel multiplier circuit for neural processing
Implementation of the circuit in Figure 76 on a Xilinx Virtex-II Pro XC2VP30-7 can be clocked at 264 MHz. Since both the neurons can be implemented in parallel, 6 connections will be processed every 3 clock cycles. The computational capacity can be calculated as shown below.

\[
D_{\text{cap}} = \frac{N_c}{m_{\text{cycle}} \times t_{\text{cycle}}} = \frac{6}{3 \times 3.79 \text{ns}} = 528 \text{MCPs}
\]  

(36)

Computational density provided by this FPGA can be calculated as shown below.

\[
F_d = \frac{N_c}{m_{\text{cycle}} \times t_{\text{cycle}} \times A_{\text{CLB}} (λ^2) \times N_{\text{CLB}}}
\]
\[
= \frac{6}{3 \times 3.79 \text{ns} \times 1.6M^* \times 79} = 4.1CPλ^2s
\]  

(37)

*NOTE:*

1. The CLB/slice areas used in the above equation and other calculations involving Xilinx FPGAs in this chapter are estimates derived from the FPGA package sizes. These are NOT ACCURATE. Die areas for FPGAs are not readily provided by Xilinx and is regarded as proprietary information by the company.

2. These estimates have been derived by estimating the die area from the published package sizes and dividing by number of published CLBs per device. Assuming that our die area estimates are correct, the CLB area computed will be higher than the actual area as we are not discounting for area occupied by others such as IOBs, BRAMs, multipliers, transceivers, and routing.

3. Ideally, with known CLB areas and the hard multiplier/DSP48e areas, we would add up the area occupied by all the CLBs, the hard multipliers/DSP48es, and the area required for routing interconnects to estimate the total area of the circuit. But, our CLB area estimates have been derived from die area estimates divided by the total number of CLBs. We are not discounting the area occupied by the hard multipliers/DSP48es, the IOBs, and the interconnects. Hence the estimated area per CLB indirectly is accounting for routing and hard multipliers. Thus we will ignore the area occupied by multipliers and routing resources in our estimates.

4. Note, that the computational density values thus computed are only estimates.
Table 11 shows the computed capacity and density values for BbNNs provided by some selected FPGAs. It should be noted that the area, and speed values are obtained using Xilinx synthesis, and place and route tools (ISE v7.1) [214].
Table 11  BbNN Computational Density on FPGAs

<table>
<thead>
<tr>
<th>FPGA</th>
<th>2/2 Neuron Block</th>
<th>CLK (MHz)</th>
<th>No. CLBs</th>
<th>$A_{CLB}$ (ML$^2$)</th>
<th>Area $A$ (ML$^2$)</th>
<th>$P_d$ (mW)</th>
<th>$D_{cap}$ (MCPS)</th>
<th>$D_{cap}$ per $P_d$</th>
<th>$F_d$ (CPX$^2$S)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Xilinx VirtexE XCV3200E-8 (λ=180nm) [131]</td>
<td>AL</td>
<td>156</td>
<td>264</td>
<td>1.25M*</td>
<td>330</td>
<td>589</td>
<td>312</td>
<td>1.33</td>
<td>0.95</td>
</tr>
<tr>
<td></td>
<td>ML</td>
<td>153</td>
<td>316</td>
<td></td>
<td>395</td>
<td>693</td>
<td>918</td>
<td>0.53</td>
<td>2.33</td>
</tr>
<tr>
<td>Xilinx Virtex-II Pro XC2VP100-7 (λ=130nm) [189]</td>
<td>AL</td>
<td>264</td>
<td>79</td>
<td>1.6M**</td>
<td>129</td>
<td>364</td>
<td>528</td>
<td>1.45</td>
<td>4.1</td>
</tr>
<tr>
<td></td>
<td>ML</td>
<td>201</td>
<td>193</td>
<td></td>
<td>315</td>
<td>475</td>
<td>403</td>
<td>0.847</td>
<td>1.28</td>
</tr>
<tr>
<td></td>
<td>MH</td>
<td>304</td>
<td>41</td>
<td></td>
<td>67</td>
<td>271</td>
<td>1821</td>
<td>6.72</td>
<td>27.25</td>
</tr>
<tr>
<td></td>
<td>ML</td>
<td>235</td>
<td>158</td>
<td></td>
<td>258</td>
<td>554</td>
<td>1408</td>
<td>2.54</td>
<td>5.47</td>
</tr>
<tr>
<td>Xilinx Virtex-4 XC4VLX200-11 (λ=90nm) [210]</td>
<td>AL</td>
<td>238</td>
<td>32</td>
<td>1.68M**</td>
<td>54</td>
<td>109</td>
<td>476</td>
<td>4.36</td>
<td>8.85</td>
</tr>
<tr>
<td></td>
<td>MH</td>
<td>219</td>
<td>57</td>
<td></td>
<td>96</td>
<td>111</td>
<td>1316</td>
<td>11.9</td>
<td>13.74</td>
</tr>
<tr>
<td></td>
<td>ML</td>
<td>221</td>
<td>153</td>
<td></td>
<td>257</td>
<td>210</td>
<td>1328</td>
<td>6.31</td>
<td>5.17</td>
</tr>
<tr>
<td>Xilinx Spartan-3 XC3S5000-5 (λ=90nm) [215]</td>
<td>AL</td>
<td>143</td>
<td>66</td>
<td>1.83M**</td>
<td>119</td>
<td>58</td>
<td>286</td>
<td>4.93</td>
<td>2.41</td>
</tr>
<tr>
<td></td>
<td>ML</td>
<td>128</td>
<td>195</td>
<td></td>
<td>351</td>
<td>114</td>
<td>256</td>
<td>2.25</td>
<td>0.73</td>
</tr>
<tr>
<td></td>
<td>MH</td>
<td>198</td>
<td>41</td>
<td></td>
<td>74</td>
<td>97</td>
<td>1186</td>
<td>12.28</td>
<td>16.07</td>
</tr>
<tr>
<td></td>
<td>ML</td>
<td>173</td>
<td>158</td>
<td></td>
<td>285</td>
<td>147</td>
<td>1035</td>
<td>7.056</td>
<td>3.64</td>
</tr>
<tr>
<td>SFRA (λ= 180nm) [216, 217]</td>
<td>AL</td>
<td>300</td>
<td>264†</td>
<td>5M</td>
<td>1320</td>
<td>-</td>
<td>600</td>
<td>-</td>
<td>0.45</td>
</tr>
<tr>
<td></td>
<td>ML</td>
<td>300</td>
<td>316†</td>
<td></td>
<td>1580</td>
<td>-</td>
<td>1800</td>
<td>-</td>
<td>1.14</td>
</tr>
</tbody>
</table>

* As reported in reference [218]
** Estimated from reported package area. See Note in section 7.4.2 above.
† Xilinx ISE Post mapping result. SFRA tool flow uses Xilinx tools until mapping and use a custom developed place and route tool after that [216, 217].
†† AH – Sum of product pipeline built using multiplier – accumulator with built-in multiplier
AL – Sum of product pipeline built using multiplier – accumulator with LUT-based multiplier
MH – Sum of product pipeline built using two parallel multipliers with built-in multiplier
ML – Sum of product pipeline built using two parallel multipliers with LUT-based multiplier
7.4.3 Results and Discussion

Sections 7.4.1 and 7.4.2 survey the computational capacities and densities provided by some commercial RISC processors and Xilinx FPGAs for 16-bit BbNN block computations. The results for capacity and density are plotted for direct comparison in each of the following cases; (i) Processor and FPGA-hard MAC (see Figure 78), (ii) Processor and FPGA-LUT MAC (see Figure 79), (iii) Processor and FPGA-hard Multiplier (see Figure 80), and (iv) Processor and FPGA-LUT Multiplier (see Figure 81). The results for computational capacity per mW are plotted in Figure 82, Figure 83, Figure 84, and Figure 85.
Figure 78  Comparing processors and FPGAs (Hard MAC) (a) Capacity (b) Density
Figure 79 Comparing processors and FPGAs (LUT MAC) (a) Capacity (b) Density
Figure 80  Comparing processors and FPGAs (Hard Multipliers) (a) Capacity (b) Density
Figure 81  Comparing processors and FPGAs (LUT Multipliers) (a) Capacity (b) Density
Figure 82  Comparing power efficiencies of processors and FPGAs (Hard MAC)

Figure 83  Comparing power efficiencies of processors and FPGAs (LUT MAC)
Figure 84  Comparing power efficiencies of processors and FPGAs (Hard Multiplier)

Figure 85  Comparing power efficiencies of processors and FPGAs (LUT Multiplier)
As observed from the results there is a gain of about 3X to 10X in computational capacities between scalar processors and FPGAs. FPGAs offer comparable computational capacities as superscalar processors with gains of about 0.5X – 2X. Processors with faster clock rates and higher instruction issue rates than the PA8700+ could offer even higher computational capacities. But, the FPGA computational densities are over two magnitudes higher than the superscalar processors, underscoring the area efficiency obtained from FPGAs. The density gains of FPGAs are 2X to 34X as compared to scalar processors. Comparing power efficiencies, we find that new FPGAs from Xilinx (Virtex 4 and Spartan 3) are more power efficient than the older FPGAs (Virtex-II Pro and VirtexE). Comparing the FPGA and processor power efficiencies, we find 2X to 6X gains with FPGA designs using the hard multiplier blocks for the MAC and parallel multiplier implementations. The power gains are not significant for FPGA LUT-based designs using both the older and newer FPGAs. Although the superscalar processors had comparable computational capacities with FPGAs, they consume about 2X to 6X more power than the FPGAs.

In general, computational densities in FPGAs are 10X higher as compared to processors [212, 213]. In our analysis, it is important to realize that we are comparing computational gains for a particular computational task, BbNN computations. Inherent parallelism observed in the BbNN block computations cannot be exploited by sequential execution on processors. On the other hand, custom implementations in FPGAs can fully exploit this parallelism. This is one of biggest factors in the observed computational
capacity gains. The newer FPGAs provide much higher capacity with lower power consumption as compared to processors.

It should be noted that the computational capacities calculated for the processors are ideal capacity values rarely achieved in practice. We are assuming instruction issue rates of 100% in our calculations. The issue rates for common workloads are much lower than the theoretical peak rates. The instruction throughput in processors depends on factors such as the pipeline implementation, data dependencies, branch prediction logic, out of order execution, and cache penalties. Also, multiple BbNN blocks can execute in parallel on FPGAs, linearly increasing the computational capacity with increasing network sizes (limited by the number of blocks that the FPGA device can hold), unlike in processors. This is shown in Figure 86.

Figure 86 Computational capacities of FPGAs and processors as a function of network size
7.4.4 Performance of SBbNs

The smart block-based neuron (SBbN) design presented in 5 is the one used in our implementation of intrinsically evolvable BbNNs. Section 5.4 presents the performance results for the design. The design can achieve 147MCPS on Virtex-II Pro at frequency of 245MHz. Why is the computational capacity low compared to the results presented in section 7.4.2? The reasoning for this is as below.

♦ SBbN design is larger than the basic neuron design considered in section 7.4.2. The design is larger to accommodate for the extra logic required for the dynamic configuration adaptability, activation function lookup table, register storage for weights and biases, and the extra multipliers required to accommodate for 1-input / 3-outputs neuron block configuration.

♦ Use of a multiply-accumulator unit instead of parallel multipliers also affects the throughput. The choice to sacrifice the throughput was made to enable the FPGA to hold larger networks. Using parallel multipliers would require twice the number of hard multipliers per neuron block as compared to the MAC based approach. Thus, the fixed number of multipliers available per FPGA quickly becomes a bottleneck for network scalability.

♦ P/T net-based dataflow implementation adopted for reliable asynchronous intercommunication between neuron blocks has one side effect. It enforces serial execution of the neuron block computation. Although, each of outputs within the neuron block compute in parallel. New inputs cannot be applied until the previous inputs are consumed and corresponding outputs generated by the neuron block. Also, the cycle to lookup the activation function value in the lookup table adds to
the computation time. In total requiring 10 clock cycles to produce a result at the output. At 245 MHz with a maximum of 6 connections processed in a given block computation the throughput is 147MCPS per neuron block. The computational density with the occupied area of 171 CLBs on Virtex-II Pro (XC2VP30) FPGA is 0.54 connections per \( \lambda^2 \)s.

As shown in Figure 86, it should be noted that the computational capacity increases linearly with increase in the network size, unlike the processors. Thus, for an \( m \times n \) network size the peak computational capacity is 147\( n \) MCPS.

### 7.5 Model Sensitivity to Parametric Variations

Analysis presented above is based on certain parametric value estimations such as the CLB area which has been estimated using the published package sizes of FPGA devices. It is important to analyze the sensitivity of our model to variations in model parameters. The analysis is presented below.

Let \( M_c \) be the ideal value of the function computed using model \( M \) and \( M_d \) be the observed value due to variation in parameter \( p \) from ideal to the observed value. If the deviation factor is \( d_p \) then,

\[
M_d = \frac{M_c}{d_p}
\]  

(38)
Thus, error in model computation is

\[ e = |M_c - M_d| = M_c \left( 1 - \frac{1}{d_p} \right) \]  

(39)

The percent deviation from the ideal value can be computed as shown below.

\[ E = \left( 1 - \frac{1}{d_p} \right) \times 100 \]  

(40)

For example, deviation in peak computational capacity of a processor due to variation in observed CPI \( (CPI_{\text{actual}}) \) from assumed ideal value \( (CPI_{\text{estimated}}) \) can be calculated as shown below.

\[ d_{\text{cpi}} = \frac{CPI_{\text{actual}}}{CPI_{\text{estimated}}} \]  

(41)

\[ E = \left( 1 - \frac{1}{d_{\text{cpi}}} \right) \times 100 \]  

(42)

Deviation in observed computational density in an FPGA to variation in CLB area can be computed as shown below.

\[ F_{d_{\text{actual}}} = \frac{F_{d_{\text{estimated}}}}{d_A} \]  

(43)

where,
Figure 87 shows a plot of the deviation $E$ in observed computational density versus the deviation factor $d_A$ of the CLB area. Consider the neuron implementation of Figure 77 in Virtex-II Pro FPGA using hard multipliers. The estimated CLB area is $1.6 \text{ M} \lambda^2$. If the actual CLB area is $1.8 \text{ M} \lambda^2$ the deviation in computation density will be by $11.11\%$ from the original value of $27.25 \text{ CP} \lambda^2$s. This gives the new density value as $24.22 \text{ CP} \lambda^2$s.

\[
d_A = \frac{A_{\text{actual}}}{A_{\text{estimated}}}
\]
7.6 Summary

A performance characterization model for BbNNs was presented in this chapter. It enables performance comparison across different computational devices based on the metrics of computational capacity and density. Computational capacity is the computational work that can be extracted from a computational device and can be modeled as number of operations per second. Computational density is a space-time metric giving the computational work extracted per unit time and area from a computational device. Computational density per watt gives the estimate of power consumption for the execution of the computation. These metrics were used to analyze the BbNN computational capacity on the RISC processors and the FPGAs. The results show FPGAs provide on an average 10X higher computational capacities than the scalar RISC processors for a single BbNN block. The computational densities of FPGAs are 2X to 34X higher than the processors. The computational capacity of FPGAs linearly increases with the increasing network sizes, unlike processors. The newer FPGAs from Xilinx (the Virtex 4 and the Spartan 3) are more power efficient than the older FPGAs. Comparing their power efficiencies with processors, we observe 2X to 6X higher computational capacities per mW provided by FPGAs. Although the superscalar processors had comparable computational capacities with FPGAs for a single neuron block computation, FPGAs consume about 2X to 6X less power and provide 2X to 34X gains in computational densities. Model’s sensitivity to variations in its parameters has also been analyzed and presented. The deviation in computed values is found to vary linearly to parametric variations.
8 SUMMARY AND CONCLUSIONS

Following list summarizes the major points, concepts, and accomplishments of this work.

♦ **Evolvable hardware systems (EHW)** use reconfigurable computing platforms such as FPGAs to evolve hardware circuitry under the control of evolutionary algorithms. The configuration bitstream is encoded as a genotype and evolved over multiple generations to find a network that meets the target fitness. Fitness is determined using an objective function that includes parameters such as correctness of circuit functionality, area, speed, and power.

♦ **Intrinsic and extrinsic hardware evolutions** are classifications of evolvable hardware systems based on the role of reconfigurable computing (RC) hardware in evolution. Intrinsic systems include the hardware in the evolution loop to measure the fitness of the genotype. Hence they perform online evolution. Extrinsic systems use a software model of the hardware and perform offline evolution using computer simulations.

♦ **Functional-level and gate-level evolution** describe the abstraction level at which the evolution is performed in an evolvable hardware system. Evolving FPGA configuration bitstream encoded as genotype in an evolutionary algorithm is circuit-level or gate-level evolution. Evolving the interconnections and internal
parameters of higher level functional modules such as multipliers, accumulators, and trigonometric functions is functional-level evolution.

- **Block-based neural networks (BbNN)** are grid-based networks of neuron blocks, the basic processing elements of the network. The outputs of the network are a unique function of the inputs, the network structure, and the synaptic weights of the neuron blocks. Training of these networks is a multi-parametric optimization problem, simultaneously evolving structure and synaptic weights of the neuron blocks. Typically genetic algorithms are used to train these networks to model input–output relationships and learn characteristic features in training datasets.

- **Offline and online training** are artificial neural network (ANN) learning schemes. In an offline learning the neural network is trained using a batch of training data offline. In an online learning scheme the neural network is trained on real data in field. Online training in neural networks improves network generalization, and enhances system reliability. The in-field re-training capability enhances ANN system performance by adapting to variations in input data.

- **Intrinsically evolvable BbNN hardware** design is presented. The design supports on-chip, online training of BbNNs on FPGAs, presenting a compact, and evolvable neural network chip for applications in dynamic environments. The BbNN on-chip training is a functional-level intrinsic evolution with neuron blocks as the functional modules.

- **Design Scalability** in space (across multiple FPGAs) and in time (using same FPGA in time multiplexed manner) is enabled by reliable, asynchronous dataflow architecture implemented in the design. Asynchronous synaptic links enable
design scalability by ensuring reliable communication between neuron blocks spread in time or space irrespective of the type of communication channels used to transfer data between neuron blocks. This makes the design portable and scalable across a heterogeneous mixture of reconfigurable computing resources.

♦ *Online training* algorithm for BbNN is presented along with a case study – Adaptive neural luminosity controller. The results of the study demonstrate the benefits of online training and showcase the applicability of the designed platform to applications in dynamic environments.

♦ *Performance characterization* model of BbNN RC implementations is presented. The model characterizes BbNN implementations across the general purpose computing devices and the FPGAs using performance metrics such as the computational device capacity, the computational density, and the power efficiency. Computational device capacity is the measure of computational work per unit time that can be extracted from a computational device structure. For BbNNs it is the number of synaptic connections processed per second (CPS) by the computing device. Computational density is a space-time metric and can be defined as the computational capacity provided by the computing device per unit silicon area. The results show FPGAs provide on an average 10X higher computational capacities than the scalar RISC processors for a single BbNN block. The computational densities of FPGAs are 2X to 34X higher than the processors. The computational capacity of FPGAs linearly increases with the increasing network sizes, unlike processors. The newer FPGAs from Xilinx (the Virtex 4 and the Spartan 3) are more power efficient than the older FPGAs.
Comparing their power efficiencies with processors, we observe 2X to 6X higher computational capacities per mW provided by FPGAs. Although the superscalar processors had comparable computational capacities with FPGAs for a single neuron block computation, FPGAs consume about 2X to 6X less power and provide 2X to 34X gains in computational densities.

This work provides a platform for further research on BbNNs in three directions – implementations, algorithms, and applications. They are discussed below.

1. Implementations

This work provides a platform for further research in custom, scalable, intrinsically evolvable ANN implementations. The designed implementation enables BbNN scalability across heterogeneous RC resources, but the designing and implementing working prototypes should be undertaken as future extensions to the project. The developed approach could also be ported to other ANN architectures such as multilayer perceptrons and cellular neural networks. The genetic algorithm (GA) operators in the implementation currently execute in software running on the PPC 405 embedded core on the FPGA die. This approach was chosen for the current implementation to maximally utilize the reconfigurable logic space to fit larger networks. But with increasing capacities of FPGAs, genetic operators can be hardware accelerated.
2. Algorithms

Active research should be pursued in exploring time bounded training algorithms for BbNNs. Online learning ability significantly expands the application space of BbNNs to dynamic environments. But many applications may require real-time performance. The training algorithms used for BbNNs are currently not time bounded. Theoretical investigations should be undertaken to establish confidence levels in training results obtained within bounded times. Another important area of research in algorithms for BbNNs is to explore reinforcement learning techniques for BbNNs. This enables BbNNs to learn from interactions with the surrounding environment. A difficult issue to solve in online training of artificial neural networks is measure fitness of a network when target outputs are unknown. Reinforcement learning algorithms have a notion of reward from environment for actions of the agent. The agent has a goal to discover the state - action policies that maximize this reward over time.

3. Applications

The biggest selling point of any technology is in its applications. This dissertation provides a glimpse into the realm of possible applications of BbNNs in dynamic environments. Applications such as speech recognition, handwriting recognition, medical diagnostics and monitoring, and navigational systems are all possible contenders in the application set. Further research efforts are required to investigate the feasibility of using BbNNs for these applications.
The performance model presented is currently logic centric. It should be extended to include routing and interconnect costs. Although the model is applied to BbNNs, it can apply to other computational tasks. Our analysis compares performance on FPGAs and processors. This should be extended to include other computing devices such as analog and digital custom ASICs.
REFERENCES
REFERENCES


[105] E. Farquhar and P. Hasler, "A bio-physically inspired silicon neuron," *Circuits and Systems I: Regular Papers, IEEE Transactions on [see also Circuits and*


[131] Xilinx, "Virtex-E 1.8V Complete Data Sheet (All four Modules)," Product Specification, DS022 (v2.3), July 17, 2002


[201] "Wind River : VxWorks (www.windriver.com)."

[202] "Timesys Linux (http://www.timesys.com/)."

[203] "Montavista Linux (http://www.mvista.com/)."


[206] "*Lutron Electronic Co, "Fluorescent Dimming Ballasts","* Datasheet, TVE (1) 02.19.04,


[208] "*Lutron Electronic Co. "Fluorescent dimming systems technical guide","* 


[214] Xilinx, "*ISE Software Manuals and help,*" 2006


APPENDIX

Acronyms used in the manuscript

ALU see Arithmetic Logic Unit

ANN see Artificial Neural Networks

ANNA see Analog Neural Network Arithmetic

API see Application Programming Interface

ASIC see Application Specific Integrated Circuits

BbNN see Block-based Neural Networks

BCSR see Block Control and Status Register

BRAM see Block Random Access Memory

CA see Cellular Automata

CBM see CAMBrain Machine

CD see Computational Device

CLB see Configurable Logic Block

CMOS see Complementary Metal Oxide Semiconductor

CoDi see Collect and Distribute

CORDIC see Coordinate Rotation Digital Computer

CPI see Clock cycles per instruction

CPS see Connections per second

CSD see Canonic Signed Digit

DA see Distributed Arithmetic
DSP see Digital Signal Processor
EDK see Embedded Development Kit
EHW see Evolvable Hardware
ETANN see Electronically Trainable Analog Neural Network
FC see Foot Candles
FEA see Fast Evolutionary Algorithm
FIFO see First In First Out
FLOPS see Floating Operations per Second
FPAA see Field Programmable Analog Array
FPGA see Field Programmable Gate Arrays
FPLD see Field Programmable Logic Devices
FPOA see Field Programmable Object Array
FPNA see Field Programmable Neural Array
FPTA see Field Programmable Transistor Array
FPTA2 see Second generation Field Programmable Transistor Array
GA see Genetic Algorithm
GDD see Generalized Disjunction Decomposition
GRD see Genetic Reconfiguration of DSPs
HPC see High Performance Computing
HPEC see High Performance Embedded Computing
HPRE see High Performance Reconfigurable Computing
I/O see Input / Output
ISE see Integrated Systems Environment
**KWhr** see Kilo Watt Hour

**LMS** see Least Mean Square

**LUT** see Lookup Table

**LVQ** see Linear Vector Quantization

**MAC** see Multiplier and Accumulator

**MCPS** see Million Connections per Second

**MDP** see Markov Decision Process

**MLP** see Multilayer Perceptron

**NNP** see Neural Network Processor

**OPB** see On-Chip Peripheral Bus

**P/T net** see Petri net or Place/transition net

**PCB** see Printed Circuit Board

**PCI** see Peripheral Component Interconnect

**PIG** see Processing Integrated Grid

**PLA** see Programmable Logic Array

**PLB** see Processor Local Bus

**PLD** see Programmable Logic Devices

**PNN** see Probabilistic Neural Network

**PPC** see PowerPC

**PSoC** see Programmable System on a Chip

**RAID** see Redundant Array of Inexpensive Disks

**RAM** see Random Access Memory

**RC** see Reconfigurable Computing
RISC see Reduced Instruction Set Computer
RP see Reconfigurable Processing
RWC see Real World Computing
SBbN see Smart Block-based Neuron
SDRAM see Synchronous Dynamic Random Access Memory
SIMD see Single Instruction Multiple Data
SoC see System on a Chip
SRAM see Static Random Access Memory
TDNN see Time-delay Neural Network
UART see Universal Asynchronous Receiver Transmitter
VP see VLSI Processing
XUP see Xilinx University Program
Saumil G. Merchant, a loving husband and son, was born 20\textsuperscript{th} September, 1976 to Kokila and Girish Merchant. He grew up in Mumbai, India and attended New Era School, a premier institution instilling cultural values along with curricular education among its students. In 1992 he graduated with distinction in S.S.C. (Secondary School Certificate) examination and joined Jai Hind College of Science Mumbai, India. He graduated with distinction in H.S.C (Higher Secondary School Certificate) in 1994 and went on to pursue professional training in Electronics Engineering at University of Mumbai. After finishing Bachelor of Engineering in 1999, he pursued training in computer networking and software programming at ACS training institute. He is a Microsoft and Sun certified professional (MCP and SCJP). He has also pursued training for MCSE (Microsoft certified systems engineer). He joined Department of Electrical and Computer Engineering, University of Tennessee, Knoxville in 2001 to pursue graduate studies in High Performance Reconfigurable Computing (HPRC). He graduated with Master of Science (MS) in Electrical Engineering in August 2003. During his graduate school he worked with Office of Information Technology – Computing and Network Services as a Systems Administrator for campus computer laboratories. After MS, he continued his graduate education to pursue doctorate in Electrical Engineering at University of Tennessee. During his doctoral studies he has worked as a Research Assistant, a Teaching Assistant, and a Teaching Associate in the Department of Electrical and Computer Engineering at University of Tennessee. He has taught junior and senior
level classes in computer systems fundamentals and computer architecture in the capacity of an instructor. He has accepted a position with NSF center for High-Performance Reconfigurable Computing at University of Florida as a Research Scientist. He is a member of IEEE and ACM. Saumil is keenly interested in music and loves to play guitar. He hopes to pursue a career as a scientist and an educationist.

By:

Jaya Bajaj